

AD-A093 252

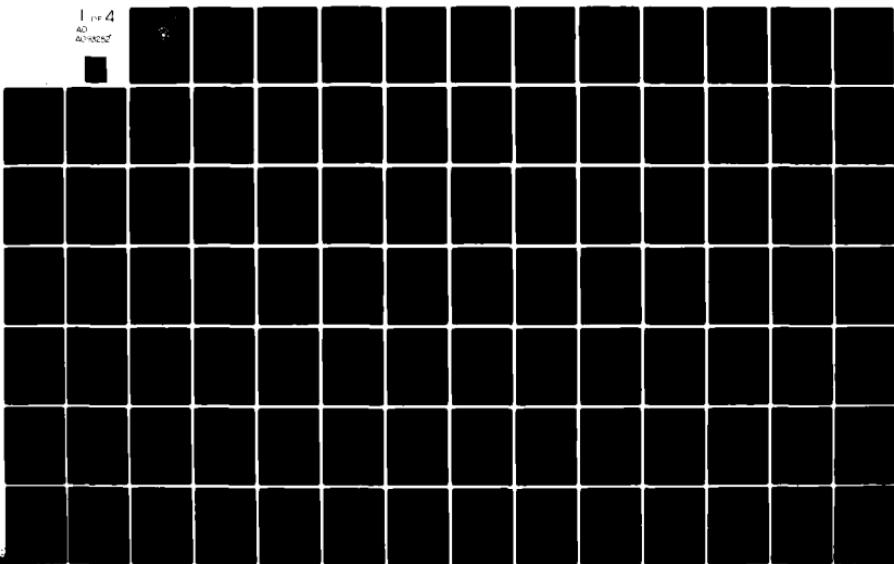
NAVAL POSTGRADUATE SCHOOL MONTEREY CA  
ADVANCED SIMULATION OF DIGITAL FILTERS. (U)  
SEP 80 G S DOYLE

F/G 9/3

UNCLASSIFIED

NL

1 of 4  
AD-9093-252



LEVEL 2

NAVAL POSTGRADUATE SCHOOL  
Monterey, California

AD A093252



# THESIS

ADVANCED SIMULATION OF DIGITAL FILTERS

by

Gerald S. Doyle

September 1980

Thesis Advisor:

D. E. Kirk

Approved for public release; distribution unlimited

80 12 29 169

SECURITY CLASSIFICATION OF THIS PAGE (When Data Entered)

| REPORT DOCUMENTATION PAGE   |   | READ INSTRUCTIONS BEFORE COMPLETING FORM |
|---|---|--|
| 1. REPORT NUMBER  | 2. GOVT ACCESSION NO.                                       | 3. RECIPIENT'S CATALOG NUMBER            |
|   |   | AD-A093 251                              |
| 4. TITLE (and Subtitle)   | 5. TYPE OF REPORT & PERIOD COVERED                          |  |
| Advanced Simulation of Digital Filters,   | Master's Thesis<br>September 1980                           |  |
| 6. AUTHOR(s)  | 7. PERFORMING ORG. REPORT NUMBER                            |  |
| Gerald S. Doyle   | 15342   |  |
| 8. PERFORMING ORGANIZATION NAME AND ADDRESS   | 10. PROGRAM ELEMENT, PROJECT, TASK AREA & WORK UNIT NUMBERS |  |
| Naval Postgraduate School<br>Monterey, California 93940   |   |  |
| 11. CONTROLLING OFFICE NAME AND ADDRESS   | 12. REPORT DATE   |  |
| Naval Postgraduate School<br>Monterey, California 93940   | September 1980  |  |
| 14. MONITORING AGENCY NAME & ADDRESS//if different from Controlling Office)   | 13. NUMBER OF PAGES   |  |
|   | 307   |  |
| 16. DISTRIBUTION STATEMENT (of this Report)   | 15. SECURITY CLASS. (of this report)                        |  |
| Approved for public release; distribution unlimited   | UNCLASSIFIED  |  |
| 17. DISTRIBUTION STATEMENT (of the abstract entered in Block 20, if different from Report)  | 18. DECLASSIFICATION/DOWNGRADING SCHEDULE                   |  |
|   |   |  |
| 19. KEY WORDS (Continue on reverse side if necessary and identify by block number)  |   |  |
| Digital Filter; Interactive Graphics; Z-Plane   |   |  |
| 20. ABSTRACT (Continue on reverse side if necessary and identify by block number)   |   |  |
| An Advanced Simulation of Digital Filters has been implemented on the IBM 360/67 computer utilizing Tektronix hardware and software. The program package is appropriate for use by persons beginning their study of digital signal processing or for filter analysis. The ASDF programs provide the user with an interactive method by which filter pole and zero locations can be manipulated. Graphical output on both the Tektronix graphics screen and the Versatec plotter are provided to observe the effects of pole-zero movement |   |  |

Approved for public release; distribution unlimited.

Advanced Simulation of Digital Filters

by

Gerald S. Doyle  
Captain, United States Army  
B.S., United States Military Academy, 1973

Submitted in partial fulfillment of the  
requirements for the degree of

MASTER OF SCIENCE IN ELECTRICAL ENGINEERING

from the

NAVAL POSTGRADUATE SCHOOL  
September, 1980

|               |  |
|---------------|--|
| Accession No. |  |
| NTIS No.      |  |
| DTIC No.      |  |
| Unnumbered    |  |
| Justification |  |
| By            |  |
| Distribution  |  |
| Availability  |  |
| Dist          |  |
| Spec          |  |

A

Author

Gerald S. Doyle

Approved by:

Dekirk

Thesis Advisor

R D Shifflett

Second Reader

Dekirk

Chairman, Department of Electrical Engineering

William M. Tolles

Dean of Science and Engineering

## ABSTRACT

An Advanced Simulation of Digital Filters has been implemented on the IBM 360/67 computer utilizing Tektronix hardware and software. The program package is appropriate for use by persons beginning their study of digital signal processing or for filter analysis. The ASDF programs provide the user with an interactive method by which filter pole and zero locations can be manipulated. Graphical output on both the Tektronix graphics screen and the Versatec plotter are provided to observe the effects of pole-zero movement.

## TABLE OF CONTENTS

|      |   |    |
|------|---|----|
| I.   | INTRODUCTION . . . . .                        | 7  |
| II.  | SELECTION OF ASDF ALGORITHMS . . . . .        | 8  |
|      | A. ALGORITHMS SELECTED . . . . .              | 9  |
|      | B. DEFINING THE DATA STRUCTURE . . . . .      | 9  |
| III. | IMPLEMENTED SOLUTION . . . . .                | 11 |
|      | A. INTERFACE WITH THE Z-PLANE . . . . .       | 11 |
|      | B. TIME RESPONSE . . . . .                    | 19 |
|      | C. FREQUENCY RESPONSE . . . . .               | 27 |
|      | D. OUTPUT PLOTS . . . . .                     | 29 |
|      | E. SUPERVISORY ROUTINES . . . . .             | 30 |
| IV.  | STRUCTURE OF ASDF COMMANDS . . . . .          | 34 |
|      | A. SUMMARY OF DATA INPUT MODES . . . . .      | 37 |
|      | 1. Interactive Graphics (IAG) . . . . .       | 37 |
|      | 2. Rectangular . . . . .                      | 38 |
|      | 3. Polar . . . . .                            | 38 |
|      | B. THE POLZRO COMMAND SUBSTRUCTURE . . . . .  | 39 |
|      | C. SUMMARY OF POLZRO SUBCOMMANDS . . . . .    | 43 |
| V.   | LOADING THE ASDF PACKAGE . . . . .            | 44 |
|      | A. LOGIN PROCEDURE . . . . .                  | 44 |
|      | B. TESTING OSX001 FOR ASDF PROGRAMS . . . . . | 45 |
|      | 1. ASDF is on OSX001 . . . . .                | 46 |
|      | 2. ASDF is not on OSX001 . . . . .            | 46 |

|   |     |
|---|-----|
| VI. USING ASDF . . . . .                                    | 50  |
| A. EXAMPLE ONE - INTERACTIVE GRAPHICS . . . . .             | 50  |
| B. EXAMPLE TWO - RECTANGULAR MODE . . . . .                 | 59  |
| C. EXAMPLE THREE - POLAR MODE . . . . .                     | 80  |
| VII. ADDITIONAL EXAMPLES . . . . .                          | 94  |
| VIII. INTERPRETATION OF ASDF OUTPUT . . . . .               | 201 |
| IX. SUMMARY AND CONCLUSIONS . . . . .                       | 212 |
| APPENDIX A: PROBABLE SOLUTIONS FOR DIFFICULTIES. . . . .    | 216 |
| APPENDIX B: IMPORTANT SUBROUTINES AND VARIABLES. . . . .    | 218 |
| APPENDIX C: STRUCTURE FOR ASDF TEXT FILE . . . . .          | 224 |
| APPENDIX D: JCL FOR EXEC HRDSCPY COMMAND . . . . .          | 226 |
| APPENDIX E: SOURCE DECK FOR ASDF191 EXEC . . . . .          | 227 |
| APPENDIX F: SOURCE DECK FOR ASDF192 EXEC . . . . .          | 229 |
| APPENDIX G: SOURCE DECK FOR ASDF COMMAND: POLZRO. . . . .   | 233 |
| APPENDIX H: SOURCE DECK FOR ASDF COMMAND: RESPONSE. . . . . | 276 |
| APPENDIX I: SOURCE DECK FOR ASDF COMMAND: HRD\$CY. . . . .  | 289 |
| LIST OF REFERENCES. . . . .                                 | 306 |
| INITIAL DISTRIBUTION LIST . . . . .                         | 307 |

## ACKNOWLEDGEMENTS

The author wishes to acknowledge the people who made this effort possible. Of greatest importance is the love and guidance provided by his parents, Margaret and C. E. Doyle, and sister, Evelyn. It is to them that this thesis is dedicated. Special mention goes to Professor Richard Hamming for his insight and explanations of finite precision effects in digital filters. Thanks are due to Professors D. E. Kirk and R. D. Strum for their suggestions and comments in structuring this work. For their assistance with system problems, thanks are due to J. Foust, F. Wheeler, R. Donat, and H. Doleman. Moreover, thanks are due to E. Christian, and M. F. Bradley for their assistance in preparing the manuscript. Of no less importance are the evening computer center operators J. Kallweit, M. Anderson, and E. Donnellan for their consideration and assistance in processing the figures. However, the author alone is responsible for any shortcomings in this thesis, for the ultimate choice of what was done was his.

## I. INTRODUCTION

Digital methods have recently begun to dominate the selection of transmission and filtering schemes. When the student first confronts the discrete domain, he encounters a series of unfamiliar concepts. While most of the discrete concepts have parallels in the continuous or s-domain, this dualism is not apparent initially.

The programs comprising the Advanced Simulation of Digital Filters (ASDF) provide the user with a convenient method for developing intuition in the discrete domain. This is achieved by allowing the user to generate digital filters by directly entering the poles and zeros into a graphics terminal. The ASDF programs then perform the calculations required to display the characteristics of the user generated filter.

The overriding objective of the ASDF program package is to provide the user with an interactive method for modifying the filter pole/zero locations in the z-plane, as well as to compute the filter responses. Both time and frequency responses are computed and displayed graphically on the Tektronix 4012 graphics terminal. [Ref. 9]

## II. SELECTION OF ASDF ALGORITHMS

There are several parameters which are particularly important in selecting the algorithms used in the ASDF programs. Since one of the primary objectives of these programs is to provide the user with clear explanations of methods for computing digital filter characteristics, direct or straightforward methods should be used. The importance of developing a user's intuition for the discrete domain and digital filters suggests that graphical rather than numerical outputs would be most appropriate. The use of graphical outputs to characterize a filter's responses implies minimum importance of precision in these results. Since the reason for computing the filter characteristics is to develop the user's intuition for the discrete domain, there are no pressing constraints on the selected algorithms with regard to computational efficiency, speed, or memory space utilization. In fact, the final ASDF package spends the greatest portion of its execution time making the interface with the z-plane, and the form of the output easy to understand and to use. The greatest part of the memory space utilized for the ASDF programs is consumed in the interfacing processes rather than in the methods by which the data is stored, used, or computed.

#### A. ALGORITHMS SELECTED

Because of the above stated objectives, a simple algorithm was selected for computation of time domain responses of digital filters. Once the user enters the desired pole and zero locations, a direct-form-two difference equation representation of the filter is generated [Ref. 5]. The unit sample sequence is used for the filter input, the difference equations are solved recursively in the discrete time domain and the unit sample response is recorded as the output. The unit step response is calculated by a similar method.

It is known that the direct-form-two filter implementation is very sensitive to parameter variations, and as such cannot be utilized in situations requiring extreme accuracy. The advantages associated with simplicity of understanding the algorithms, the ease of programming the general case, and the deemphasis of accuracy in outputs for marginally stable filters outweighs this disadvantage.

#### B. DEFINING THE DATA STRUCTURE

A detailed description of the important variables in the ASDF programs is given in Appendix B. There is, however, an overriding data structure common to all portions of the ASDF package which is important.

The array POLZRO holds the locations of the poles and zeros of the filter under analysis. In all cases, zeros are

stored in POLZRO(I,J) for values of I from one to ten. Pole locations are stored in POLZRO(I,J) for values of I from eleven to twenty. Only the top half plane pole of each complex pair is stored. There are five sections of POLZRO(I,J), i.e. values of J from one to five. POLZRO(I,1) is the real part of the rectangular representation of the ith root. POLZRO(I,2) is the imaginary part of the rectangular representation of the ith root. POLZRO(I,3) and POLZRO(I,4) are the magnitude and angle portions of the ith root location in polar form. POLZRO(I,5) is the root type designator. Root type designators are: one for real zeros, two for complex zeros, three for real poles, and four for complex poles.

The array IROOTS(I) holds the numbers of roots of each type of root already entered into the system. IROOTS(1) and IROOTS(3) hold the number of real zeros and poles, respectively. IROOTS(2) and IROOTS(4) hold the number of complex zero and pole pairs, respectively.

The variable IERROR is the error flag, which is set whenever the user generates an error. There are numerous possible errors. These include trying to delete roots which have not been entered, or adding roots which cause the maximum system order to be exceeded.

### III. IMPLEMENTED SOLUTION

Having determined the general form of the solution it remained to generate the software implementation. There were five major areas to be programmed: the interface with the z-plane, the time response, the frequency response, the plotting of output curves, and the supervisory routines.

#### A. INTERFACE WITH THE Z-PLANE

Since the method by which the user modifies the pole and zero locations in the z-plane is of no theoretical interest, the discussion of this implementation will be brief. Extensive coverage of the subroutines employed and the definitions of the variables used is reserved for Appendix B.

The ASDF command which allows the user to make pole-zero modifications in the z-plane is POLZRO. This command initiates execution of a load module which is structured as depicted in figure 3-1. Each of the boxes shown represents a subroutine. Lines with arrow heads on both ends indicate that program control passes to the subroutine and then directly back to the calling routine with no intermediate branches. The main program, MAIN, initializes the required arrays, and tests to ensure that the user has generated a realizable causal filter.

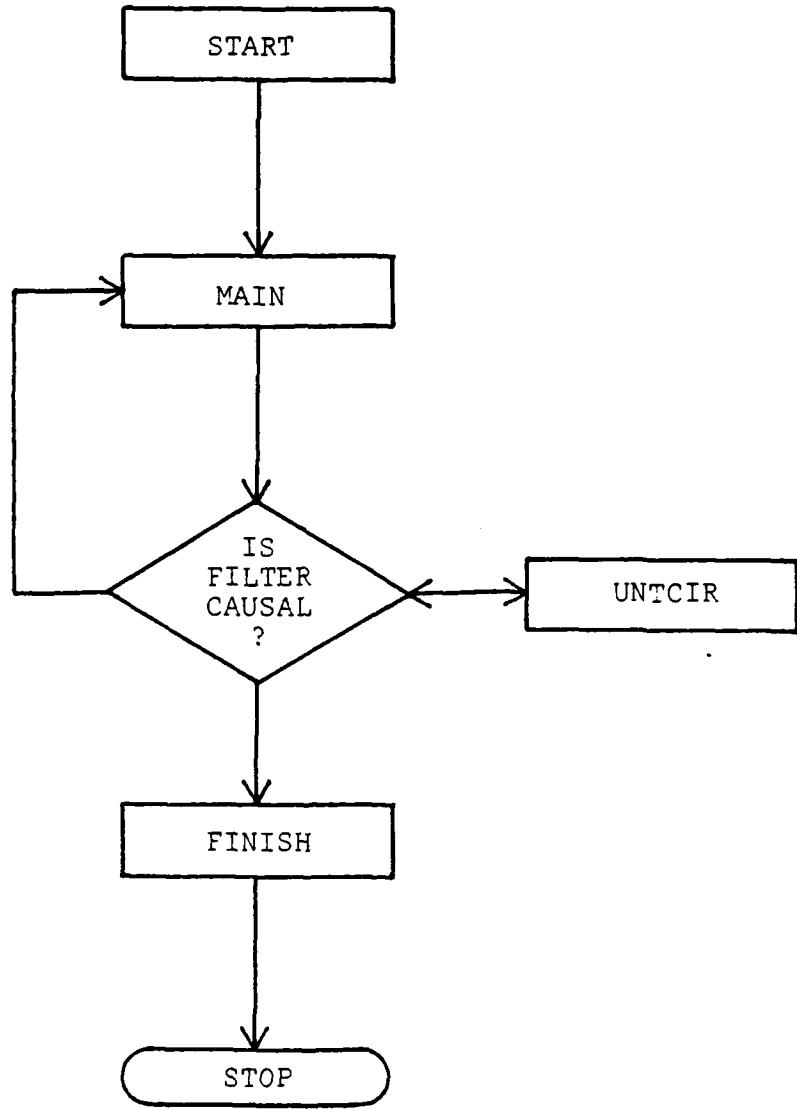


Figure 3-1 Flowchart Of POLZRO

The actual interaction with the z-plane is accomplished in subroutine UNTCIR. The structure of UNTCIR is diagrammed in figure 3-2. The large double ended arrow indicates that there are many subroutines of the form CRRMM. The subroutines LETTER and BOXUC generate the unit circle and command array. PLOT-10 software [Ref. 10] statements determine the location of the user positioned cursor. This cursor position is adjusted with software tabs to one of twenty-six possible locations. Based on the X and Y location of the adjusted cursor position a specific subroutine is selected for execution. The flashing alphanumeric cursor is positioned in the selected command box using the adjusted cursor location as a reference. The subroutine then reads two alphanumeric characters typed by the user. The combination "space", "e" indicates that the user wishes the selected subroutine to be executed. The combination "space", "x" indicates that the user wishes to terminate the pole zero manipulation phase of the program.

All of the commands which change the status of the z-plane have names of the form CRRMM where C is either "A" for add root(s) or "D" for delete root(s). The RR indicates root type: RZ - real zero, CZ - complex zero, RP - real pole, CP - complex pole. The MMM stands for the mode of data entry. IAG stands for interactive graphics i.e. the roots will be adjusted with the cursor. POL and RCT stand for polar and rectangular, respectively. The general

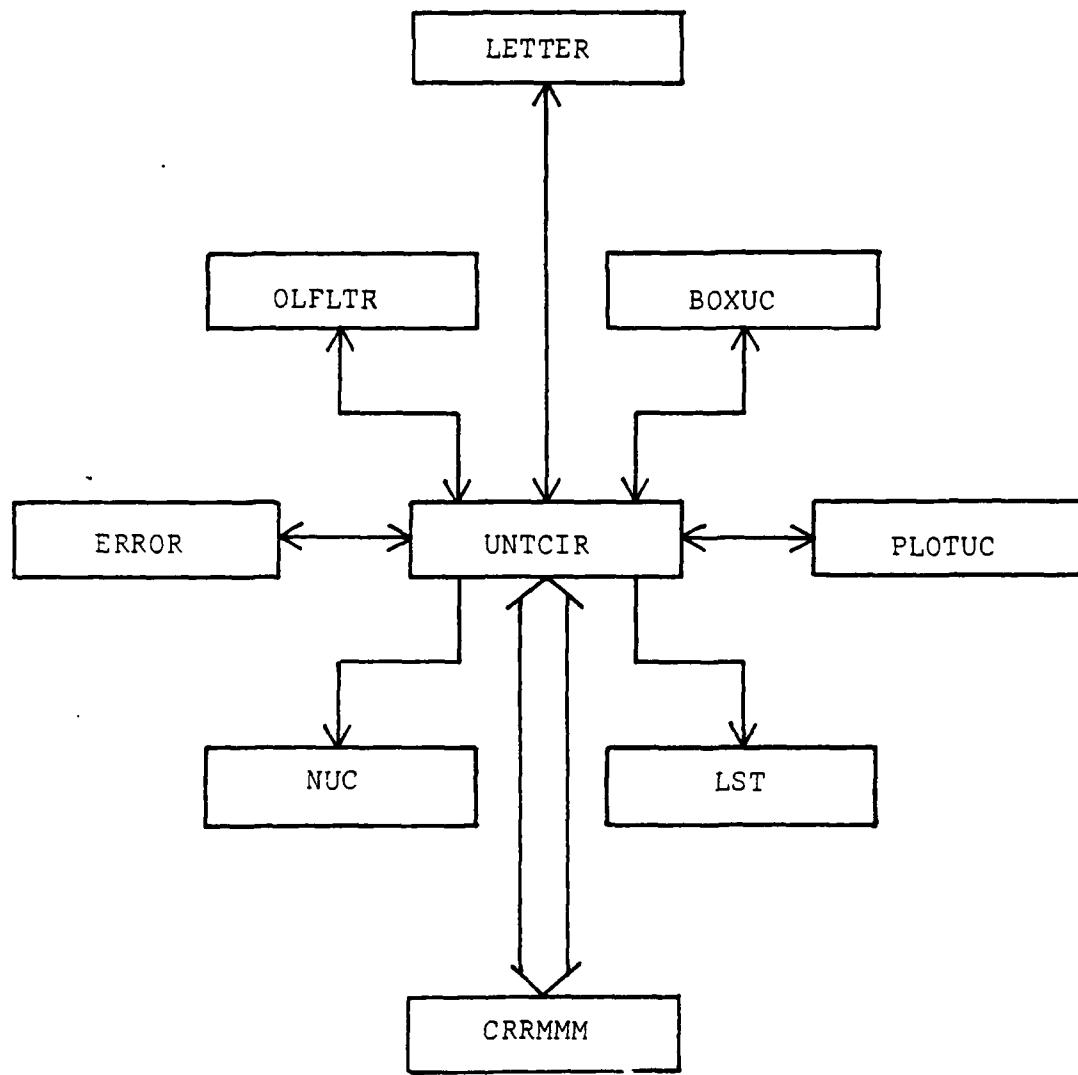


Figure 3-2 Structure Of Subroutine UNTCIR

structure of the CRRMM subroutines is described in figure 3-3.

All CRRMM subroutines follow the same general pattern. The POLZRO table is checked to determine whether or not the issued command is valid. Poles and zeros must be present before they can be deleted. There cannot be more than ten poles or ten zeros. The desired pole or zero location is next acquired. For subroutines adding roots<sup>1</sup> the entered location is that of the root(s) to be added. For subroutines deleting roots the entered location is any location near the root(s) to be deleted. Using subroutine LOCATE, the POLZRO table is searched for the root of the correct type which is nearest the specified location. This nearest root is then highlighted. In all cases, except when adding roots in the IAG mode, the user is asked whether or not the correct location has been determined. Once the root location is verified the root is added and plotted with subroutines STRRTS and PLOTRT. For subroutines deleting roots the POLZRO table is adjusted with subroutine UPDATE and the unit circle is redrawn.

The user may make an error in carrying out the above steps, i.e., by placing a pole outside the unit circle, by exceeding the maximum system order, or by entering a zero outside ten units from the origin. In each of these cases an

---

<sup>1</sup> Hereafter, poles and zeros will be referred to as roots.

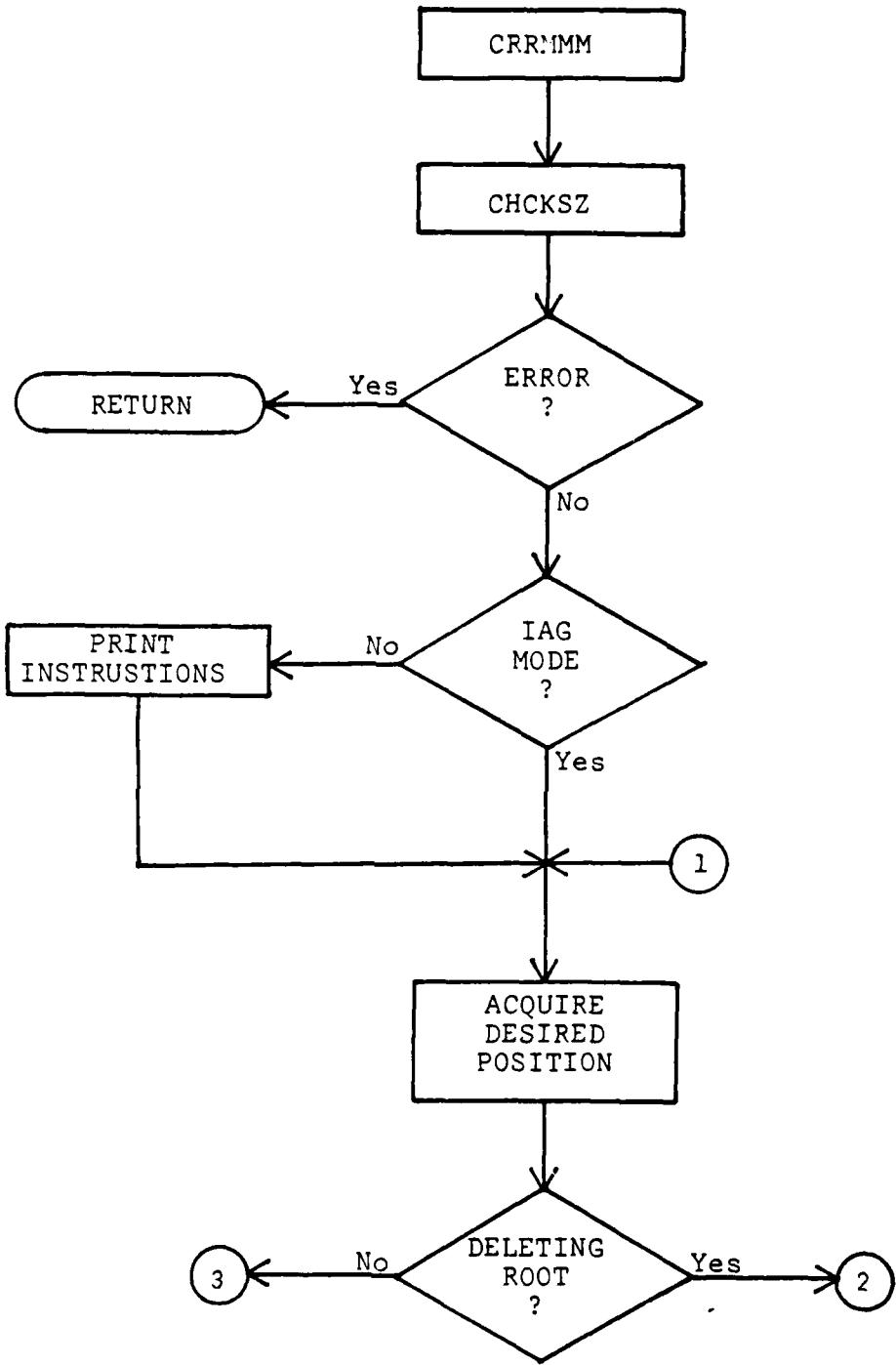


Figure 3-3a Structure of CRRMM Subroutines

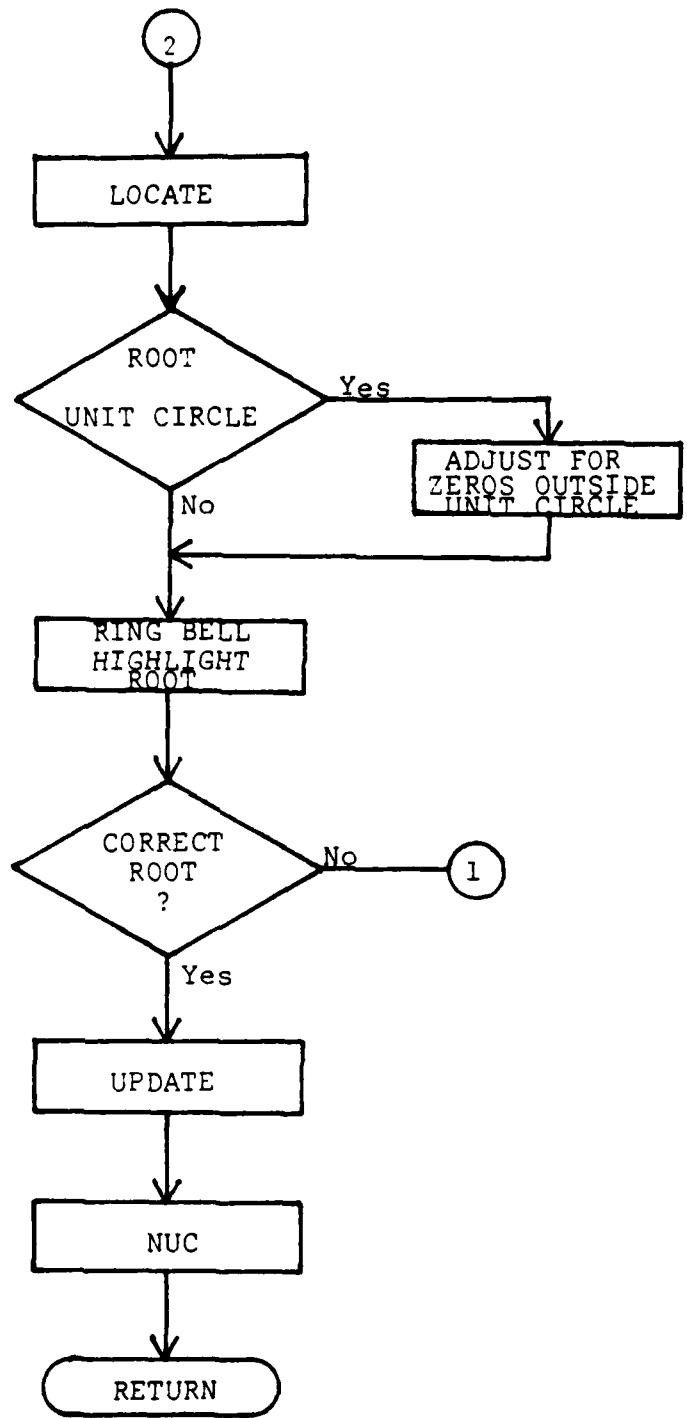


Figure 3-3b Structure Of CRRMM Subroutines Continued

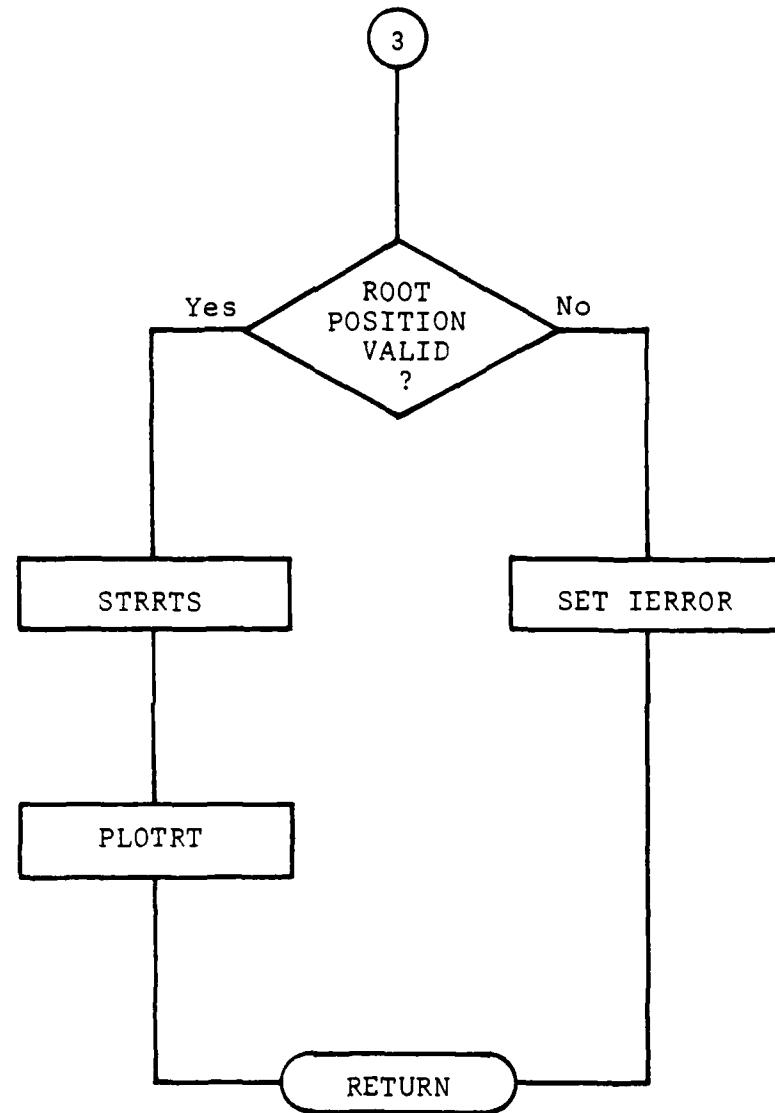


Figure 3-3c Structure Of CRRMM Subroutines Continued

error flag is set. Subroutine ERROR handles the printing of messages and subroutine LST prints a listing of the current filter status before the program resumes.

## B. TIME RESPONSE

The transfer function of a digital filter is defined in equation 3.1. The  $z_i$ ,  $p_i$ ,  $a_k$ , and  $b_r$  will be defined in a subsequent section. The variable A is an arbitrary constant assigned by the user and is called the filter gain.

$$H(z) = \frac{A \prod_{i=1}^M (z-z_i)}{\prod_{i=1}^N (z-p_i)} = \frac{\sum_{r=0}^M b_r z^{r-N}}{1 - \sum_{k=1}^N a_k z^{-k}} \quad (3.1)$$

Inherent in generating the time domain response with a direct-form-two filter implementation are the determination of the coefficients  $a_k$  and  $b_r$  in equation (3-1), and the computation of the unit sample and unit step sequences. Having determined the filter coefficients, the time domain response of the filter is determined by using the appropriate filter input sequence and recording the output of the filter for the desired number of points. This is accomplished by recursively solving a difference equation which characterizes the filter for 1024 time points. The standard direct-form-two filter implementation is shown in figure 3-4. The  $z^{-1}$  terms represent unit time delays. This

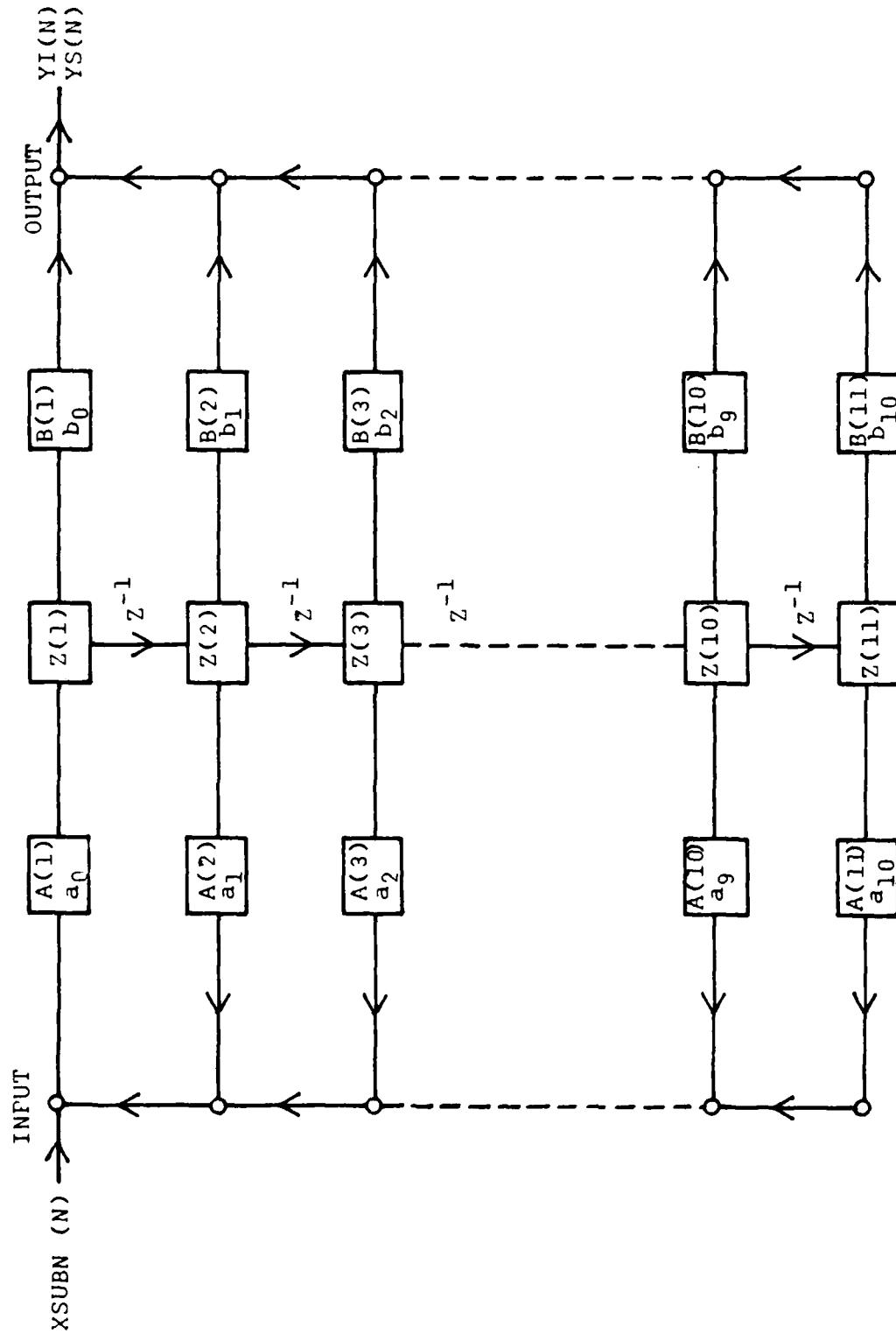


Figure 3-4 Direct Form Two Filter Implementation

figure corresponds to the difference equations:

$$y(n) = \sum_{k=1}^N a_k y(n-k) + \sum_{r=0}^N b_r x(n-N+r) \quad (3.2)$$

To compute the filter's time response, three operations are required: calculate the  $a_k$  and  $b_r$  coefficients, generate the input sequence  $x(k)$ ,  $k=0, 1, \dots, 1024$ , solves the difference equations and stores the filter output values. There are four central subroutines which perform these operations: ASUBK, BSUBR, RSPNSE, and COEFF. Subroutines ABSUK, BSUBR, and COEFF generate the filter coefficients starting with the pole and zero locations specified. Subroutine RSPNSE solves the difference equations by coordinating the other three routines, generating the appropriate input sequence, and storing the output sequence values.

The ASUBK and BSUBR subroutines are identical in structure and purpose. ASUBK computes the degree of the denominator polynomial as two times the number of complex pole pairs plus the number of real poles. A complex vector is formed named POLES, which holds a listing of all the poles of the filter under analysis. The POLZRO array stores real poles in the form  $X+j0$ . Only the top half plane pole of each complex pole pair is stored, i.e.,  $(X+jY)$ , where X and Y are non-negative. The vector POLES has entries for all real poles and both poles of each complex pole pair.

Once the POLES vector has been generated the subroutine COEFF multiplies out the factors of the form  $(z-p_i)$  to generate the coefficients of the denominator polynomial.

The algorithm for multiplying out the denominator polynomial is essentially the same as would be done by hand. multiplication of a series of literal factors of the form  $(z-p_i)$ . The vector POLES is passed to the COEFF subroutine as the vector V. Since the denominator factors are of the form  $(z-p_i)$ , the V vector is changed to hold the values  $-p_i$ . If the system is of order less than ten, the remaining positions of V are filled with zeros. The degree of the denominator polynomial is subsequently used to determine how many poles are actually located at the origin.

The vectors used in the subroutine COEFF hold the coefficients for the polynomial being generated. The literal powers of "z" are suppressed. The vector H1 always contains the partial product of the K factors previously multiplied together. The vector H2 represents the old partial product times the "z" of the  $(z-p_i)$  factor. Since the coefficient of "z" is always one, H2 is a left shifted version of H1. The vector H3 represents the partial product times the next pole location ( $p_i$ ). This next  $-p_i$  value is stored in V(1). The new H1 vector is formed by adding the H2 and H3 vectors. H1 now contains the product of the first  $K+1$  factors. The values in the V vector are next shifted such that the next pole location to be multiplied is always

in the V(1) position. These four steps are repeated ten times to generate the coefficients of the complete polynomial in "z". The formula for the transfer function requires coefficients of the denominator polynomial in terms of  $z^{-1}$  so the order of the coefficients is reversed.

Figure 3-5 depicts several iterations of the algorithm used in the COEFF subroutine. Figure 3-5a shows the initial conditions for each of the vectors defined in the above paragraph. Figure 3-5c shows the values of the vectors after the first iteration. Figure 3-5f shows the vector values after the second iteration. The third and subsequent iterations follow this pattern.

In precisely the same way as described above, the  $a_k$  coefficients are generated with the ASUBK subroutine. The zero locations are stored in POLZRO exactly as are the poles. The generation of the vector ZEROS and the use of the subroutine COEFF parallels the BSUBR subroutine exactly.

The significant variables in subroutine RSPNSE are: XSUBN, INPUT, OUTPUT, FLTRGN, A, and B. The vectors A and B hold the already computed values of  $a_k$  and  $b_k$ . A(1) holds  $a_0$ ; A(2) holds  $a_1$  . . . A(11) holds  $a_{10}$ . The  $b_r$  are stored similarly in the B vector. XSUBN is the current value of the input sequence. INPUT is the value of the node so labeled in figure 3-4. OUTPUT is similarly noted on figure 3-4. FLTRGN is the value of the filter gain, and is assigned by the user. The vector Z holds the delayed INPUT values.

|    | V |   |   |   |   |   |                 |
|----|---|---|---|---|---|---|-----------------|
| H1 | . | . | . | 0 | 0 | 0 | 1               |
| H2 | . | . | . | 0 | 0 | 0 | 0               |
| H3 | . | . | . | 0 | 0 | 0 | 0               |
|    |   |   |   |   |   |   | -p <sub>1</sub> |
|    |   |   |   |   |   |   | -p <sub>2</sub> |
|    |   |   |   |   |   |   | -p <sub>3</sub> |
|    |   |   |   |   |   |   | -p <sub>4</sub> |
|    |   |   |   |   |   |   | .               |
|    |   |   |   |   |   |   | .               |
|    |   |   |   |   |   |   | .               |

Figure 3-5a. Initial Conditions Of COEFF Vectors.

|    | V |   |   |   |   |   |                 |
|----|---|---|---|---|---|---|-----------------|
| H1 | . | . | . | 0 | 0 | 0 | 1               |
| H2 | . | . | . | 0 | 0 | 1 | 0               |
| H3 | . | . | . | 0 | 0 | 0 | -p <sub>1</sub> |
|    |   |   |   |   |   |   | -p <sub>1</sub> |
|    |   |   |   |   |   |   | -p <sub>2</sub> |
|    |   |   |   |   |   |   | -p <sub>3</sub> |
|    |   |   |   |   |   |   | -p <sub>4</sub> |
|    |   |   |   |   |   |   | .               |
|    |   |   |   |   |   |   | .               |
|    |   |   |   |   |   |   | .               |

Figure 3-5b. Values Of COEFF Vectors Before The End Of The First Iteration.

|    |   |   |   |   |   |   |        |
|----|---|---|---|---|---|---|--------|
|    |   |   |   |   |   | V |        |
| H1 | . | . | . | 0 | 0 | 1 | $-p_1$ |
| H2 | . | . | . | 0 | 0 | 1 | 0      |
| H3 | . | . | . | 0 | 0 | 0 | $-p_1$ |

Figure 3-5c. Values Of COEFF Vectors starting The Second Iteration.

|    |   |   |   |   |   |        |            |
|----|---|---|---|---|---|--------|------------|
|    |   |   |   |   |   | V      |            |
| H1 | . | . | . | 0 | 0 | 1      | $-p_1$     |
| H2 | . | . | . | 0 | 1 | $-p_1$ | 0          |
| H3 | . | . | . | 0 | 0 | $-p_2$ | $+p_1 p_2$ |

Figure 3-5d. Values Of COEFF Vectors before The End of The Second Iteration.

|    | V |   |   |   |                |             |        |
|----|---|---|---|---|----------------|-------------|--------|
| H1 | . | . | . | 1 | $-(p_1 + p_2)$ | $(p_1 p_2)$ | $-p_3$ |
| H2 | . | . | . | 1 | $-p_1$         | 0           | $-p_4$ |
| H3 | . | . | . | 0 | $-p_2$         | $(p_1 p_2)$ | $-p_5$ |
|    |   |   |   |   |                |             | $-p_6$ |
|    |   |   |   |   |                |             | .      |
|    |   |   |   |   |                |             | .      |
|    |   |   |   |   |                |             | .      |

Figure 3-5e. Values Of COEFF Vectors Starting The  
Third Iteration.

|    | V |   |                |                   |                  |        |  |
|----|---|---|----------------|-------------------|------------------|--------|--|
| H1 | . | . | 1              | $-(p_1 + p_2)$    | $(p_1 p_2)$      | $-p_3$ |  |
| H2 | . | 1 | $-(p_1 + p_2)$ | $(p_1 p_2)$       | 0                | $-p_4$ |  |
| H3 | . | 0 | $-p_3$         | $+(p_1 + p_2)p_3$ | $-(p_1 p_2 p_3)$ | $-p_5$ |  |
|    |   |   |                |                   |                  | $-p_6$ |  |
|    |   |   |                |                   |                  | .      |  |
|    |   |   |                |                   |                  | .      |  |
|    |   |   |                |                   |                  | .      |  |

Figure 3-5f. Values Of COEFF Vectors before The End Of The  
Third Iteration.

Z(1) is no delay; Z(2) is delayed one time unit; Z(3) is delayed two time units, etc.

The subroutine RSPNSE generates the appropriate input sequence. For the unit sample response the input sequence is 1, 0, 0, 0, . . . . For the unit step response the input sequence is 1, 1, 1, 1, . . . . The appropriate value of XSUBN is determined by the type of input sequence. The variable INPUT is then computed to be the sum of XSUBN and the  $a_k$ 's times the delayed INPUT values. The filter output is the sum of the  $b_r$ 's times the delayed INPUT values. These output values are then multiplied by the filter gain, FLTRGN, and stored in the appropriate array: YI for the unit sample response, YS for the unit step response.

### C. FREQUENCY RESPONSE

For discrete systems, the frequency response is found by evaluating the system transfer function at points on the unit circle. Subroutine FRQNCY generates both the phase and the magnitude of the transfer function.

The important variables in the FRQNCY subroutine are: AA, BB, THETA, Z, NNUM, and NDEN. The variables AA and BB are the double precision values of the A and B vectors described in the section on time response. THETA is the angular displacement around the unit circle for which a value of the frequency response is calculated. Z is the

classical z-plane variable:

$$Z = \exp(j \text{ THETA}) \quad (3.3)$$

NNUM is the number of numerator terms. NDEN is the number of denominator terms.

The frequency response is computed for 1024 points around the unit circle. All points computed are for THETA greater than zero and less than  $\pi$ . The values of Z for THETA greater than  $-\pi$  and less than zero are neither computed nor plotted since the magnitude of the transfer function is an even function of THETA and the phase response is an odd function of THETA.

The generation of the  $a_k$  and  $b_r$  coefficients has already been discussed in the section on time domain response. The evaluation of  $H(z)$  is straightforward. The value of THETA is incremented through 1024 steps from zero to  $\pi$ . For each value of THETA generated, the value of Z is computed. The value of  $H(z)$  is then computed in two parts. The numerator is the sum of NNUM terms of the form  $b_r$  times  $z^{-r}$  for  $r=0, 1, 2, \dots, NNUM-1$ <sup>1</sup>. The denominator is one minus the sum of (NDEN-1) terms of the form  $a_k$  times  $z^{-k}$  for  $k=1, 2, 3, \dots, NDEN-1$ <sup>2</sup>. Dividing numerator by denominator

---

<sup>1</sup> NNUM is equal to the degree of the numerator plus one.

<sup>2</sup> NDEN equals the degree of the denominator plus one.

yields  $H(z)$ . The phase of  $H(z)$  is then determined using the principal values of the arctangent function; the results are stored in the vector  $YP$ . The magnitude of  $H(z)$  is computed, multiplied by  $FLTRGN$ , the filter gain, and subsequently stored in the vector  $YM$ .

#### D. OUTPUT PLOTS

The output plots generated by ASDF are generated by two different software programs each being different implementations of the same plotting requirements. One set of plots is generated using PLOT-10 software on the Tektronix 4012 terminal. Another set of plots utilizes the Versatec plotter and associated software. [Ref. 7] The PLOT-10 software is adequately covered in reference 10. The Versatec software is explained in Technical Note-034 in the computer center.

The plots which are generated on both devices are essentially the same. There are five plots generated on the 4012 terminal: unit sample response, unit step response, phase response, magnitude of the transfer function, and magnitude of the transfer function in decibels. Both of the time domain plots are terminated when the output value has stabilized to within one percent of the maximum generated system output. All 1024 points of the phase and magnitude plots are plotted.

The form of the Versatec output is similar to that of the 4012. One additional plot is included. It shows the unit circle with poles and zeros of the filter being analyzed. Plotting is terminated when the filter output stabilizes to within one percent of the maximum system output generated.

On both devices, the values of unit sample response are stored in a vector YI and plotted with subroutine PLTIMP. The unit step response values are stored in YS, and plotted with subroutine PLTSTP. The phase response is stored in vector YP. The magnitude of the transfer function is stored in vector YM. The magnitude of the transfer function in decibels is stored in YMDB. The three vectors YP, YM, and YMDB are all plotted with subroutine PLTTRF. The Versatec plot of the unit circle is generated with subroutine UNTCR. The 4012 plot of the unit circle and command array are generated with the subroutine UNTCIR.

#### E. SUPERVISORY ROUTINES

There are three supervisory routines used with the ASDF programs. These supervisory routines make the loading of ASDF transparent to the user. There is a substantial amount of file manipulation required to store and load the ASDF programs. A knowledge of the hardware and software available for these purposes is not particularly useful to the user. For these reasons, the supervisory routines are discussed only briefly. Two of these routines are based on

CP/CMS and IBM EXEC environment; the third is written in the IBM-360 Job Control Language.

The JCL program moves the ASDF program from its permanent storage location on DISK02 to the CP/CMS disks OSX001. The two EXEC routines generate an appropriate CP/CMS work space, and manipulate the ASDF text file into a usable form.

The EXEC program ASDF191 resides on the user 191-P-disk. This routine automatically requests and formats ten cylinders of temporary disk space. The ASDF TEXT file is moved from the OSX001 disk to the newly created temporary disk space 192-T. Once in place, The ASDF TEXT file name is changed to ASDF EXEC to generate the next file with the correct file type. ASDF EXEC is then edited to remove the first set of data cards which hold the ASDF192 EXEC program. The 192-T-disk is released and the user is requested to type two commands to the system. The "login 192 P" command makes the 192 disk the P-disk. The "EXEC ASDF192" command begins the execution of the second EXEC file.

The general ASDF192 EXEC structure is depicted in figure 3-6. ASDF192 EXEC is created by ASDF191 EXEC and resides on disk 192. In a manner similar to ASDF191, ASDF192 splits the ASDF TEXT file, which contains all of the component parts of the ASDF program, into a series of smaller files. Once all files have been separated, titles are altered appropriately, text files are loaded into core, and load

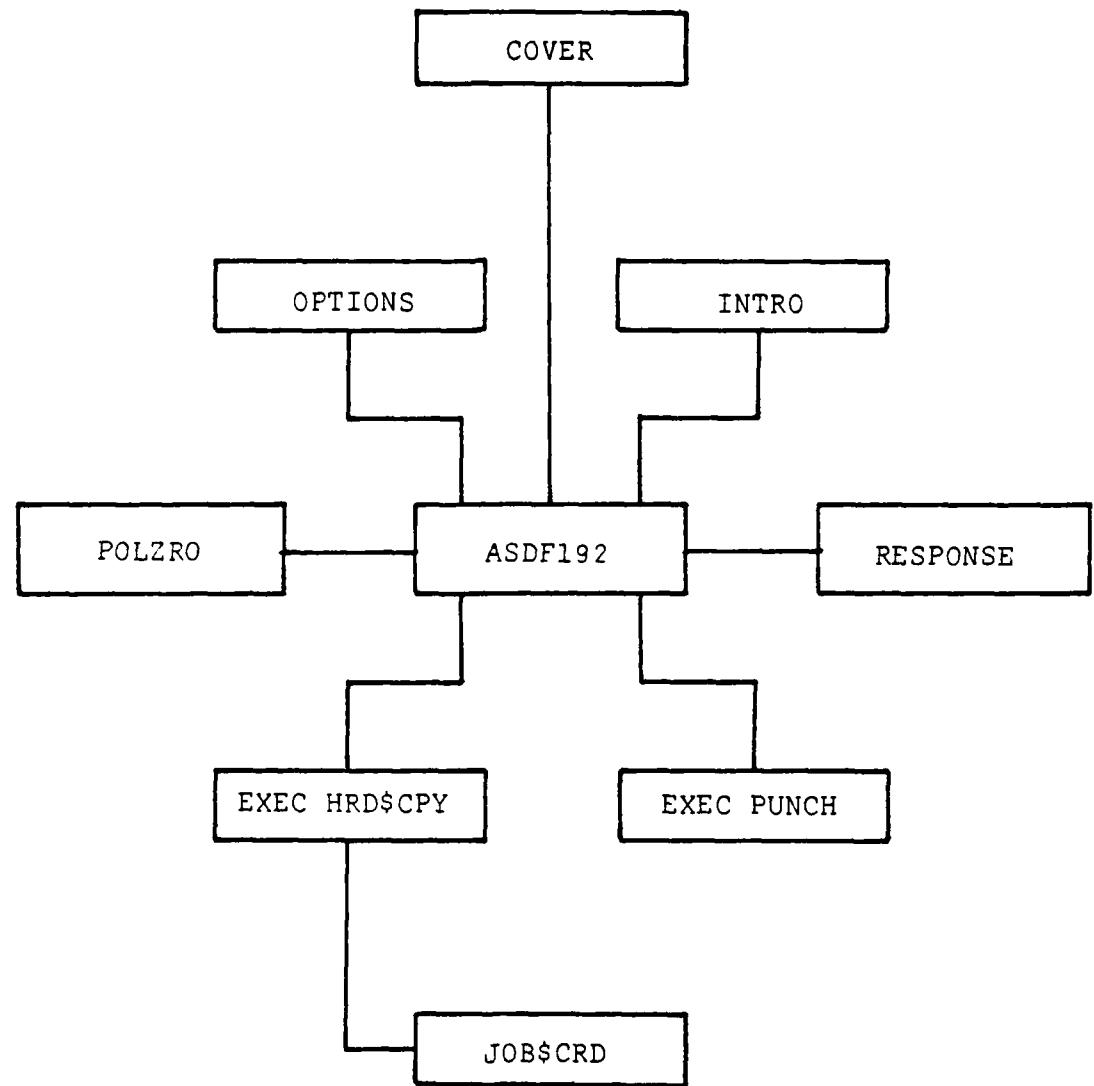


Figure 3-6 Structure Of ASDF192 EXEC

modules are generated. ASDF192 then reverts to an infinite loop, reading and implementing the desired user command. There are six user commands available to the user: POLZRO, RESPONSE, EXEC PUNCH, EXEC HRD\$CPY, OPTIONS, and INTRO. The applicability of these commands is briefly discussed in chapter four. This brief description is also presented by executing the OPTIONS command once ASDF has been loaded.

#### IV. STRUCTURE OF ASDF COMMANDS

The ASDF program generates the time and frequency responses of realizable digital filters of order ten or less. Chapter three describes the algorithms used for these computations. The procedure for executing the ASDF program generally consists of two distinct steps. The first step is to enter the poles and zeros of the filter to be analyzed. The second step is to perform the calculations required to generate and plot the desired filter responses. There are six commands which may be executed within the ASDF environment providing the user with the ability to control the form of the output, to enter the poles and zeros of the filter, and to clarify most questions pertaining to the meaning and use of the general commands. The six fundamental commands available to the user are: OPTIONS, INTRO, POLZRO, RESPONSE, EXEC PUNCH, and EXEC HRDSCPY. Only the POLZRO command has a subordinate command structure. All of these commands are issued by typing the command on the terminal keyboard in response to: \*ASDF-RE.

The OPTIONS command provides a listing of all commands available to the user. Each command is accompanied by a brief description of its intended use.

The INTRO command writes on the screen six pages of information pertaining to the POLZRO command substructure.

INTRO includes a general description of the data input modes, and a description of several input situations with the appropriate executable commands.

The POLZRO command allows the user to modify or create a filter in the z-plane. All adjustment of poles and zeros must take place with this command. By issuing this command the user may add and delete poles and/or zeros as well as adjust the filter gain constant. The commands which are issued within the POLZRO environment are described in a later section of this chapter.

The RESPONSE command displays the characteristics of the filter being created by the user. Five displays are presented: unit sample response, unit step response, phase of the transfer function, magnitude of the transfer function, and the magnitude of the transfer function in decibels.

The EXEC PUNCH command allows the user to punch a card deck of the filter pole and zero locations on the offline punch. This punched output can be picked up in room I-140 of the computer center. The cards punched by this command may be subsequently reentered into the system so that this particular filter can be referenced or modified at a later date.

When the user desires to enter a filter in this way, the punched cards are presented to one of the computer operators over the counter in room I-140. The cards are punched in

the correct format for direct submission into the CP/CMS card reader. The operator subsequently reads this deck into the user's virtual card reader. As the user signs onto a terminal and gains access to CP/CMS, the computer includes an additional message in the standard login typeout showing that the user has a virtual reader file. This message is of the form:

FILES:- 01 RDR, NO PRT, NO PUN

When the user wishes to access this old filter data he must execute the CP/CMS command OFFLINE READ \*. The OFFLINE READ command will read the punched card filter data from the user's virtual card reader, and generate a file on the user's disk space entitled FILE FT01F001. Any files with this name present before the OFFLINE READ command is issued will be over-written by the new file. If the user does not wish to lose an older FILE FT01F001, he should use the CP/CMS ALTER command to change the name of the old file that he wishes to protect. Once the user has successfully loaded the ASDF program, the ASDF signature i.e., \*ASDF-RE, is presented. The OFFLINE READ command may be issued any time that this signature appears.

The EXEC HRDSCPY command is available only when the SUBMIT function of CP/CMS is functioning. When the SUBMIT command is not functional a message is sent to the user during the login procedure which states that SUBMIT is not available. the output from this command is ultimately

available in the computer center, and consists of two parts. The first part of the output is the numerical listing of the values of the responses computed by the ASDF program. The EXEC HRD\$CPY command is the only command which will allow the user access to these numerical values. The second part of the output is a series of Versatec plots, each similar to the screen presentations of the RESPONSE command, with one additional plot of the unit circle and pole/zero locations. When the EXEC HRD\$CPY command is executed the ASDF program will ask several questions, using the responses to generate a JOB card. The response to the "ENTER DESIRED JOB NAME" is the title which appears on the final output. ASDF then submits the filter characteristics to the operating system for processing. The hard copy output will be found in the standard output boxes.

#### A. SUMMARY OF DATA INPUT MODES

There are three modes through which the poles and zeros may be entered into the z-plane: 1) interactive graphics, 2) rectangular, and 3) polar. Each of these modes has particular attributes and limitations.

##### 1. Interactive Graphics (IAG)

This mode was designed to enter poles and zeros rapidly, in cases where accuracy is not of prime importance. The interactive graphics mode is characterized by the appearance of the graphics cursor (the intersection of two

lines which trace across the terminal screen). The position of the cursor is controlled by the two thumb wheels located to the right of the interactive ASCII keyboard on the Tektronix 4012 terminal. The coverage of the interactive graphics cursor is limited to values of X and Y greater than -1.1 and less than +1.1. Zeros outside this area must be entered with either the polar or rectangular commands. Careful adjustment of the cursor can usually locate poles or zeros within .002 units of the desired location. Poles must be located within the unit circle.

### 2. Rectangular

This mode was designed to enter from the terminal keyboard, poles and zeros which are known in rectangular coordinates. It is slower than the interactive graphics mode because there is a significant amount of screen rewriting required. The rectangular mode allows much greater accuracy in the location of poles and zeros. Poles may not be entered on or outside the unit circle. Zeros must be located within ten units of the z-plane origin.

### 3. Polar

This mode was designed to enter from the terminal keyboard, poles and zeros which are known in polar coordinates. This mode is also slower than the interactive graphics mode. It allows poles and zeros to be entered to any permissible position in the z-plane. Poles must be entered within the unit circle. Zeros must be entered within

ten units of the z-plane origin. Each polar command has a description of the constraints on the data to be entered automatically written on the screen. This mode is particularly appropriate when constructing all-pass linear phase filters.

#### B. THE POLZRO COMMAND SUBSTRUCTURE

In an attempt to maximize execution speed, a minimum of information is written on the screen, thus reducing the rewrite time after execution of each command. When program execution begins, the user is presented with the unit circle, and a listing of commands on the top left side of the screen. The commands are abbreviated in the following manner. The general command type or mode is specified across the top of the array as INTERACTIVE, RECT, and POLAR (see figure 4-1). Each of these modes conforms to the above description. Down the left side of the array are the commands of the form CRR, where C is the change to be made, A - for add a root, D - for delete a root. RR is for the type of root to be acted upon by the command: RZ - real zero, CZ - complex zero, RP - real pole, and CP - complex pole. As an example, the box in the center column aligned with the row titled DCZ stands for the command "Delete a Complex Zero - Rectangular Coordinates. There are two unique commands listed as NUC, and LST. The New Unit Circle (NUC) command simply redraws the unit circle and command

UNIT CIRCLE COMMANDS

CMD S INTER-ACTIVE KEYBOARD RECT POLAR

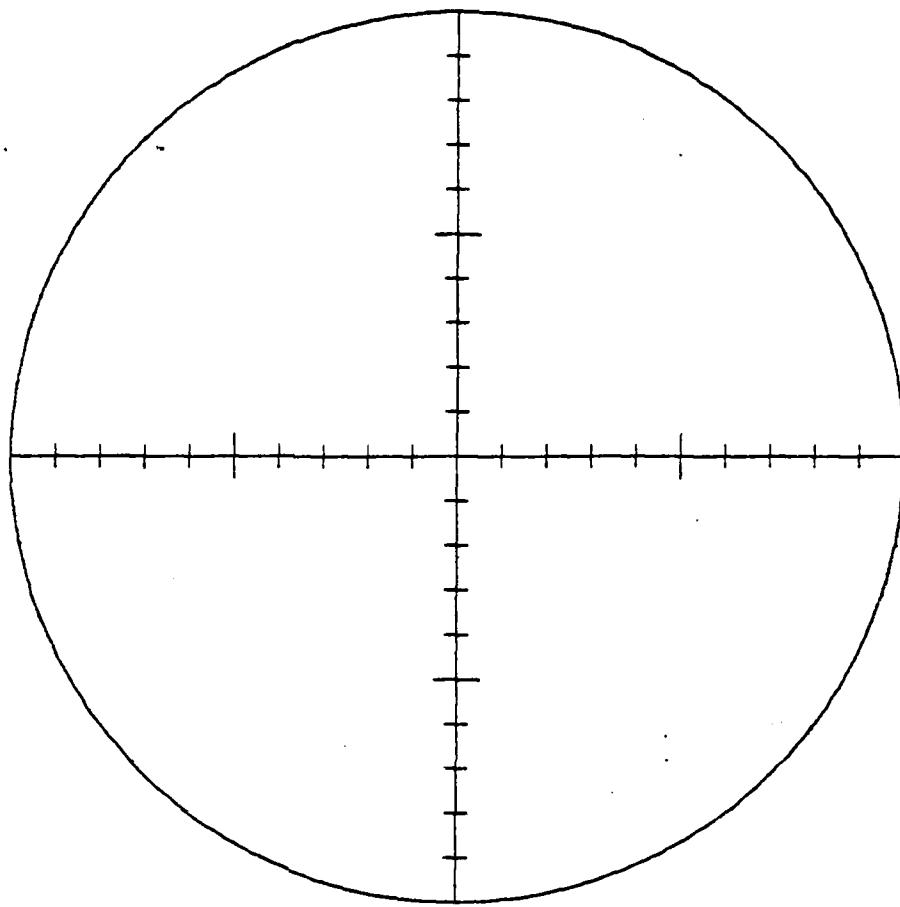


Figure 4-1 Basic Display Format

array. This is appropriate when either too many entries have been made to the terminal, and the command array is no longer clear, or when noise in the line from the computer causes a deformed array or unit circle to be drawn. The LST command provides the user with a listing of the current status of the filter being analyzed, in a self explanatory format.

In all cases when the unit circle and command array just described appear on the screen, an audible tone or bell is heard. This bell indicates to the user that the cursor is to be positioned within one of the boxes in the command array. In order to execute a command, the cursor is positioned in the box associated with the desired command. A single keyboard character (any character but the "return" key is acceptable) is then typed. The cursor then disappears. The system presents a carat pointing to the command that the computer is about to execute; the flashing cursor blinks within the box associated with the command which is about to be executed. If the box so indicated is the command that was selected, the user types a "space", an "e" (for execute) and then "carriage return". In cases where a rectangular or polar mode command is to be executed, the screen is then erased, and new information is printed. In cases where an interactive graphics command is to be executed, only the cursor reappears. This second appearance of the cursor is not accompanied by a bell or audible tone.

This indicates that the cursor is to be positioned within the unit circle. Once so positioned, a single keyboard character is typed (not "return"), and, as appropriate, the unit circle is redrawn to reflect the change in pole or zero locations. After this update of the z-plane, the circle and command array are redrawn with the cursor accompanied by the audible tone.

There are only two exceptions to this scenario. First, if the flashing cursor does not flash in the correct box, the wrong command will be executed. If an incorrect box contains the flashing cursor, the user should not type the "space", "e", sequence. Instead, he should type two other characters (e.g., "space", "space") and then "return." The cursor returns along with the audible tone, calling for a readjustment of the cursor, closer to the desired command box. The second exception occurs when the placement of all of the poles and zeros is completed. In this case, after aligning the cursor with any box, the sequence "space", "x" (for exit), "return" should be typed. This will terminate the input, or modification, stage of the program and present the user with a series of options for the next stage of filter processing. At this point a display appears which explains the options available to the user.

### C. SUMMARY OF POLZRO SUBCOMMANDS

When the cursor appears along with an audible tone, the user is to position the cursor within the command array, and type a keyboard character (not "return"). When the flashing cursor appears within a box, he types ("space", "e", "return") to execute the specified command. "Space" and any other character but "x" will return the user to the command table for cursor readjustment. To terminate the input, or modification mode, the cursor is positioned over any box, and once the flashing cursor enters the box, the characters "space", "x", "return" are typed.

## V. LOADING THE ASDF PACKAGE

The procedure for using the ASDF program consists of either six or seven steps depending on whether or not the ASDF package is resident on OSX001. Usually the program sections of ASDF are stored on the T2314 disk pack OSX001. Each Monday morning the OSX001 disks are scratched so that the ASDF program must be moved from the permanent storage location on DISK02, to the temporary storage location on OSX001. The user may simply sign onto a 4012 terminal, and execute three commands to load ASDF into his virtual machine. Once this loading process has been successfully completed, the commands previously discussed are at the user's disposal for filter analysis.

### A. LOGIN PROCEDURE

With one minor exception, the standard login procedures (specified in Section 4.4.3 of the CP/CMS User's Manual) [Ref. 4] are applicable when entering the CP/CMS system to use ASDF. Due to the size of the ASDF programs the user must request a 400k virtual machine when logging onto CP/CMS. The virtual machine is requested as follows:

login XXXXTNN 400k

where XXXX is the user's computer center number, T is the type of user i.e. G for general user, and P for private

user, and NN is the two digit terminal number. The 400k request in the LOGIN is absolutely mandatory. Without this request the user will be able to load the ASDF program, however, when attempting to execute the RESPONSE command, an error: "INPUT COMMAND ERROR" will result. Should this error occur when the command is correctly spelled the user has no alternative but to logoff and log back on to the system requesting the correct size virtual machine. The remainder of the login procedure is identical to the examples in the CP/CMS user's manual.

#### B. TESTING OSX001 FOR ASDF PROGRAMS

The second step in loading the ASDF programs is to determine whether or not a copy of the programs exists on OSX001. The ASDF programs are permanently stored on the operating system DISK02. The first time that the programs are used each week, the user must move them from DISK02 to the disk OSX001. To determine whether or not OSX001 has the ASDF package, issue the command:

```
TOCP ASDF191 EXEC P1
```

The system will respond:

```
EXECUTION BEGINS...
```

```
237 = OSX001
```

```
ENTER DSNAME OR '/*'
```

The correct user response is:

```
F0718.asdf191
```

At this time one of two responses will appear. The particular response received is dependent on whether or not ASDF resides on OSX001.

1. ASDF is on OSX001

When the ASDF programs are located on OSX001, the system response is:

EXTENTS EXHAUSTED, EOF SIMULATED.

4 BLOCKS 63 RECORDS READ

This message indicates that file ASDF191 has satisfactorily been transferred to the user's virtual machine and the user is ready to continue with the subsequent loading steps.

2. ASDF is not on OSX001

When the ASDF programs are not on OSX001, the system response will be:

DATA SET NOT FOUND (OS/360 S213)

ENTER DSNAME OR '/\*'

This response indicates that the user must move the ASDF programs to OSX001 before the loading procedure may be resumed. The simplest method for accomplishing this transfer is to generate a file on CP/CMS which exactly duplicates the Job Control Language program which follows.

To generate the file which transfers ASDF, logon to CP/CMS. Once the system's responses have been entered and the system is ready, issue the command:

EDIT ASDF JCL

Then type in, or read in<sup>1</sup>, the program which follows.

```
// Standard JOB Card (User's Manual Sec. 3.3.2.1)
// EXEC PGM=IEBGENER
//SYSPRINT DD SYSOUT=A
//SYSIN DD DUMMY
//SYSUT1 DD DSN=F0718.ASDF,VOL=SER=DISK02,UNIT=3330,
//      DCB=(RECFM=FB,LRECL=80,BLKSIZE=3200),DISP=(OLD,KEEP)
//SYSUT2 DD DSN=F0718.ASDF,VOL=SER=OSX001,UNIT=2314,
//      DCB=(RECFM=FB,LRECL=80,BLKSIZE=3200),DISP=(NEW,KEEP),
//      SPACE=(TRK,(40,1),RLSE)
// EXEC PGM=IEBGENER
//SYSPRINT DD SYSOUT=A
//SYSIN DD DUMMY
//SYSUT1 DD DSN=F0718.ASDF191,VOL=SER=DISK02,UNIT=3330,
//      DCB=(RECFM=FB,LRECL=80,BLKSIZE=800),DISP=(OLD,KEEP)
//SYSUT2 DD DSN=F0718.ASDF191,VOL=SER=OSX001,UNIT=2314,
//      DCB=(RECFM=FB,LRECL=80,BLKSIZE=800),DISP=(NEW,KEEP),
//      SPACE=(800,(3,1),RLSE)
//
```

Once this program has been correctly read in to the user's disk, it must be submitted to the operating system using the standard SUBMIT command:

SUBMIT ASDF JCL P1 XXXX

XXXX is the user's computer center number. If the SUBMIT function is working the following messages will be returned:

\*\* CARDS XFERED TO 0098P \*\*

FNAME FTYPE P1 SENT FOR OS BATCH JOB

After a short delay the system will send a second message:

FROM 0098P33 : JOB SENT TO OS WITH 21 CARDS WRITTEN (Time)

The user should then revert back to section B above which

---

<sup>1</sup>A deck containing this program is available from Professor Kirk, Sp 302.

discusses the TOCP command. After giving the system a period of time to execute the JCL job which was just submitted, execution of the TOCP command will indicate that the ASDF files are present. If the operating system has not completed executing the transfer, the TOCP request will respond as in paragraph two above.

#### B. LOADING ASDF

Once ASDF resides on disk OSX001, the remaining required steps are simple. The user issues the command:

EXEC ASDF191

The system will type a series of lines onto the terminal. At the conclusion of these typewritten lines the user is prompted to issue the next two commands:

LOGIN 192 P

The system responds:

192 REPLACES P (191)

The next required entry is:

EXEC ASDF192

These two commands will cause a very long list of CP/CMS commands to be typed on the screen. Each of these CP/CMS commands is automatically executed by the operating system in the process of loading the ASDF programs. There are no further commands required from the user to complete the loading process.

When the entire ASDF program package is loaded, the user will be presented with a title page and the instruction: "HIT SPACE AND RETURN TO CONTINUE." Once the user has typed "space" and "return" the display will write out a listing of the commands at his disposal. These commands have already been discussed in chapter four.

## VI. USING ASDF

Each of the following sections constitutes an example for one of the three input modes. Each example uses only one input mode. In general, these modes may be combined during the generation of any particular filter. The mode selected should be the one most convenient to the user.

### A. EXAMPLE ONE - INTERACTIVE GRAPHICS

This first example uses the ASDF program in the interactive graphics mode. The objective is to observe the responses of a digital filter which has two real zeros, one at the origin and another at +0.8, two complex poles located at  $(0.8 \pm j0.2)$ , and the filter gain is 1.000. The interactive graphics mode is used since the exact locations of the poles and zeros are not critical. For the purposes of this example, it is assumed that the user has already followed the login procedure described in the above paragraphs, and has loaded the ASDF program. The user has already seen the title page, and the two pages of command descriptions. The screen is clear except for the top left corner which shows:

\*ASDF-RE

This group of letters is the signature for the ASDF program

and indicates that the program is ready to execute the user's next command.

Since we must first enter the poles and zeros into the z-plane the appropriate command to type is:

POLZRO

The ASDF program will then draw the screen as shown in figure 6-1, and generate an audible tone. Initially the cursor will be located at some arbitrary position or perhaps may not appear on the screen at all. Movement of the thumb wheels moves the cursor position. Since we wish to execute in the interactive graphics mode, to add a real zero, we move the cursor (intersection of the two lines tracing across the screen) into the box in the left column labeled ARZ, (Add a Real Zero) figure 6-2. We then type any keyboard character except "return".<sup>1</sup> The trace cursor will disappear, and the flashing alphanumeric cursor will appear. The program will print a carat pointing to the box selected by the user. The flashing cursor will move into the box selected.

The user then types the command "space", "e", "return". The flashing cursor disappears, and the trace cursor reappears. The absence of an audible tone at this time indicates that the trace cursor is to be positioned within the unit circle.

---

<sup>1</sup>The 4012 terminal in the computer center requires a "control-s" after every response.

| UNIT CIRCLE COMMANDS |             |          |       |
|----------------------|-------------|----------|-------|
| CMD'S                | INTERACTIVE | KEYBOARD | POLAR |
| ACZ                  | □           | □        | □     |
| ACP                  | □           | □        | □     |
| ARZ                  | □           | □        | □     |
| ARP                  | □           | □        | □     |
| DCZ                  | □           | □        | □     |
| DCP                  | □           | □        | □     |
| DRZ                  | □           | □        | □     |
| DRP                  | □           | □        | □     |
| NUC                  | □           | □        | □     |
| LST                  | □           | □        | □     |

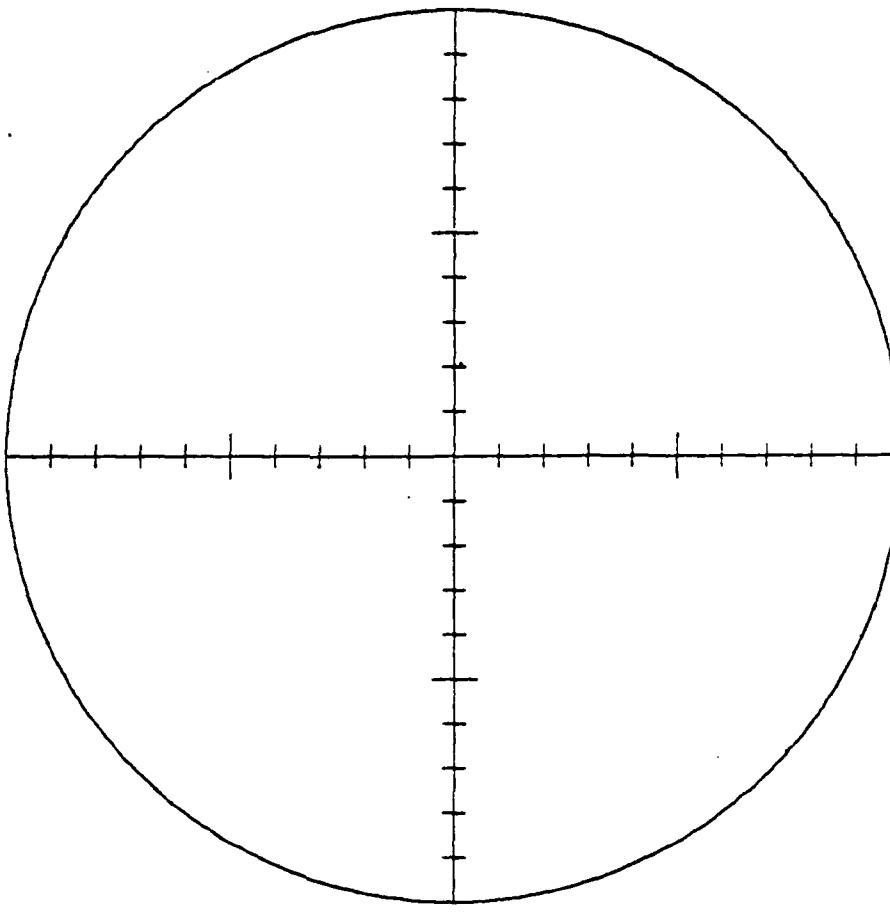


Figure 6-1 Initial Screen Representation After Issuing The Command POLZR

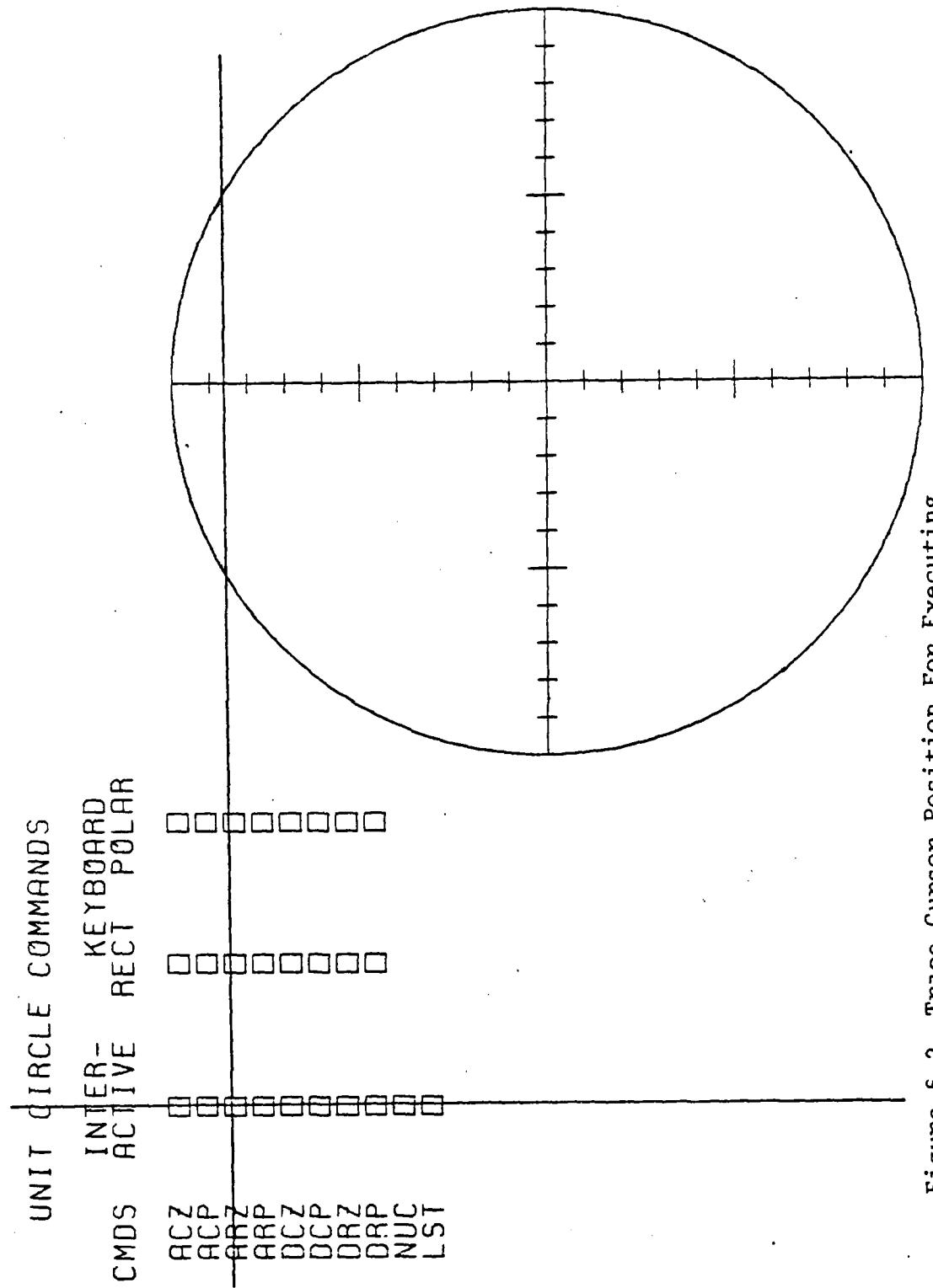


Figure 6-2 Trace Cursor Position For Executing The Command "Add A Real Zero"-Interactive Graphics Mode

The trace cursor is adjusted to the position of the desired real zero, (the origin in this case), as shown in figure 6-3. Any keyboard character except "return" is then typed. The ASDF program plots the zero at the origin, and returns the trace cursor with the audible tone. The audible tone reminds the user that the trace cursor is to be positioned in the command array. Since another real zero is to be entered, the cursor is positioned as in figure 6-1b again, and the same steps are followed. When the trace cursor reappears without the audible tone, position it within the unit circle as near as possible to the point  $(0.8 +/- j0.0)$  as shown in figure 6-4. (To enter the zero precisely at 0.8 the rectangular or polar mode would be used.) The steps for entering the complex pole pair exactly parallel those for the previous entries, and are depicted in figures 6-5, and 6-6.

Once all the poles and zeros have been entered, the trace cursor may be aligned with any command box, and a character typed (not "return"). Once the alphanumeric cursor enters that box, the user types "space", "x", "return". The screen is cleared and the user is asked if he wishes to change the default filter gain. Since the default value is 1.0, the user responds "n", the ASDF program clears and responds with: \*ASDF-RE

The next step in the normal sequence is for the user to look at the filter characteristics. To display these

| UNIT CIRCLE COMMANDS |                          |                          |
|----------------------|--------------------------|--------------------------|
| CMD\$                | INTER-ACTIVE             | KEYBOARD RECT POLAR      |
| ACZ                  | <input type="checkbox"/> | <input type="checkbox"/> |
| ACP                  | <input type="checkbox"/> | <input type="checkbox"/> |
| ARZ                  | <input type="checkbox"/> | <input type="checkbox"/> |
| ARP                  | <input type="checkbox"/> | <input type="checkbox"/> |
| DCZ                  | <input type="checkbox"/> | <input type="checkbox"/> |
| DCP                  | <input type="checkbox"/> | <input type="checkbox"/> |
| DRZ                  | <input type="checkbox"/> | <input type="checkbox"/> |
| DRP                  | <input type="checkbox"/> | <input type="checkbox"/> |
| NUC                  | <input type="checkbox"/> | <input type="checkbox"/> |
| LST                  | <input type="checkbox"/> | <input type="checkbox"/> |

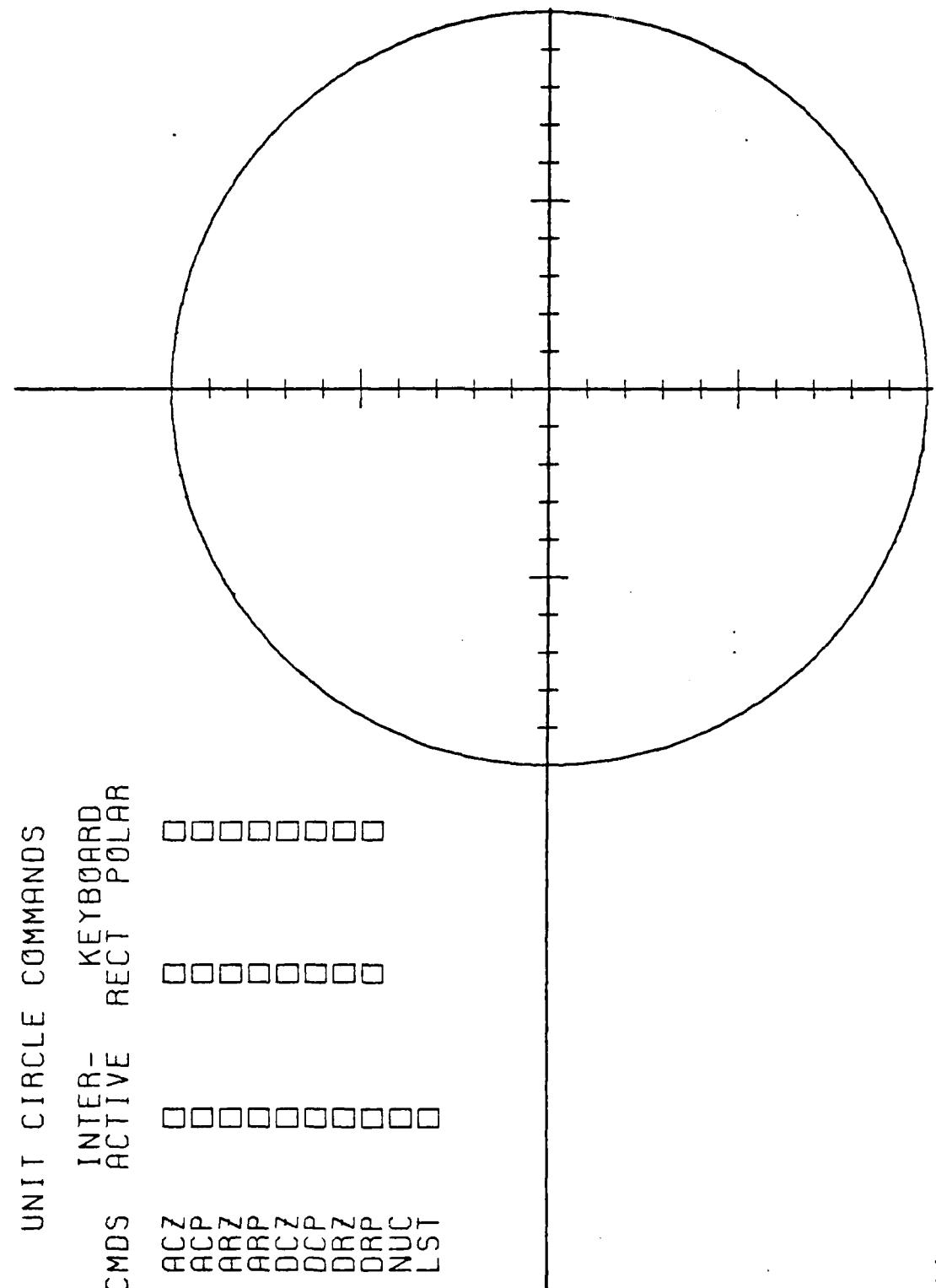


Figure 6-3 Trace Cursor Position Required To Place A Real Zero At The Origin

### UNIT CIRCLE COMMANDS

| CMD\$ | INTER-ACTIVE             | KEYBOARD<br>RECT         | POLAR                    |
|-------|--------------------------|--------------------------|--------------------------|
| ACZ   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| ACP   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| ARZ   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| ARP   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| DCZ   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| DCP   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| DRZ   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| DRP   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| NUC   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| LST   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |

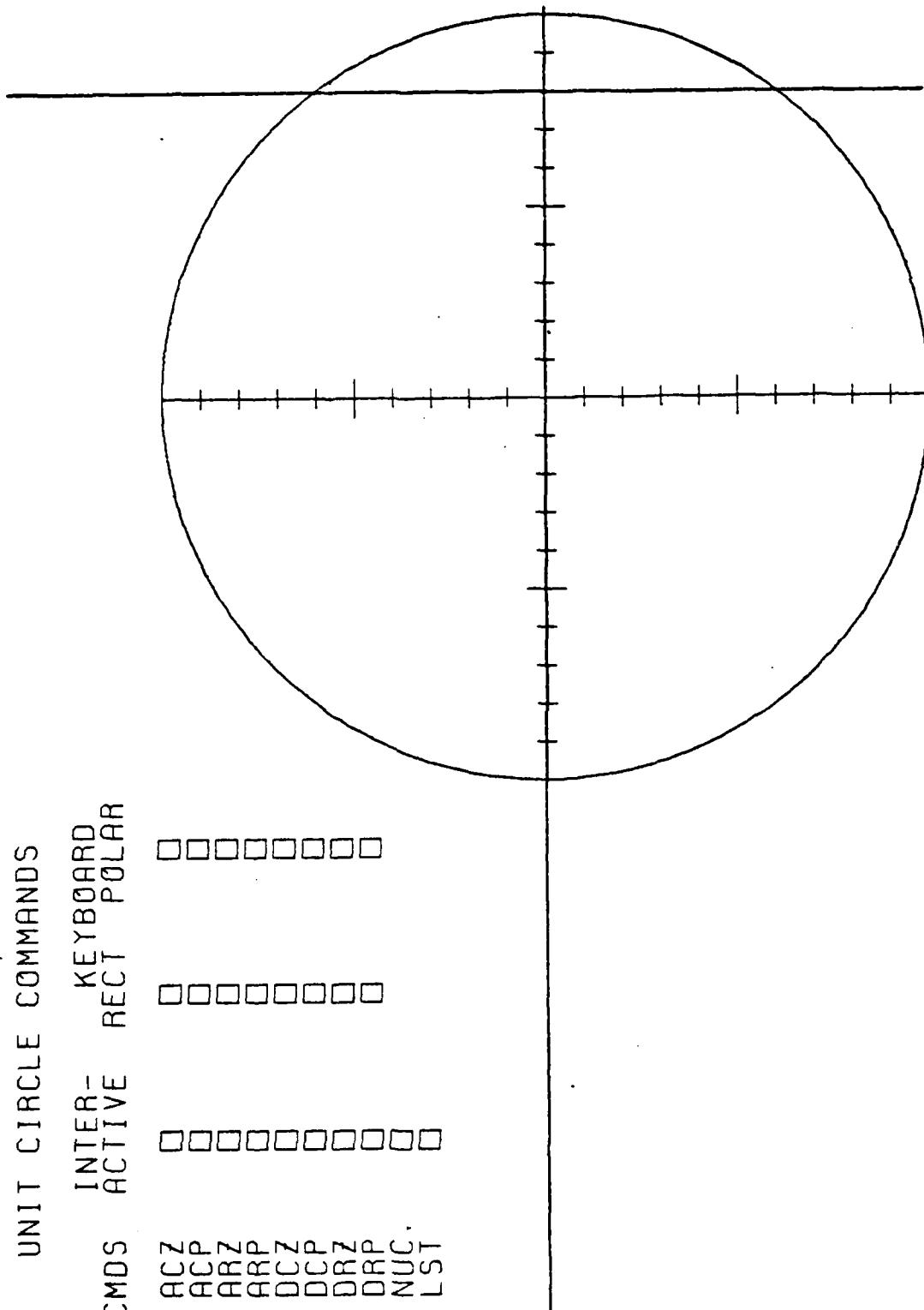
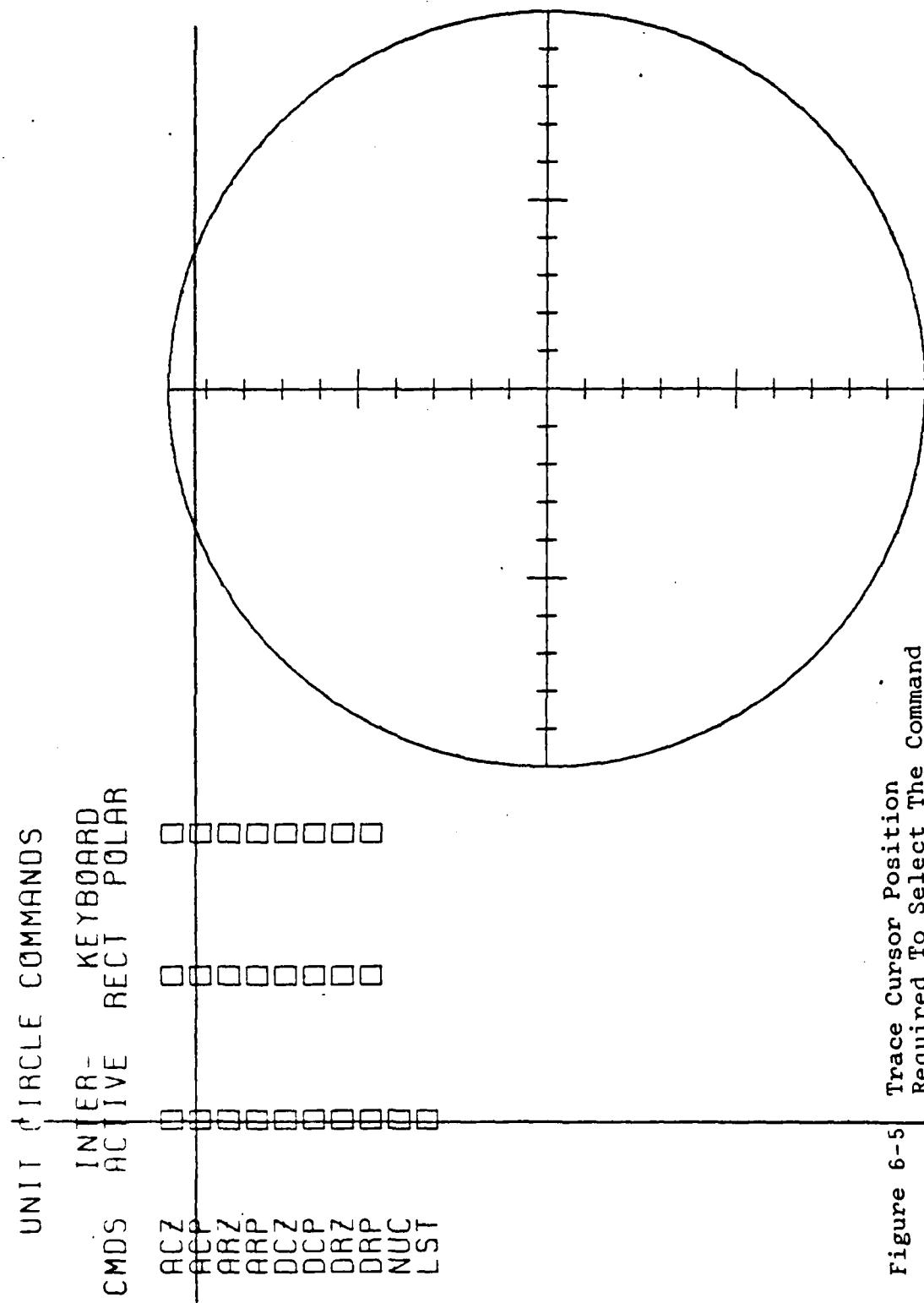


Figure 6-4 Trace Cursor Position Required To Put A Real Zero At (+0.8)



Trace Cursor Position  
Required To Select The Command  
"Add A Complex Pole"-Interactive  
Graphics Mode

Figure 6-5

### UNIT CIRCLE COMMANDS

| CMD\$ | INTERACTIVE              | KEYBOARD<br>Polar        |
|-------|--------------------------|--------------------------|
|       | RECT                     |                          |
| ACZ   | <input type="checkbox"/> | <input type="checkbox"/> |
| ACP   | <input type="checkbox"/> | <input type="checkbox"/> |
| ARZ   | <input type="checkbox"/> | <input type="checkbox"/> |
| ARP   | <input type="checkbox"/> | <input type="checkbox"/> |
| DCZ   | <input type="checkbox"/> | <input type="checkbox"/> |
| DCP   | <input type="checkbox"/> | <input type="checkbox"/> |
| DRZ   | <input type="checkbox"/> | <input type="checkbox"/> |
| DRP   | <input type="checkbox"/> | <input type="checkbox"/> |
| NUC   |                          | <input type="checkbox"/> |
| LST   |                          | <input type="checkbox"/> |

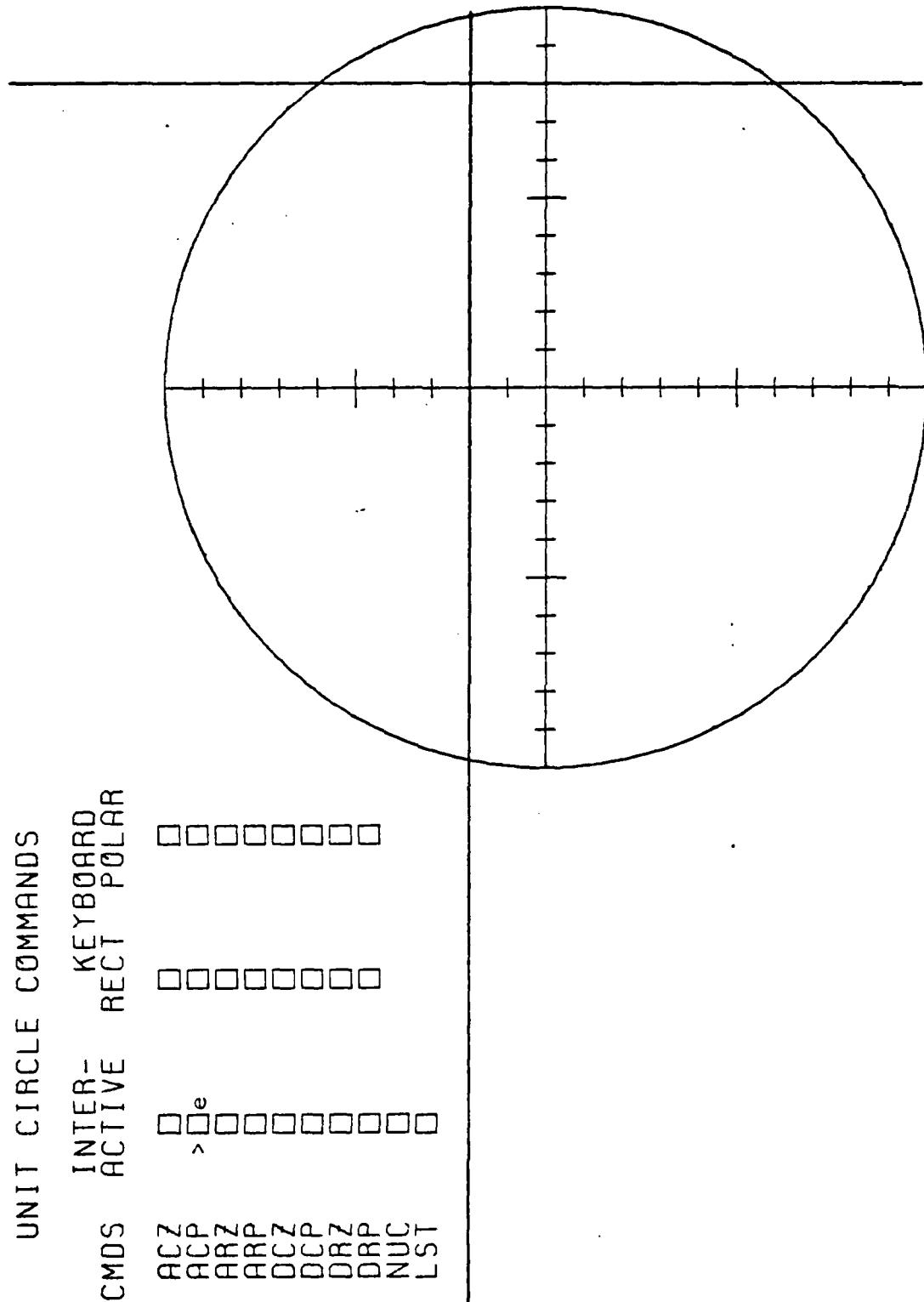


Figure 6-6 Trace Cursor Position Required To Enter A Complex Pole At  $(0.8+/-j0.2)$

characteristics the command typed is:

RESPONSE

To get a hard copy of the filter responses the command:

EXEC HRD\$CPY

is typed. Figures 6-7a, b, c, d, e, f, and g show the pertinent portions of the output.

### 3. EXAMPLE TWO - RECTANGULAR MODE

This second filter example is taken from [Ref. 5], page 222. The filter is a fourth-order low pass Chebyshev. The derivation of the transfer function is described in the text. The given transfer function is factored to give the desired pole/zero locations. The filter has two complex zeros at  $(-1.0 \pm j0.0)$  and two complex pole pairs, one pair at  $(.7498 \pm j.5348)$ , and one pair at  $(.7774 \pm j.2120)$ . The filter gain is given as 0.001836.

In a manner exactly paralleling the previous example, the user selects the command ACZRCT (which stands for Add a Complex Zero - Rectangular Coordinates), by positioning the trace cursor in the appropriate box, as in figure 6-8a. Once a keyboard character is typed, and the alphanumeric cursor moves into the box, the "space", "e", and "return" keys are typed. The ASDF program will erase the screen and draw the display shown in figure 6-8b. The user then types in the rectangular coordinates of either complex zero in the first complex zero pair, figure 6-8c. The system will



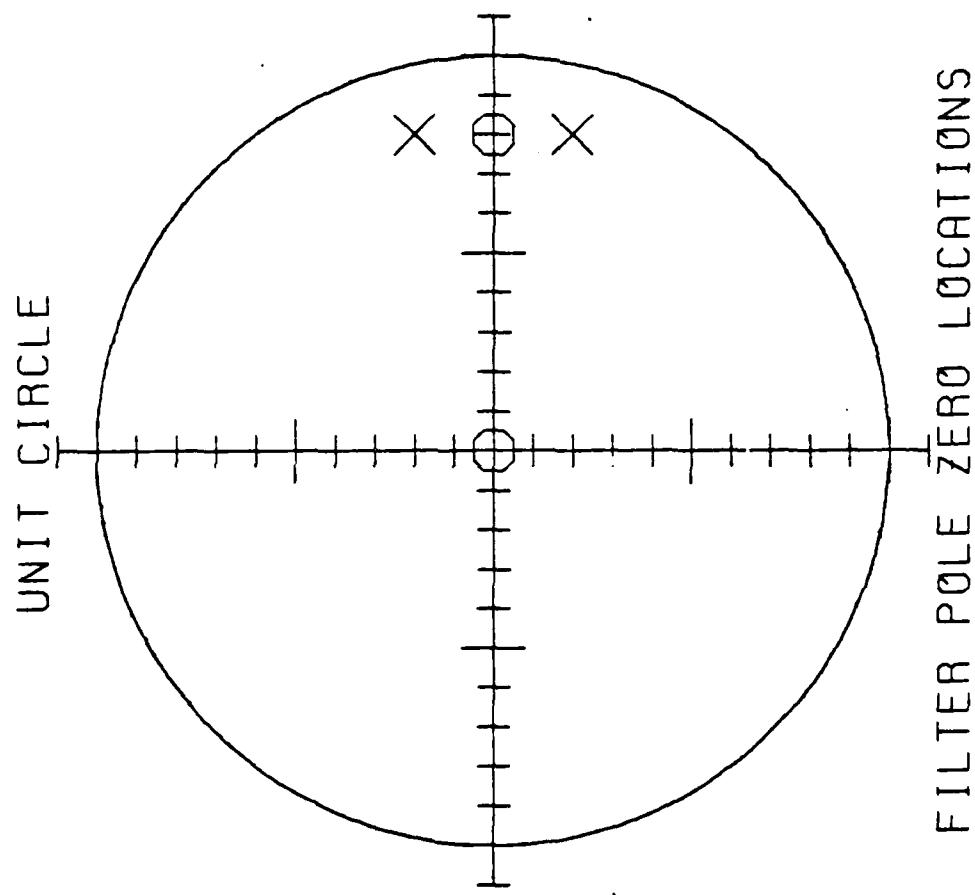


Figure 6-7b Pole Zero Locations For Example Two

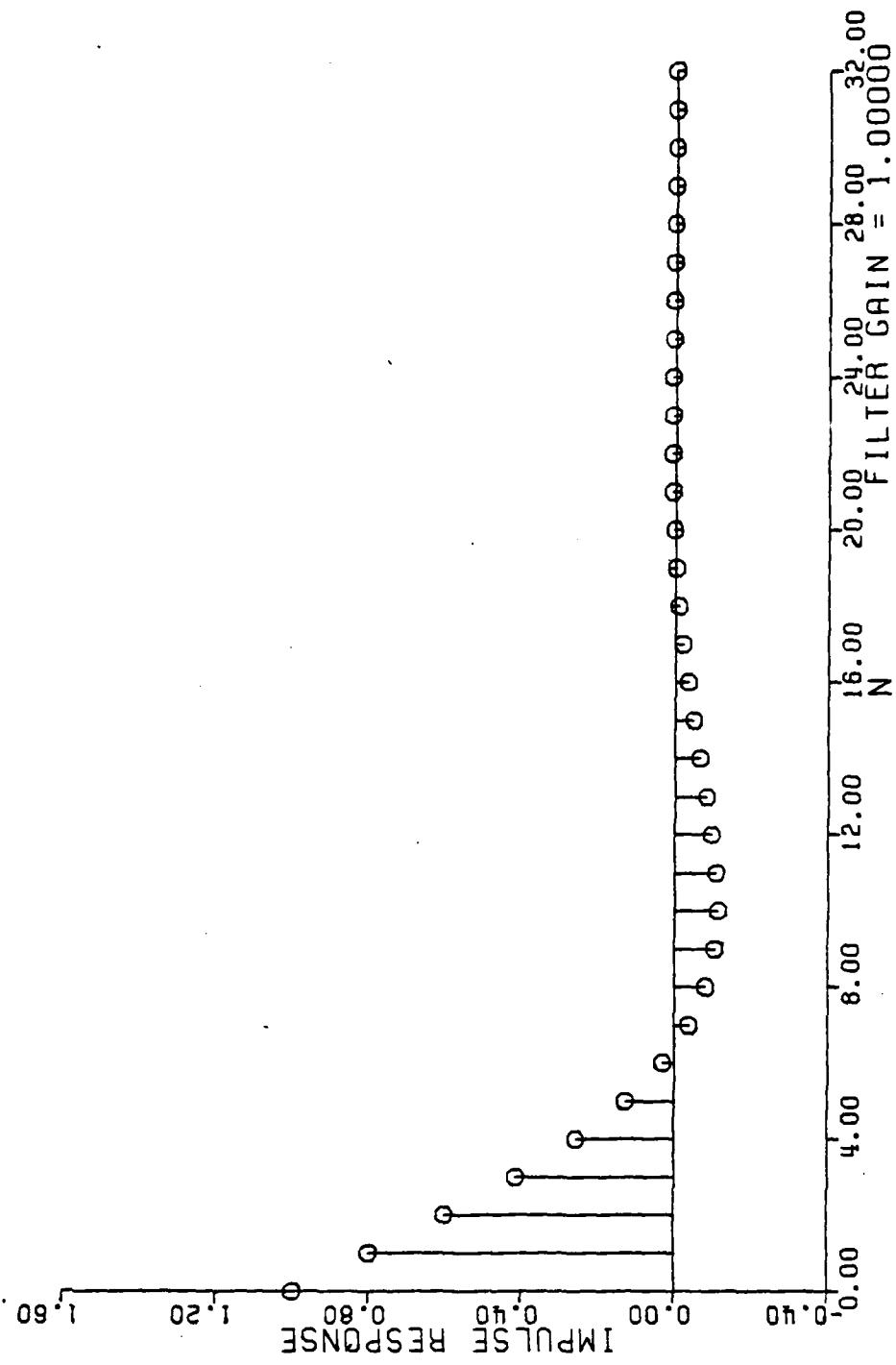


Figure 6-7c Unit Sample Response For Example Two

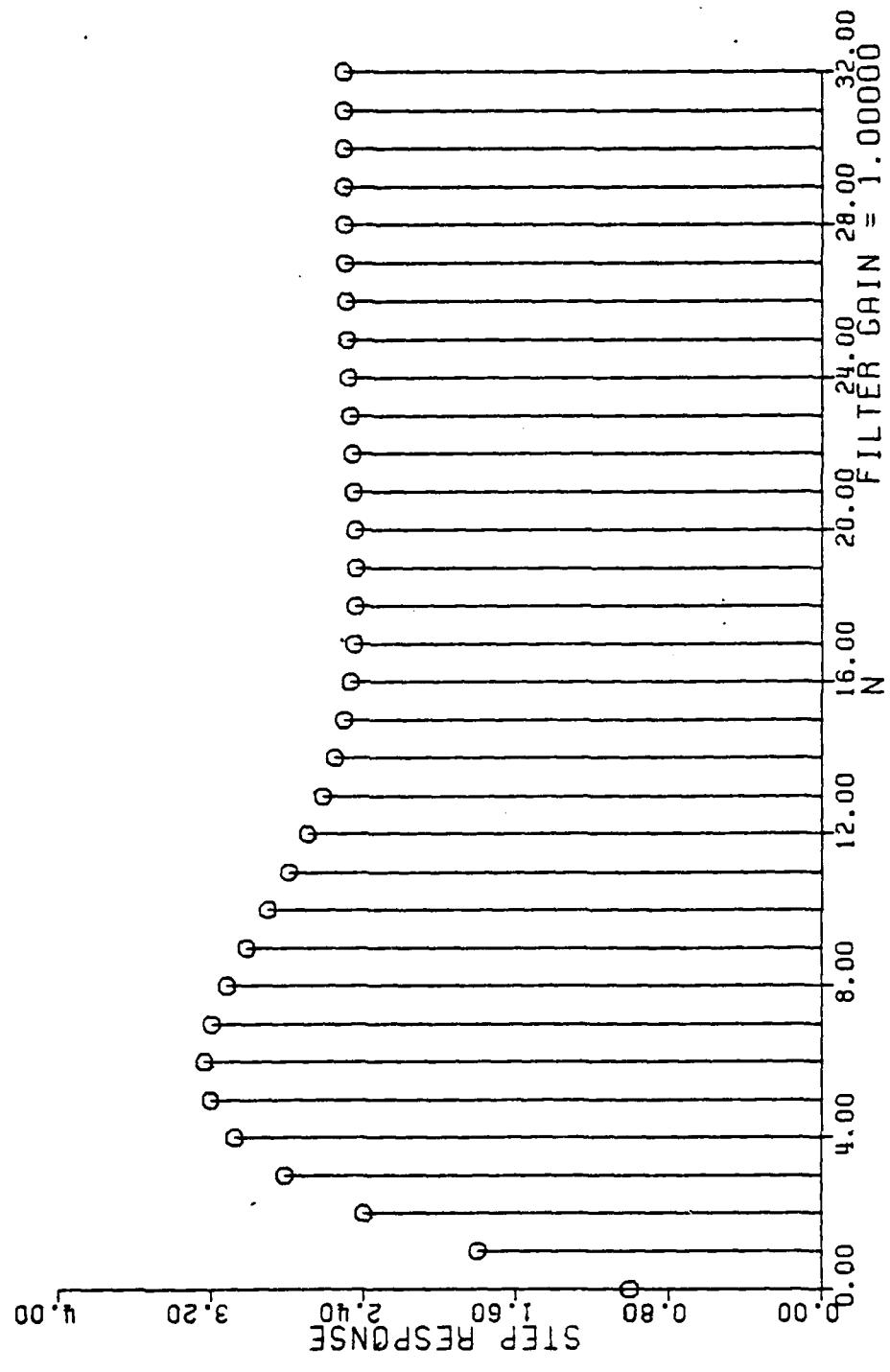


Figure 6-7d Step Response For Example Two

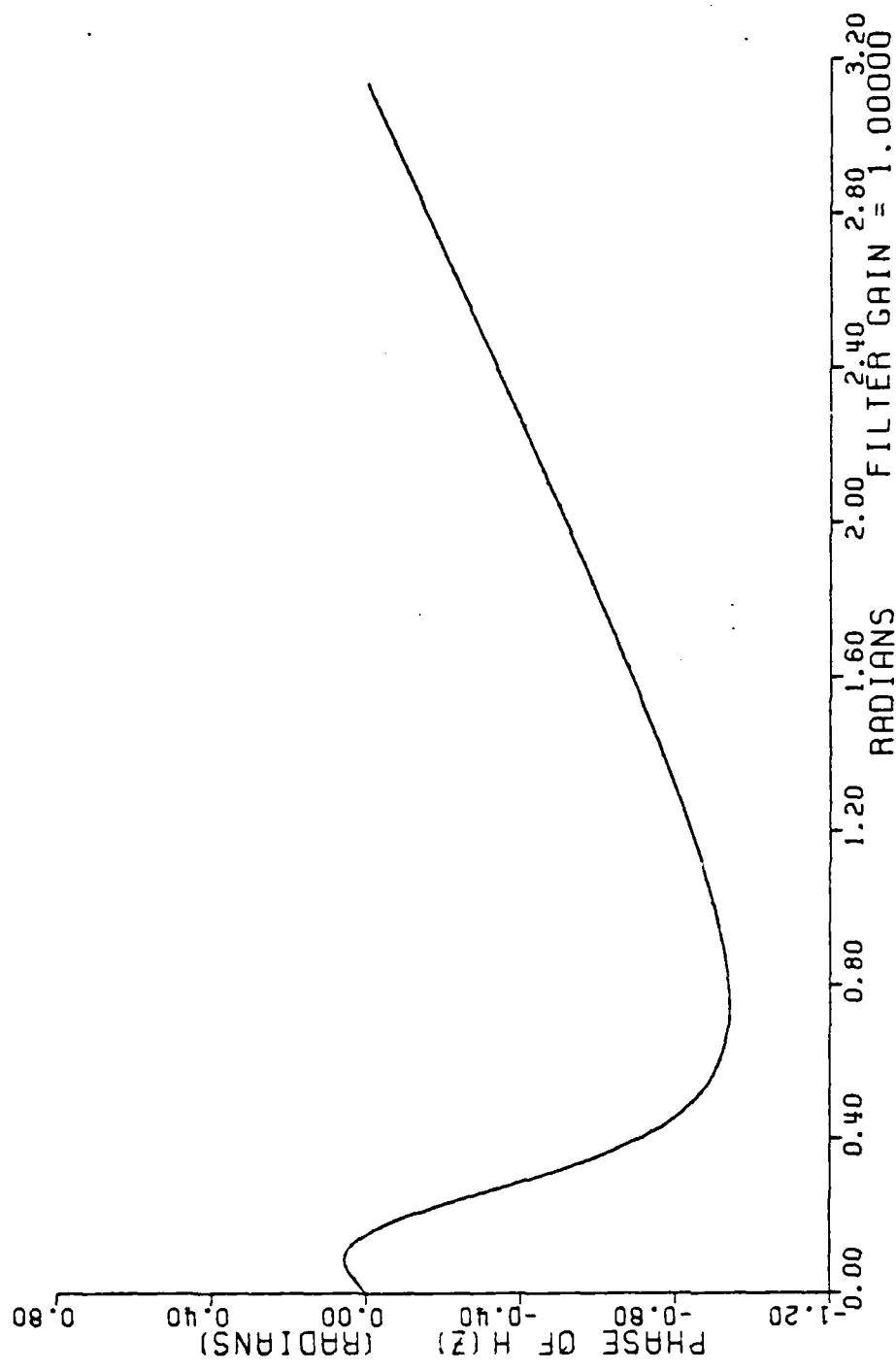


Figure 6-7e Phase Response For Example Two

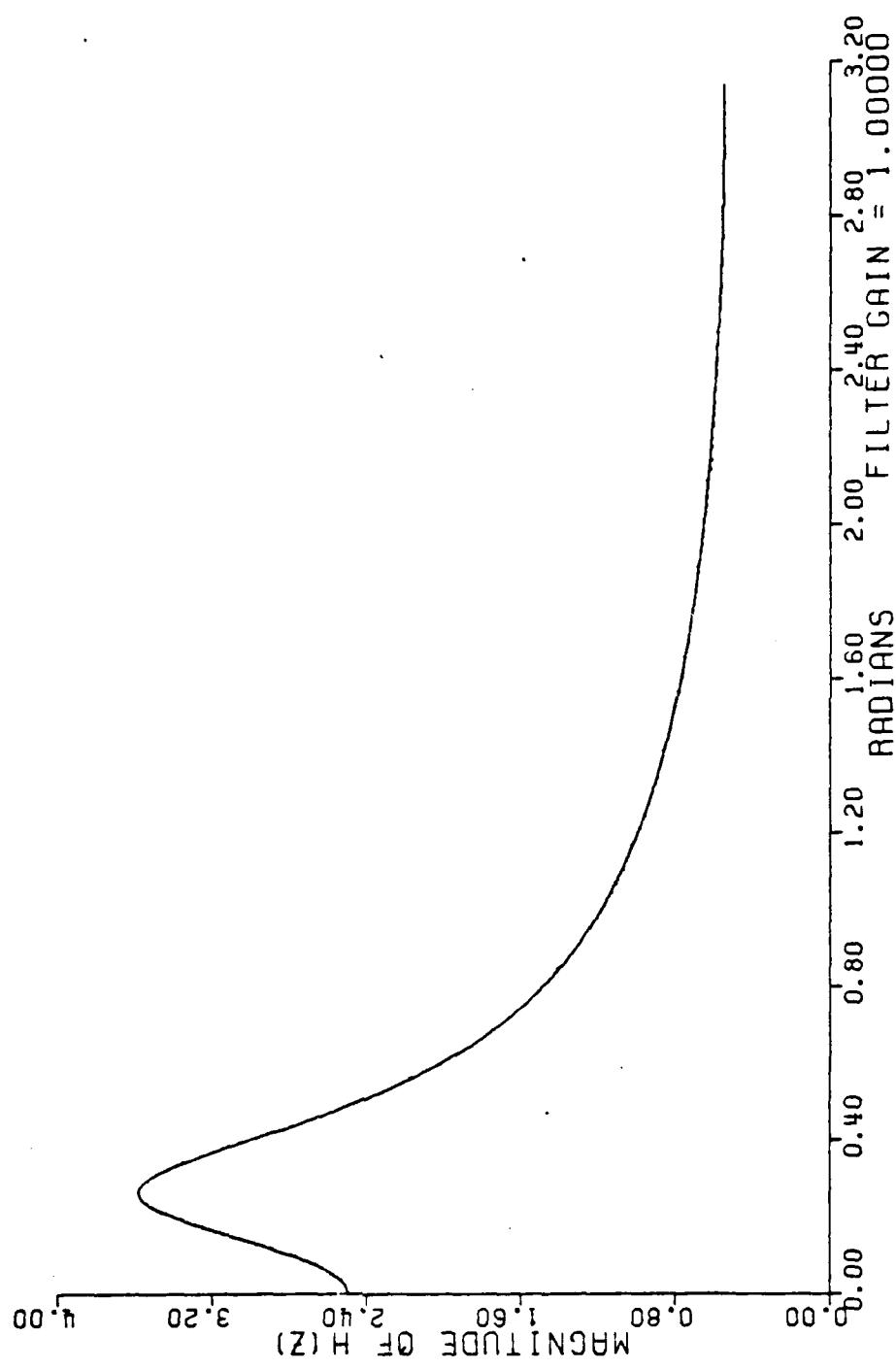


Figure 6-7f Magnitude Of  $H(z)$  For Example Two

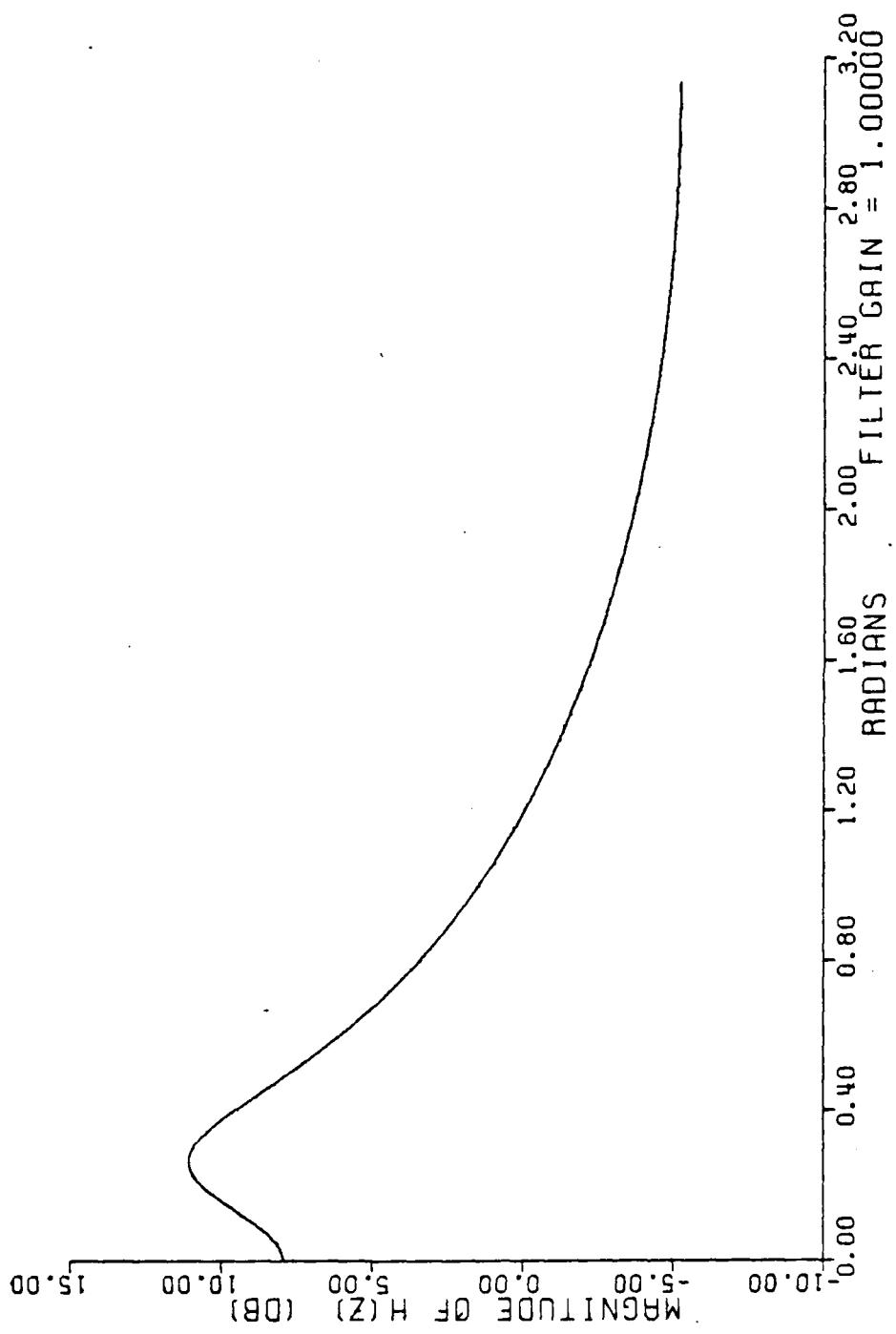


Figure 6-7g Magnitude Of The Transfer Function In Decibels For Example Two

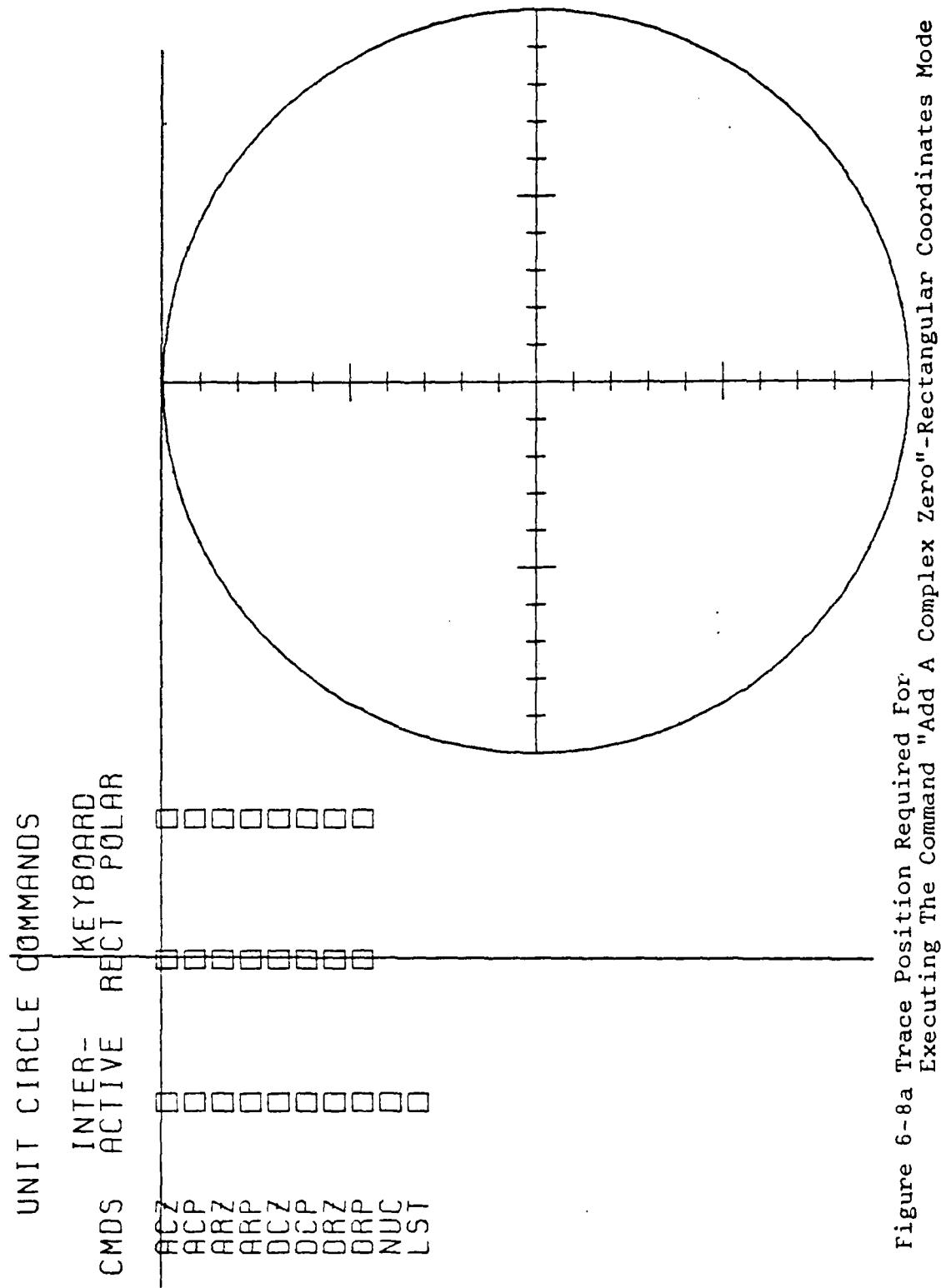


Figure 6-8a Trace Position Required For Executing The Command "Add A Complex Zero"-Rectangular Coordinates Mode

TO ADD A COMPLEX ZERO TO THE DISPLAY, ENTER THE REAL AND IMAGINARY PARTS WITHIN THE BOXES PROVIDED. EACH NUMBER REQUIRES A DECIMAL. REAL PART MINUS SIGNS MUST BE INCLUDED WITHIN THE BOX. NOTE: ALL COMPLEX ZEROS MUST BE WITHIN TEN UNITS OF THE ORIGIN.

REAL  +/- J  IMAGINARY

Figure 6-8b Screen Display For The Command ACZRCT

TO ADD A COMPLEX ZERO TO THE DISPLAY, ENTER THE REAL AND IMAGINARY PARTS WITHIN THE BOXES PROVIDED. EACH NUMBER REQUIRES A DECIMAL. REAL PART MINUS SIGNS MUST BE INCLUDED WITHIN THE BOX. NOTE: ALL COMPLEX ZEROS MUST BE WITHIN TEN UNITS OF THE ORIGIN.

REAL                   IMAGINARY  
>> +/- J

THE NEW COMPLEX ZERO WILL BE -1.000000 +/- J 0.0  
IF CORRECT TYPE 'Y', IF NOT 'N'

Figure 6-8c Screen Display After Entering The First Complex Zero

ask whether or not the root location has been correctly entered. The user responds 'y' for yes, 'n' for no. If the root has been incorrectly entered, an 'n' response will rewrite the screen for another attempt. Upon receiving a 'y' response ASDF rewrites the unit circle and command array, and plots the new root. The second complex zero is entered exactly as the first.

The complex poles are entered as were the zeros. The trace cursor is first placed in the box ACPRCT. (Add a Complex Pole - Rectangular Coordinates), as in figure 6-9. Figure 6-10 shows the unit circle after all poles and zeros have been entered. The POLZRO command is terminated by aligning the trace cursor with any box, typing a character, waiting for the flashing alphanumeric cursor to enter the box, and typing "space", "x". The system responds by asking about the filter gain. In this example the filter gain is to be changed to .001836, so the correct response is 'y'. The new filter gain, 0.001836, is typed to terminate the POLZRO command.

To view the filter responses, the user enters the command:

RESPONSE

when the \*ASDF-RE signature appears. The hard copy responses of the filter are shown in figures 6-11a through 6-11g.

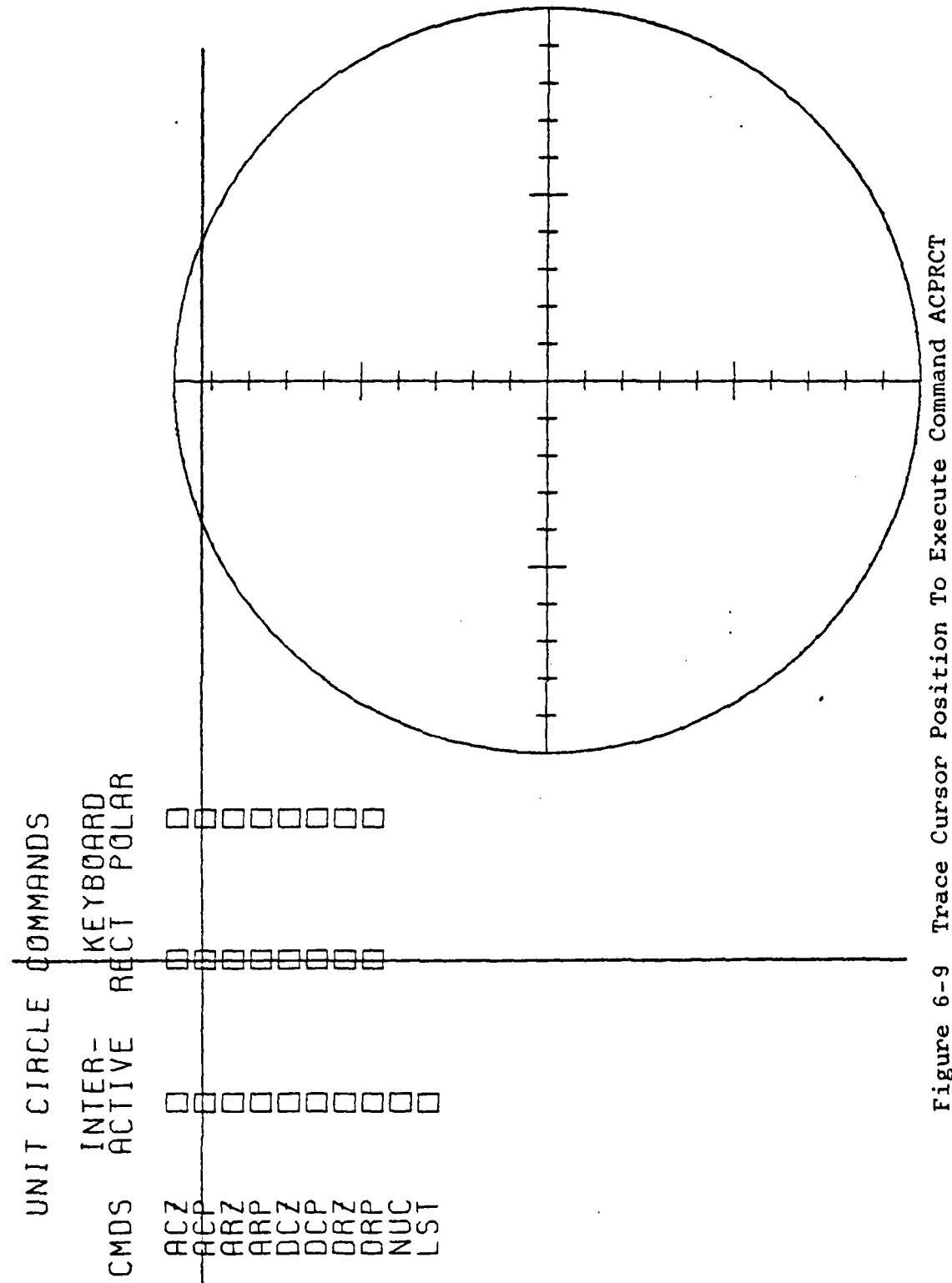


Figure 6-9 Trace Cursor Position To Execute Command ACPRCT

### UNIT CIRCLE COMMANDS

| CMD'S | INTER-ACTIVE             | KEYBOARD                 | RECT                     | POLAR                    |
|-------|--------------------------|--------------------------|--------------------------|--------------------------|
| ACZ   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| ACP   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| ARZ   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| ARP   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| DCZ   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| DCP   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| DRZ   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| DRP   | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> | <input type="checkbox"/> |
| NUC   |                          |                          |                          |                          |
| LST   |                          |                          |                          |                          |

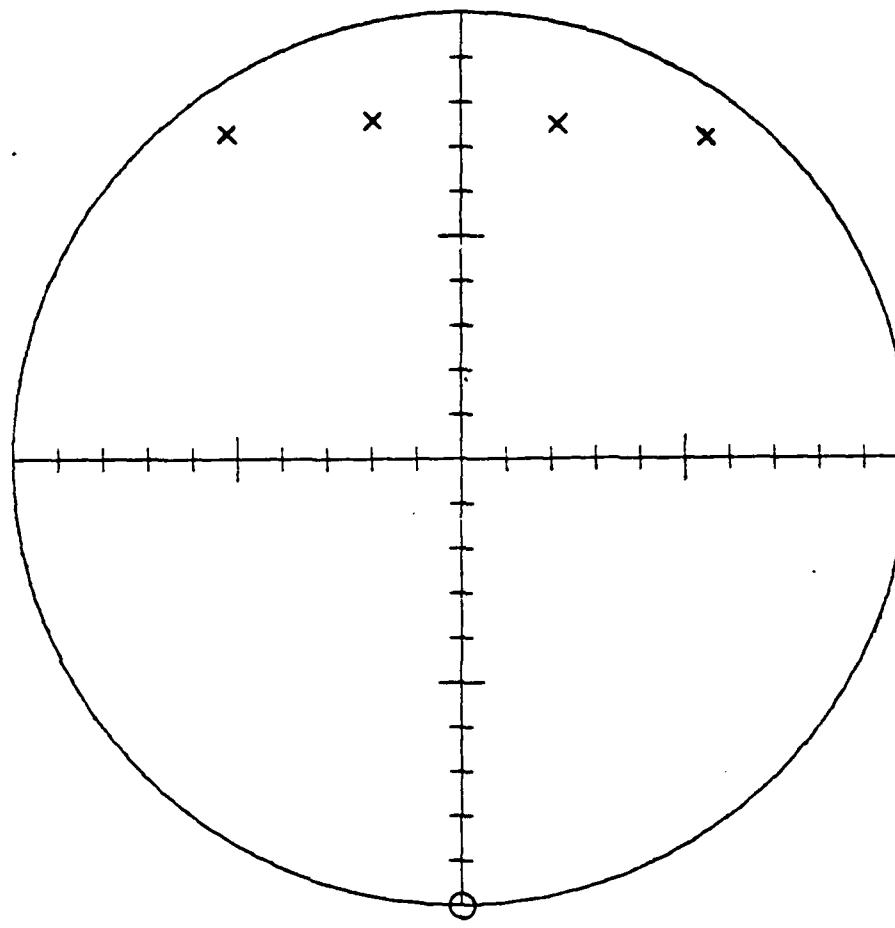


Figure 6-10 Unit Circle After All Poles and Zeros Have Been Returned-Example Two

```

NUMBER OF REAL ZEROES: 0
NUMBER OF COMPLEX ZEROES: 2
NUMBER OF REAL POLES: 0
NUMBER OF COMPLEX POLE PAIRS: 2
FILTER GAIN: 0.00180000

```

Figure 6-11a Pole Zero Locations For Example Two

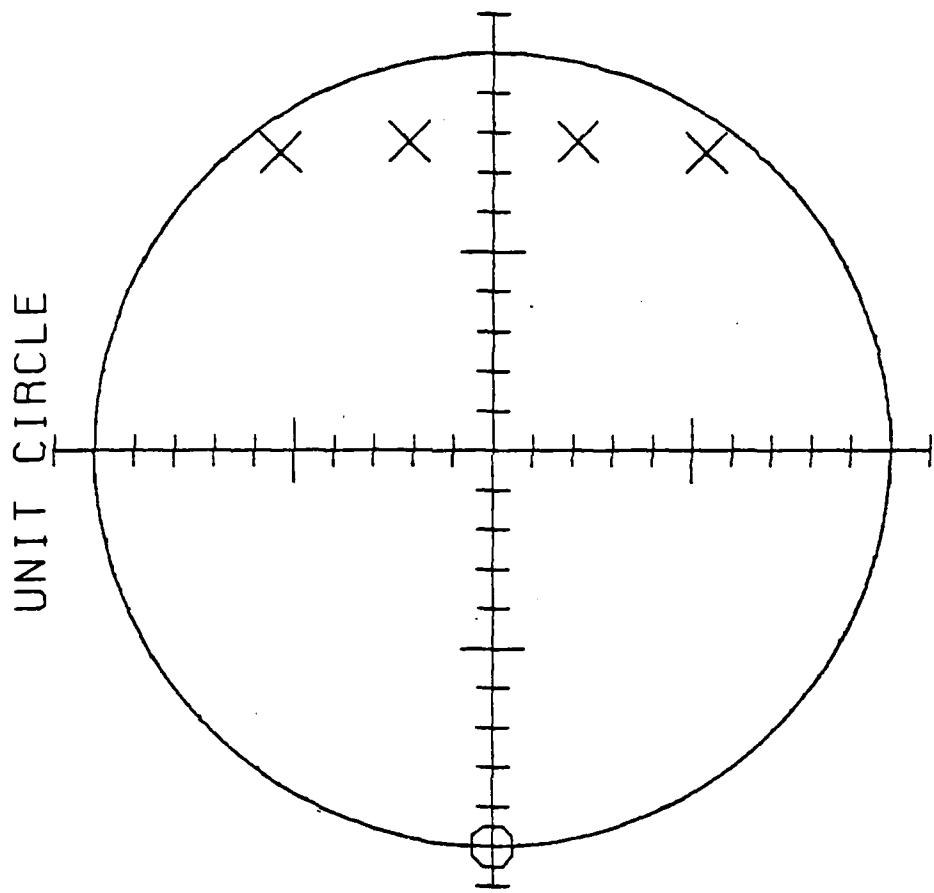


Figure 6-11b Pole Zero Locations For Example Two

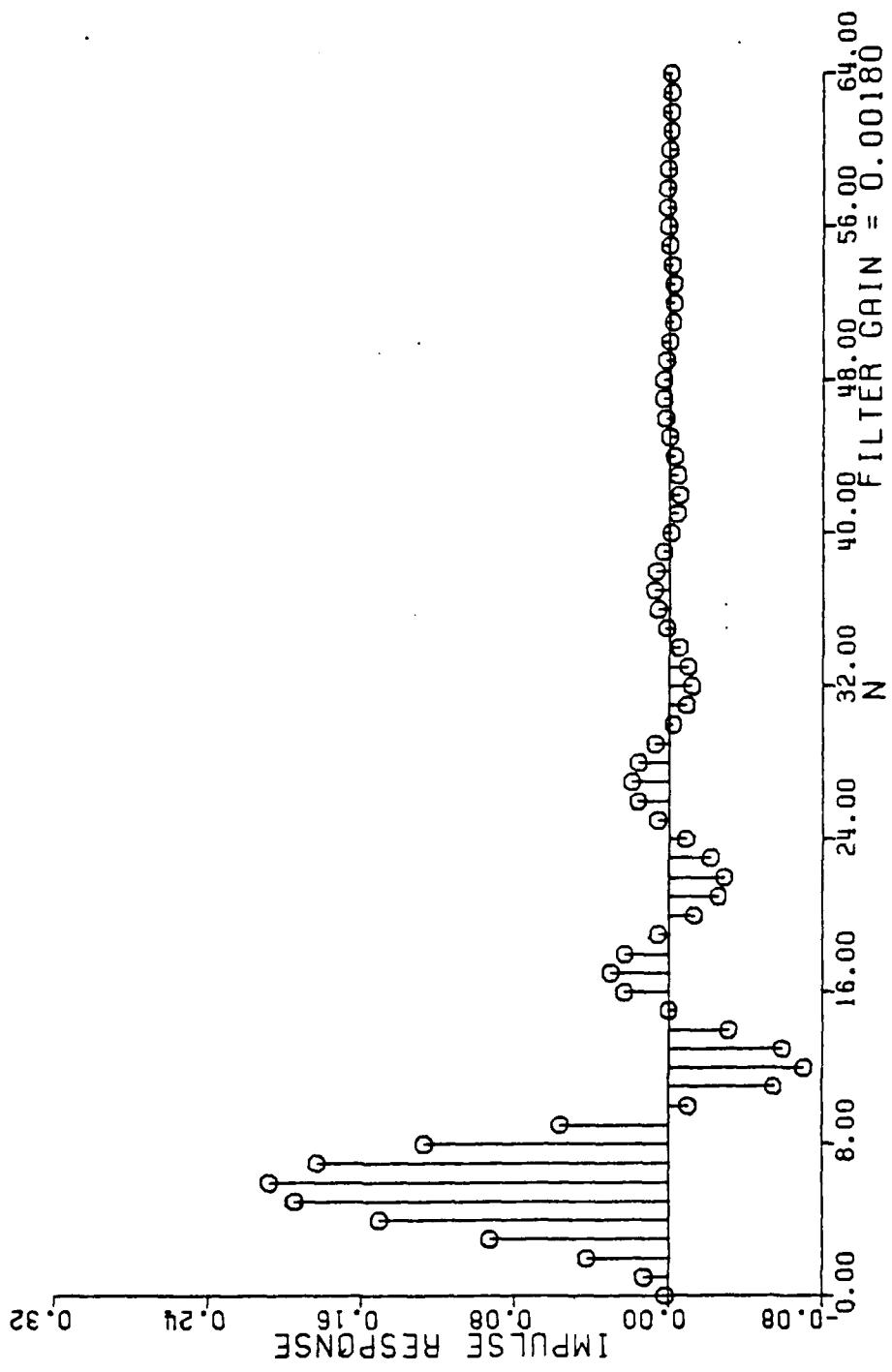


Figure 6-11c Unit Sample Response For Example Two

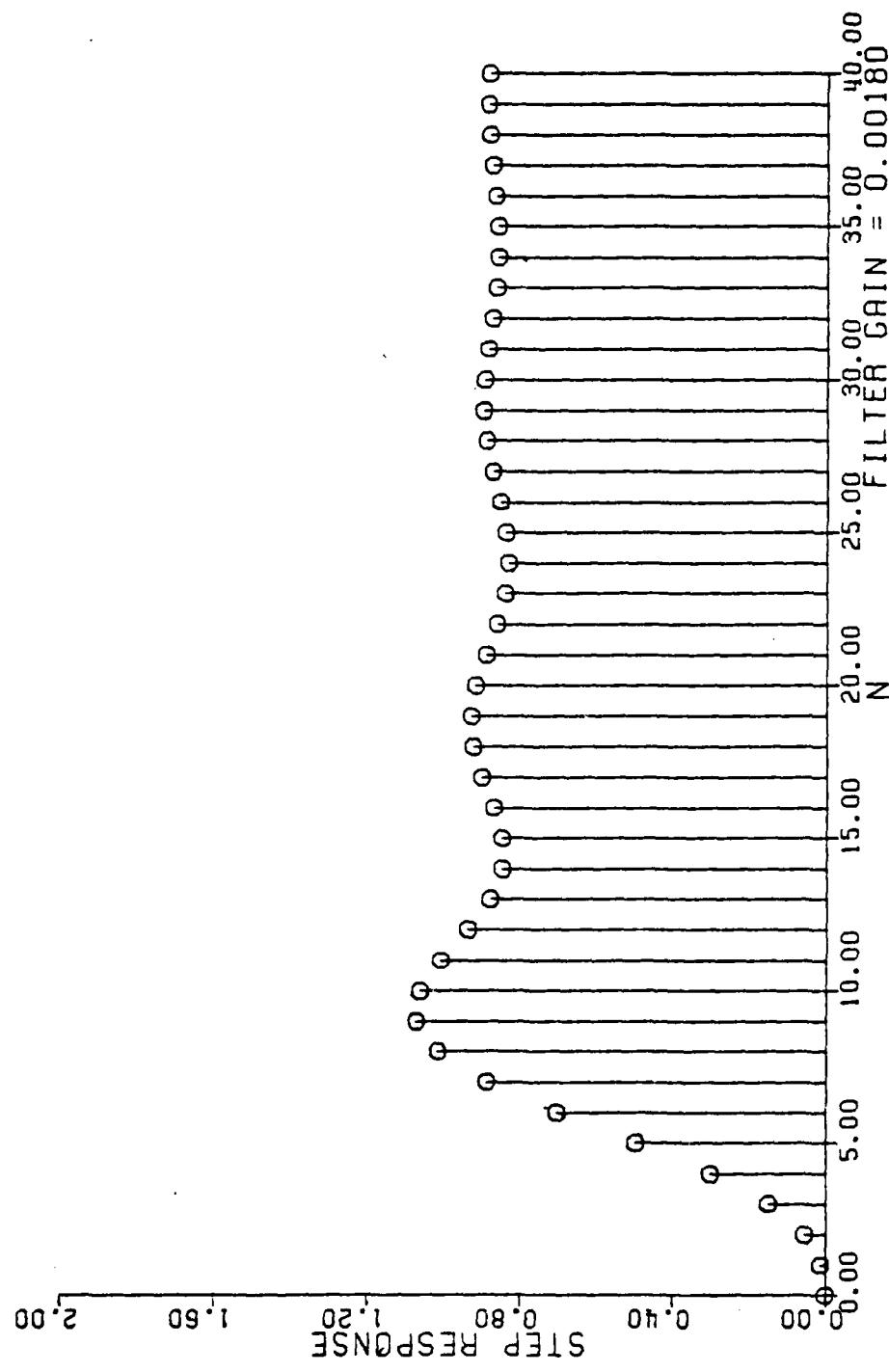


Figure 6-11d Unit Step Response For Example Two

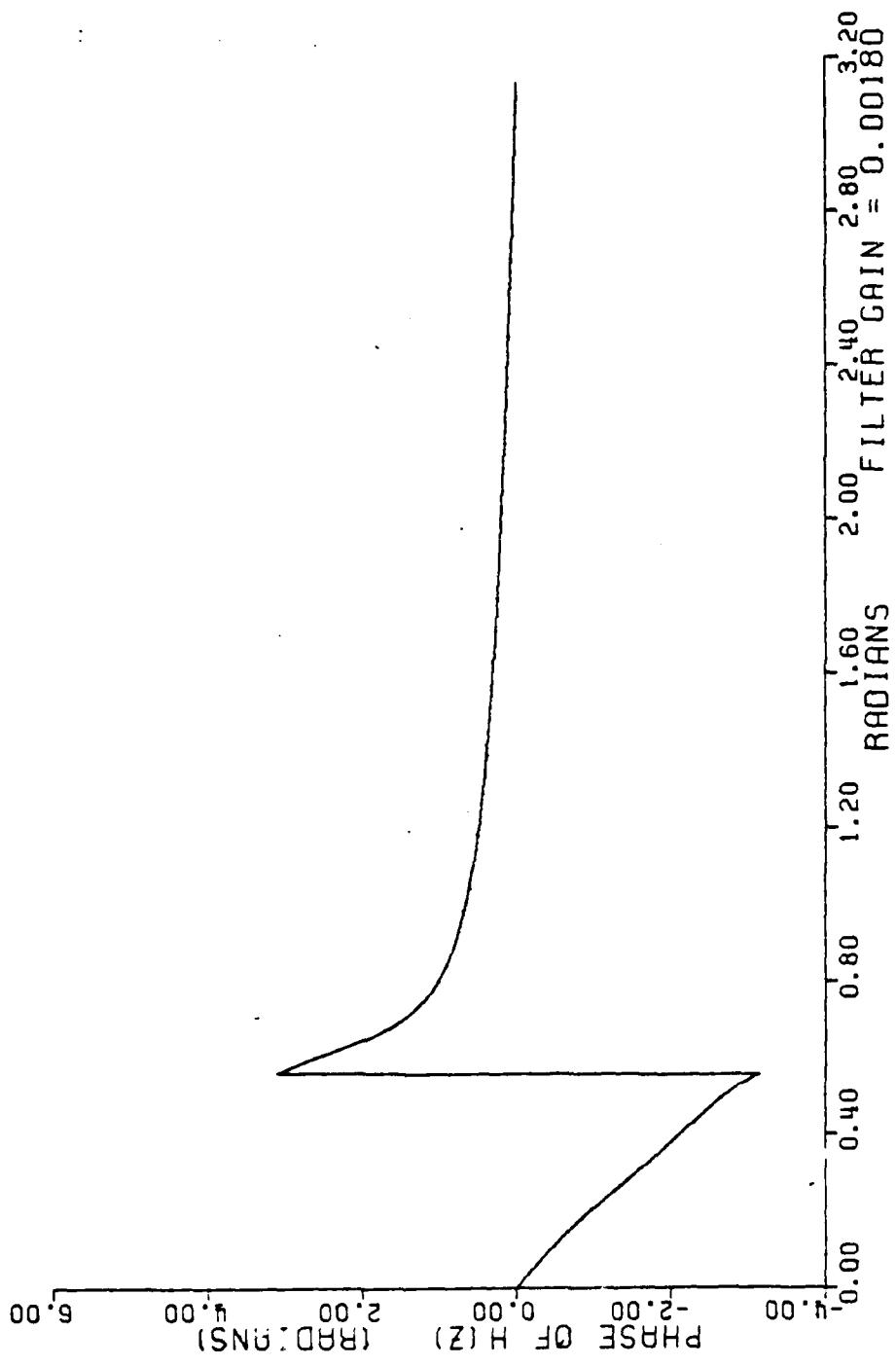


Figure 6-11e Phase Response For Example Two

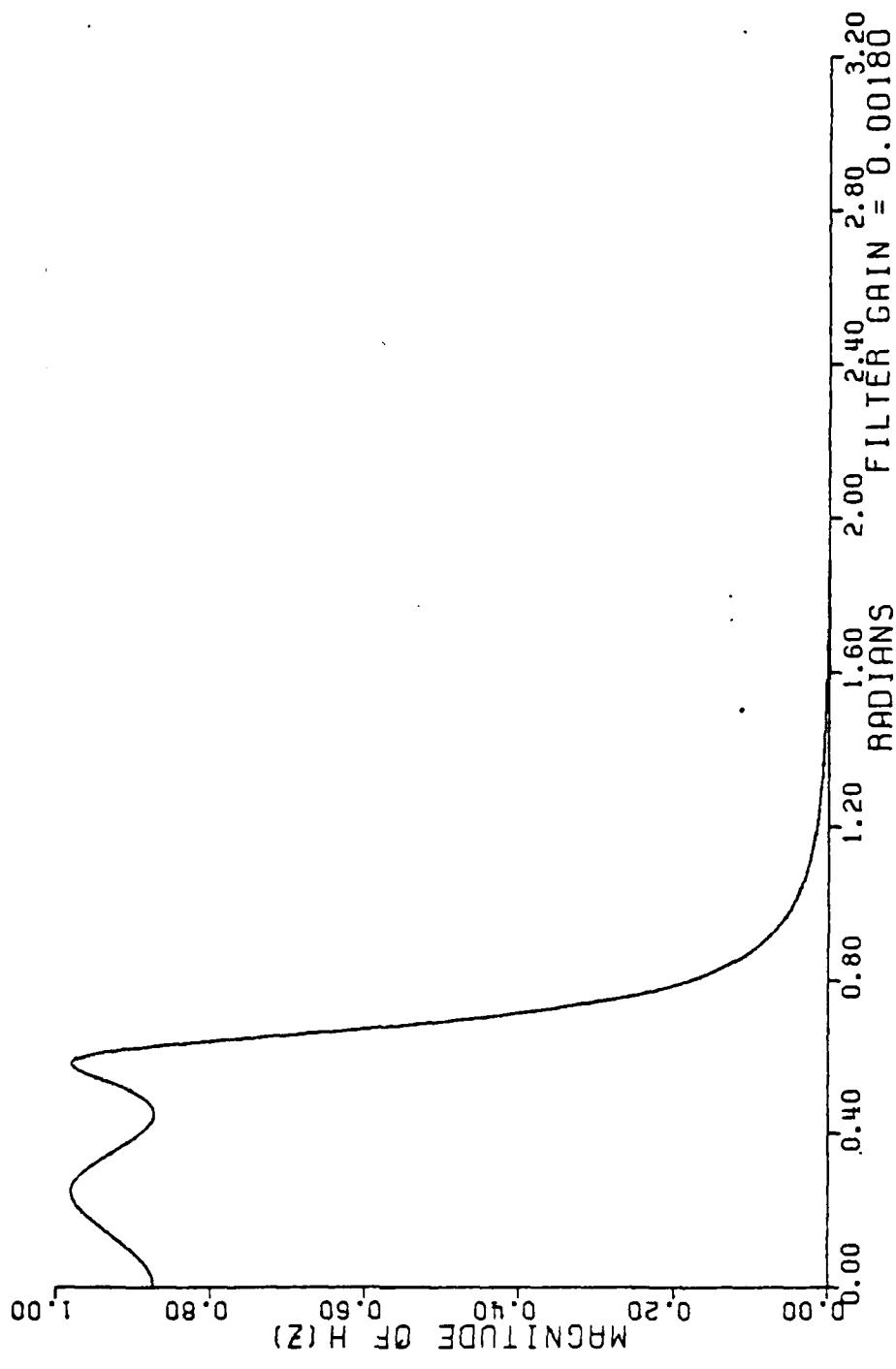


Figure 6-11f Magnitude of  $H(z)$  For Example Two

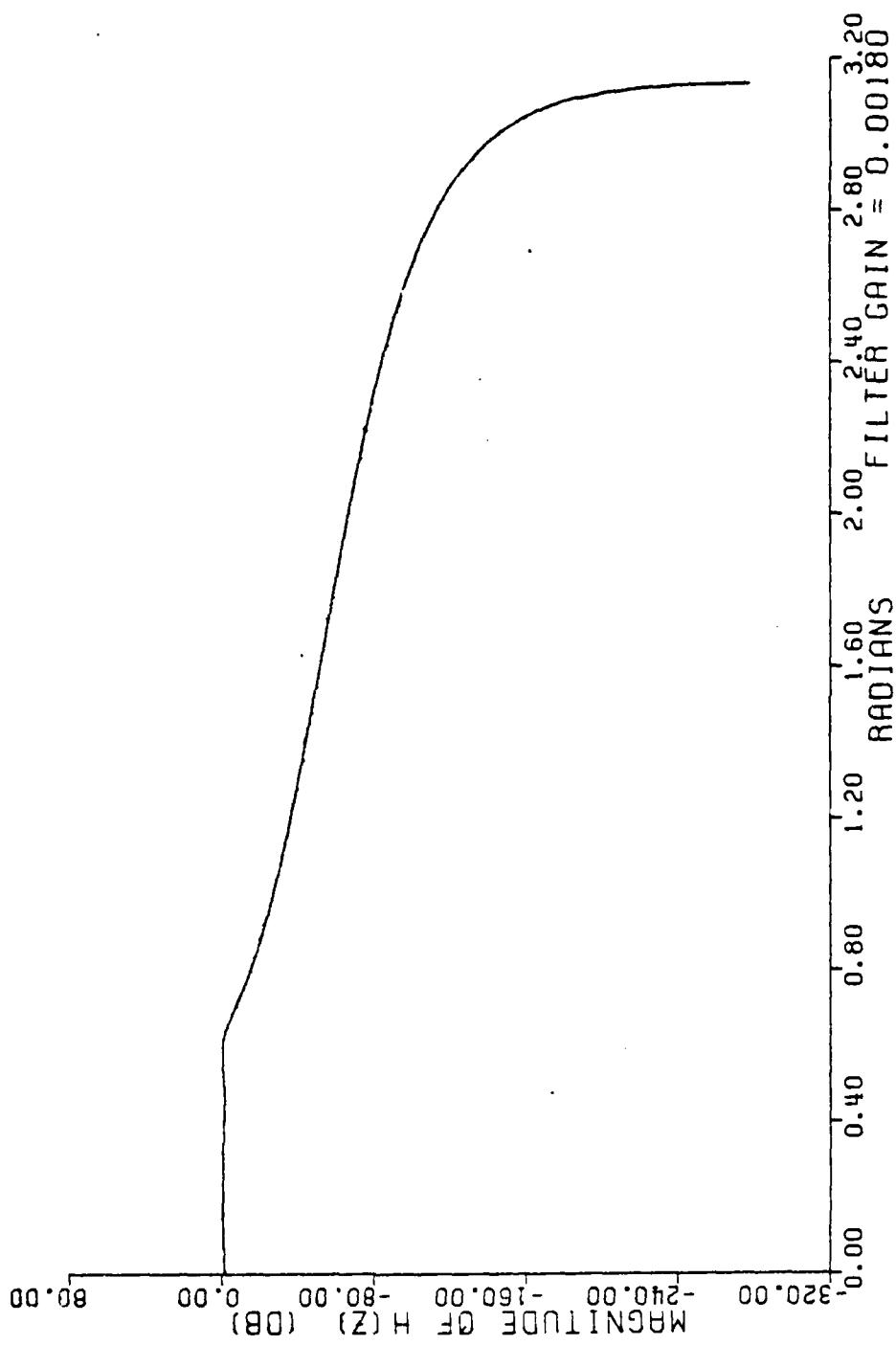


Figure 6-11g Magnitude Of  $H(z)$  In Decibels For Example Two

### C. EXAMPLE THREE - POLAR MODE

This example uses the polar mode to generate an all pass filter. The filter complex pole pairs are to be located at (0.2 at +/- 45 degrees), and (0.5 at +/- 30 degrees). The filter zeros are to be at (5.0 at +/- 45 degrees), and (2.0 at +/- 30 degrees). The filter gain is to be 0.01. The first step is to change the specifications in degrees to radians. Thirty degrees equals .5235 radians. Forty five degrees is .7854 radians. The entry of poles and zeros exactly parallels the above examples, however, the desired commands are ACPPLR, (Add a Complex Pole - Polar Coordinates), and ACZPLR, (Add a Complex Zero - Polar Coordinates). Figure 6-12a shows the trace cursor position for ACPPLR. Figure 6-12b shows the trace cursor position for ACZPLR. The angular part of any pole or zero entered in the polar mode must be in radians. Figure 6-12c shows the entry of the first complex zero pair. Figure 6-12d shows the entry of the first complex pole pair. Figure 6-12e shows the change in filter gain from 1.00 to 0.01. Figures 6-13a through 6-13g show the hard copy responses for this filter. It should be noted that zeros which plot outside of the unit circle are indicated by stars. All such zeros are plotted at a radius of 1.1 along the same angular component as the actual zero location. Zeros are plotted this way for two reasons: first to make the output display consistent for all relevant filters, and second to emphasize zeros which

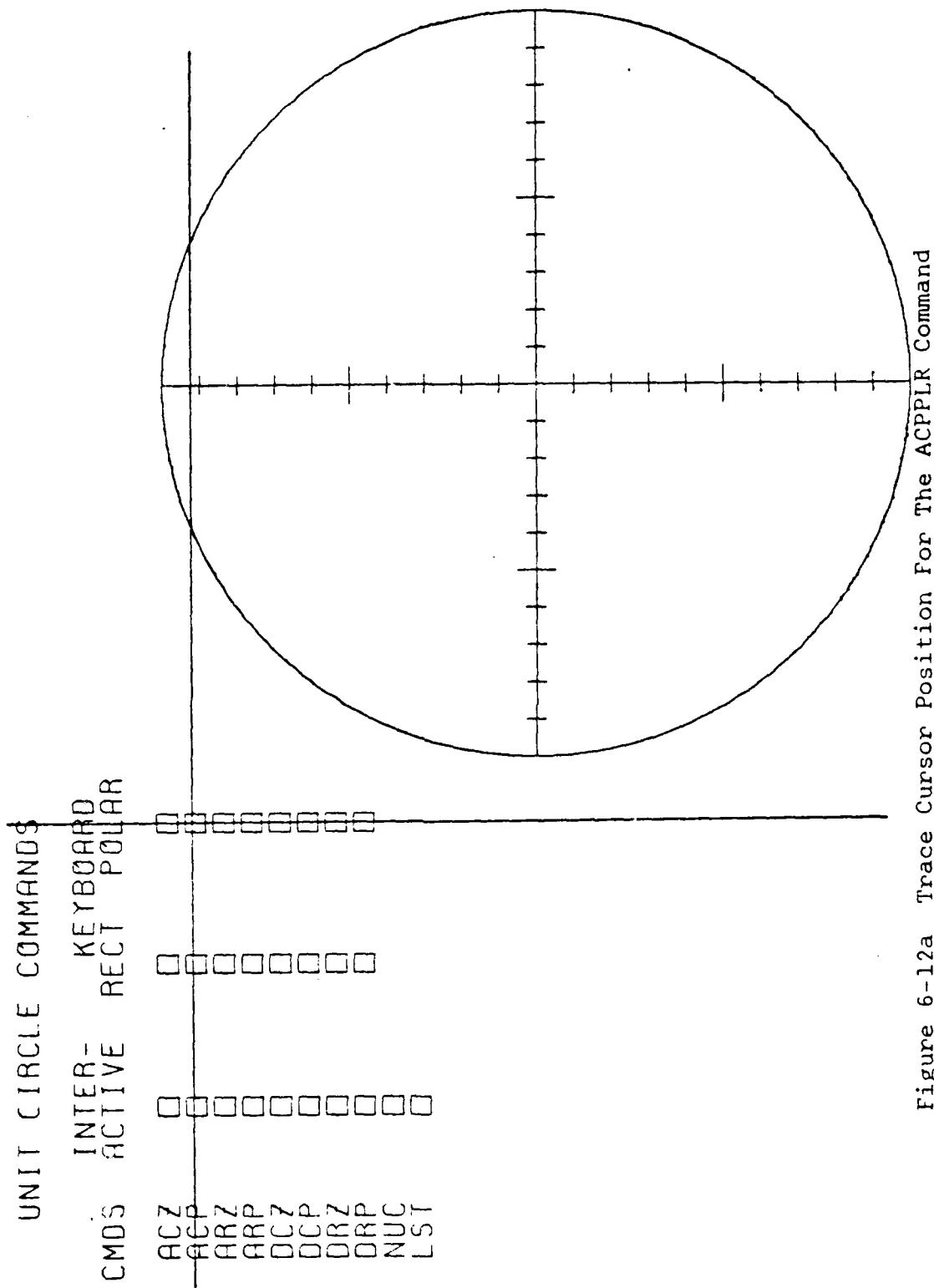


Figure 6-12a Trace Cursor Position For The ACPLR Command

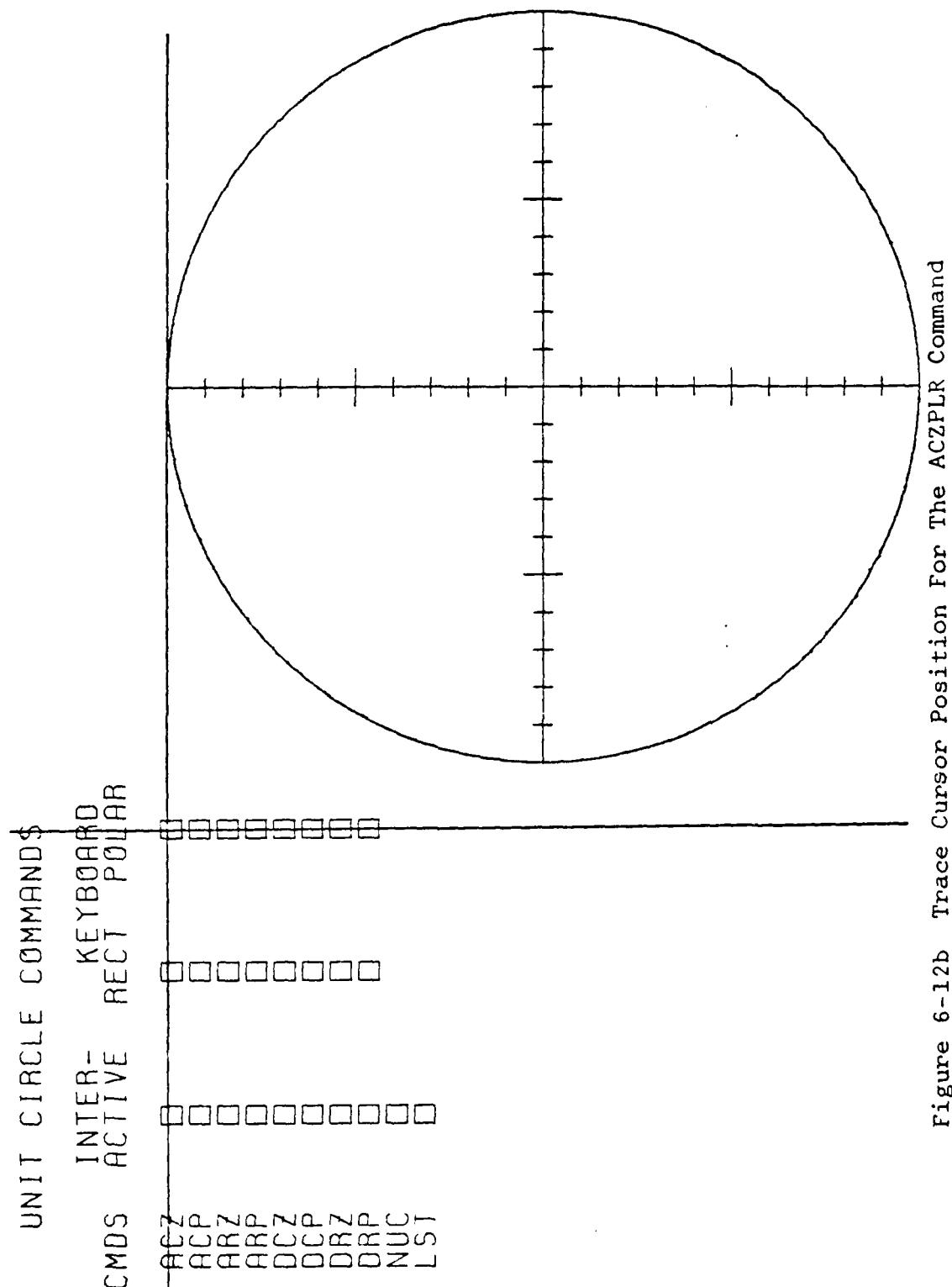


Figure 6-12b Trace Cursor Position For The ACZPLR Command

TO ADD A COMPLEX ZERO TO THE  
DISPLAY, ENTER THE RADIAL AND  
THETA COMPONENTS WITHIN PROVIDED  
BOXES. THE MAGNITUDE OF RHO MUST  
BE LESS THAN TEN, THETA(RADIANS)  
EACH NUMBER REQUIRES A DECIMAL,  
AND AS APPROPRIATE A MINUS SIGN.  
BOTH ARE CONFINED TO THE BOXES.

MAGNITUDE                           ANGLE  
>>  + -

THE NEW COMPLEX ZEROS WILL BE 15.000000 + - $\sqrt{0.7854000}$   
IF CORRECT TYPE 'Y', IF NOT 'N'.

Figure 6-12c Screen Display After Entering The First Complex  
Zero Pair In Polar Coordinates

TO ADD A COMPLEX POLE WITHIN THE  
UNIT CIRCLE ENTER THE RADIAL AND  
THETA COMPONENTS WITHIN PROVIDED  
BOXES. RHO MUST BE ONE OR LESS.  
THETA MUST BE ENTERED IN RADIANS.  
EACH NUMBER REQUIRES A DECIMAL,  
AND AS APPROPRIATE A MINUS SIGN.  
BOTH ARE CONFINED TO THE BOXES.

MAGNITUDE                           ANGLE  
  >> + / -

THE NEW COMPLEX POLES WILL BE 0.20000000 + / - 0.7854000  
IF CORRECT TYPE 'Y', IF NOT 'N'.

Figure 6-12d Screen Display After Entering The First Complex Pole Pair In Polar Coordinates

THE FILTER GAIN IS CURRENTLY 1.00000000

DO YOU WISH TO CHANGE THE FILTER GAIN?

(TYPE Y OR N)

TYPE IN THE NEW FILTER GAIN 12 OR FEWER NUMBERS  
INCLUDE A DECIMAL POINT

>0.01

NEW FILTER GAIN IS: 0.01000000

Figure 6-12e Screen Representation After Changing Filter Gain

```

Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z
Z REAL Z INAGINARY Z RHO Z THE T A Z
Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z
Z 3.5355272 Z + / - 3.5355396 Z 5.0000000 Z + / - 0.7854000 Z + / - 0.5235003 Z
Z 1.7321472 Z + / - 0.998287 Z 2.0000000 Z + / - 0.0100000 Z + / - 0.0100000 Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z * * * * * Z
Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P
P 0.1414211 P + / - 0.1414216 P 0.2499570 P 0.5000000 P + / - 0.7854000 P + / - 0.5235000 P
P 0.4330373 P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P
P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P * * * * * P

```

NUMBER OF REAL ZEROES: 0  
 NUMBER OF COMPLEX ZERO PAIRS: 2  
 NUMBER OF REAL POLES: 0  
 NUMBER OF COMPLEX POLE PAIRS: 2  
 FILTER GAIN: 0.0100000

Figure 6-13a Pole Zero Locations For Example Three

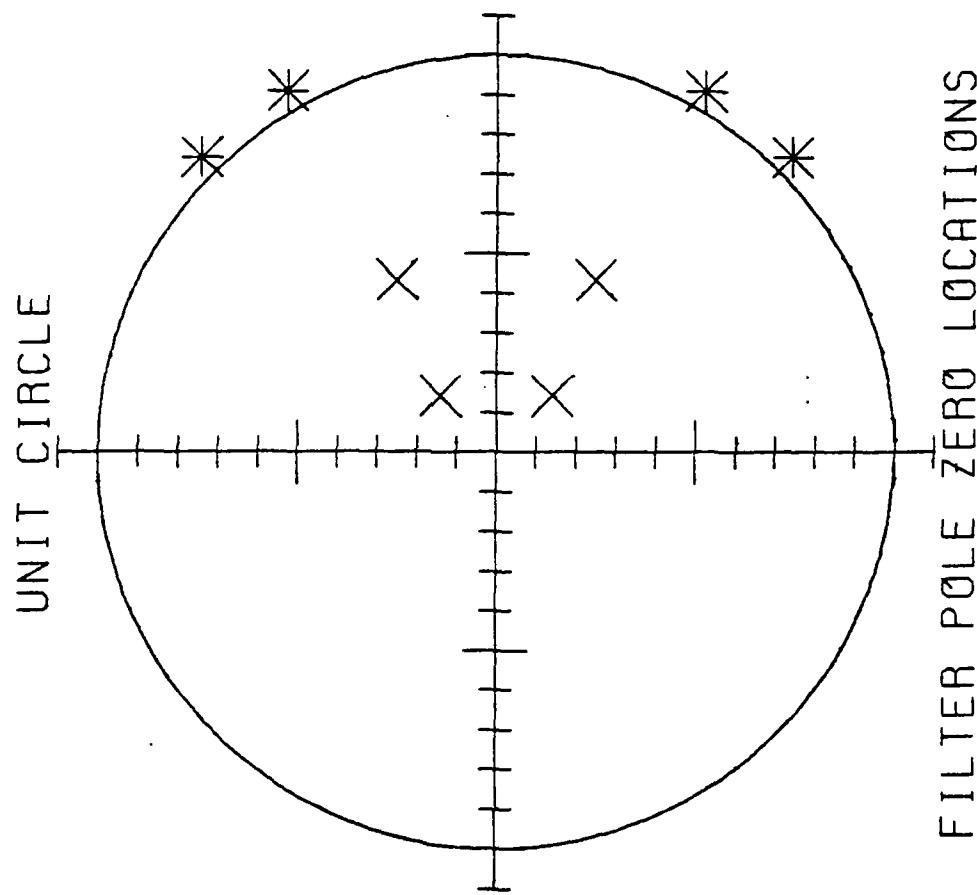


Figure 6-13b Pole Zero Location For Example Three

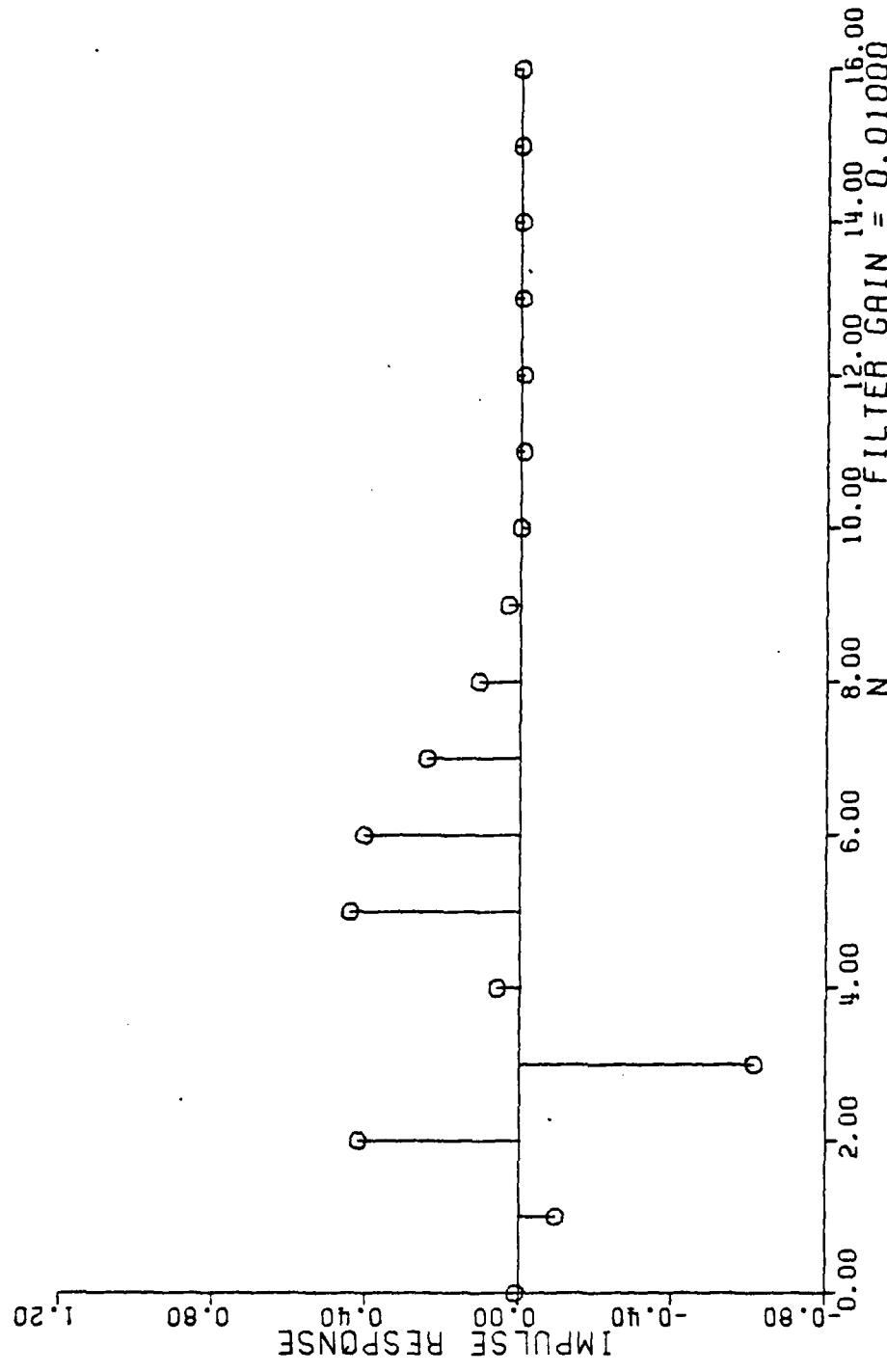


Figure 6-13c Unit Sample Response For Example Three

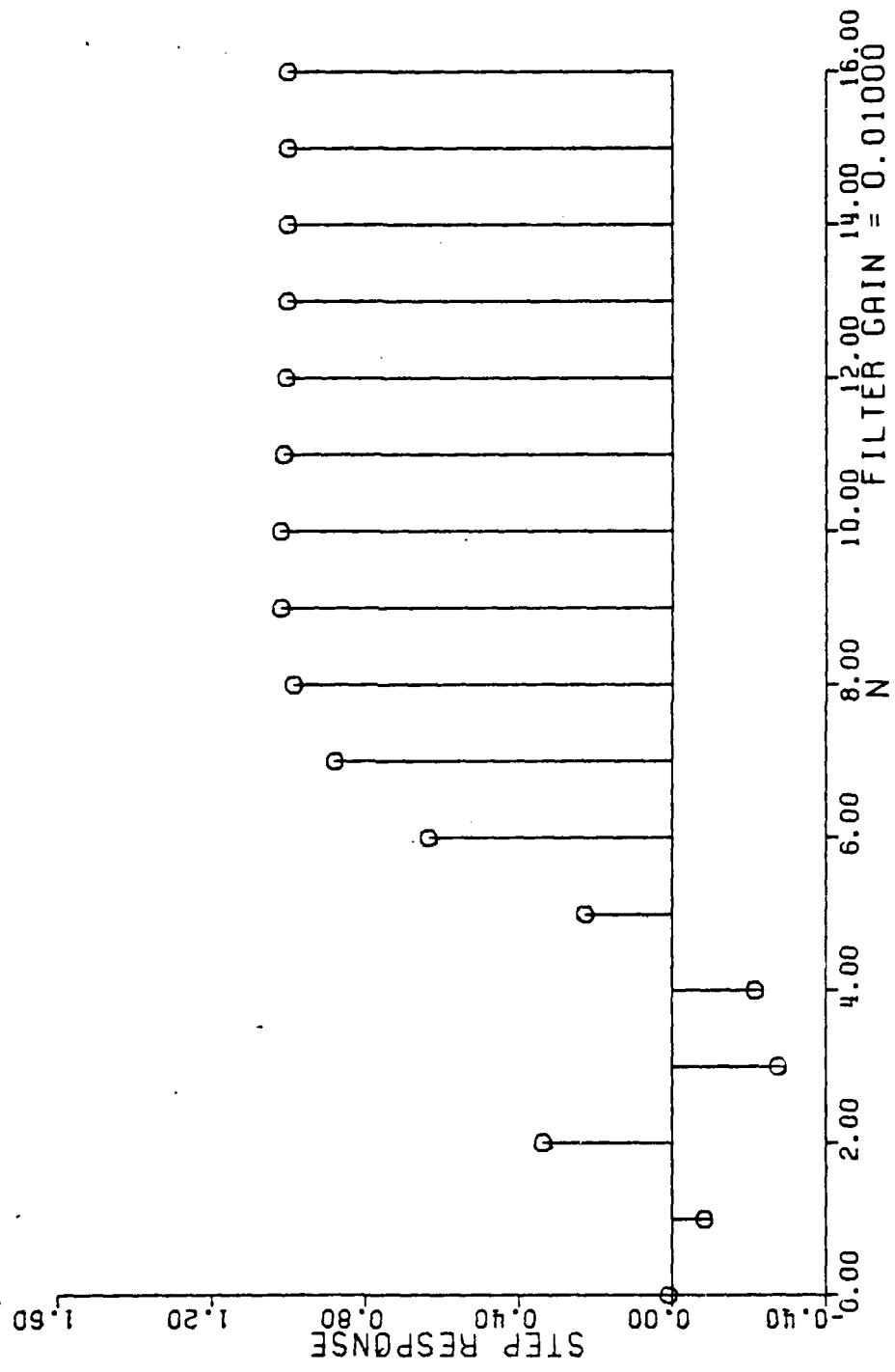


Figure 6-13d Unit Step Response For Example Three

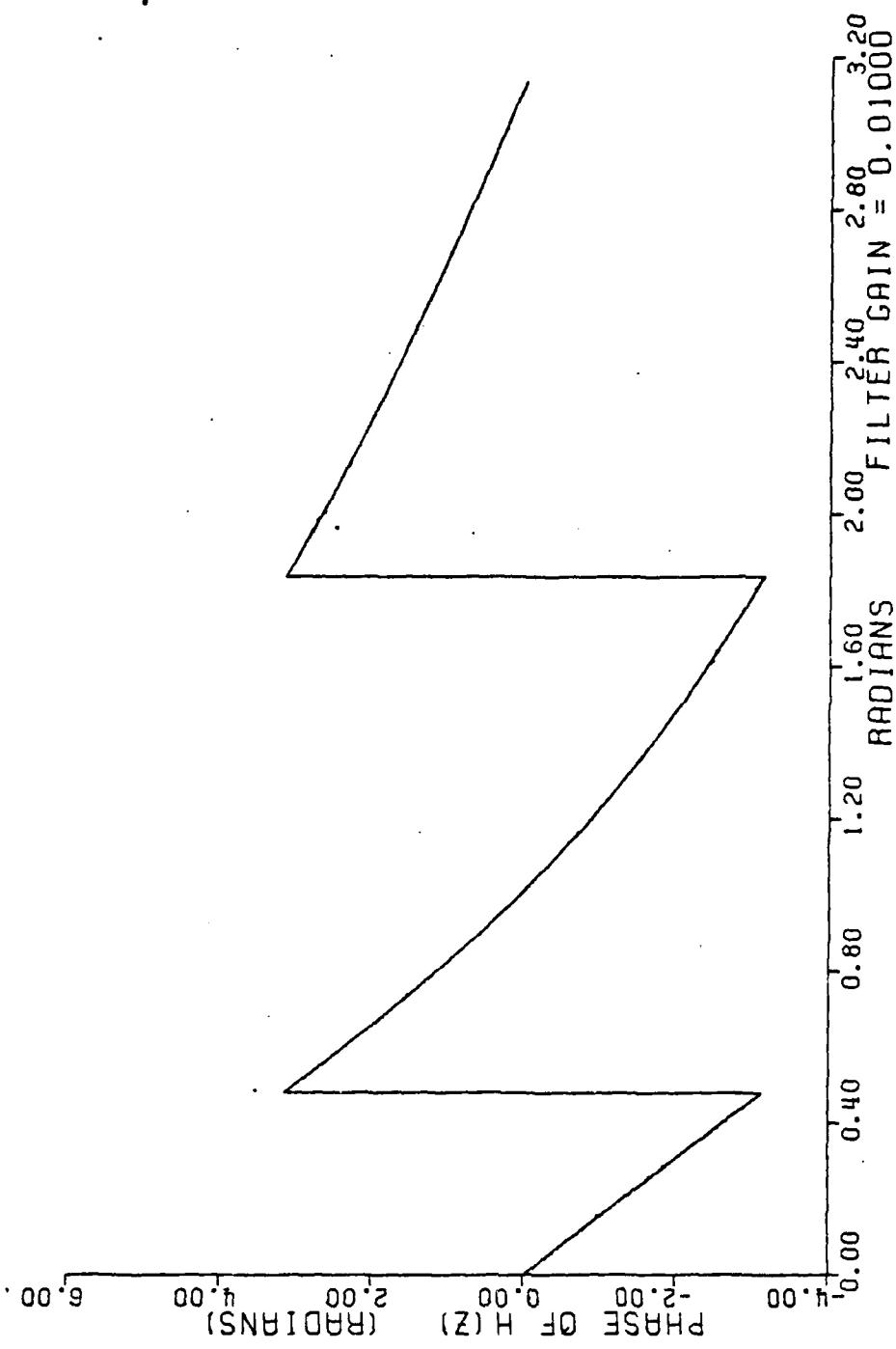


Figure 6-13e Phase Response For Example Three

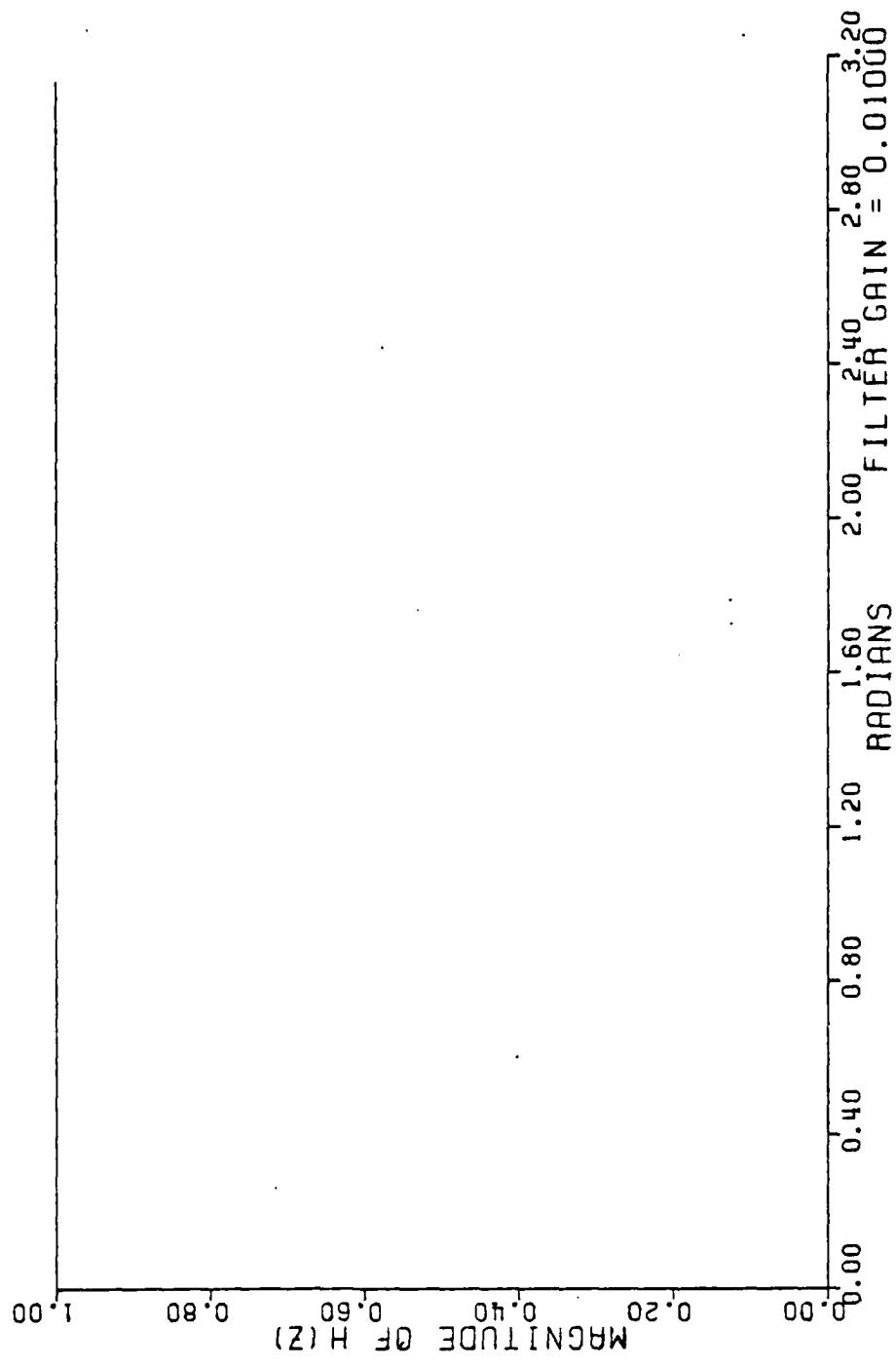


Figure 6-13f Magnitude Of  $H(z)$  For Example Three

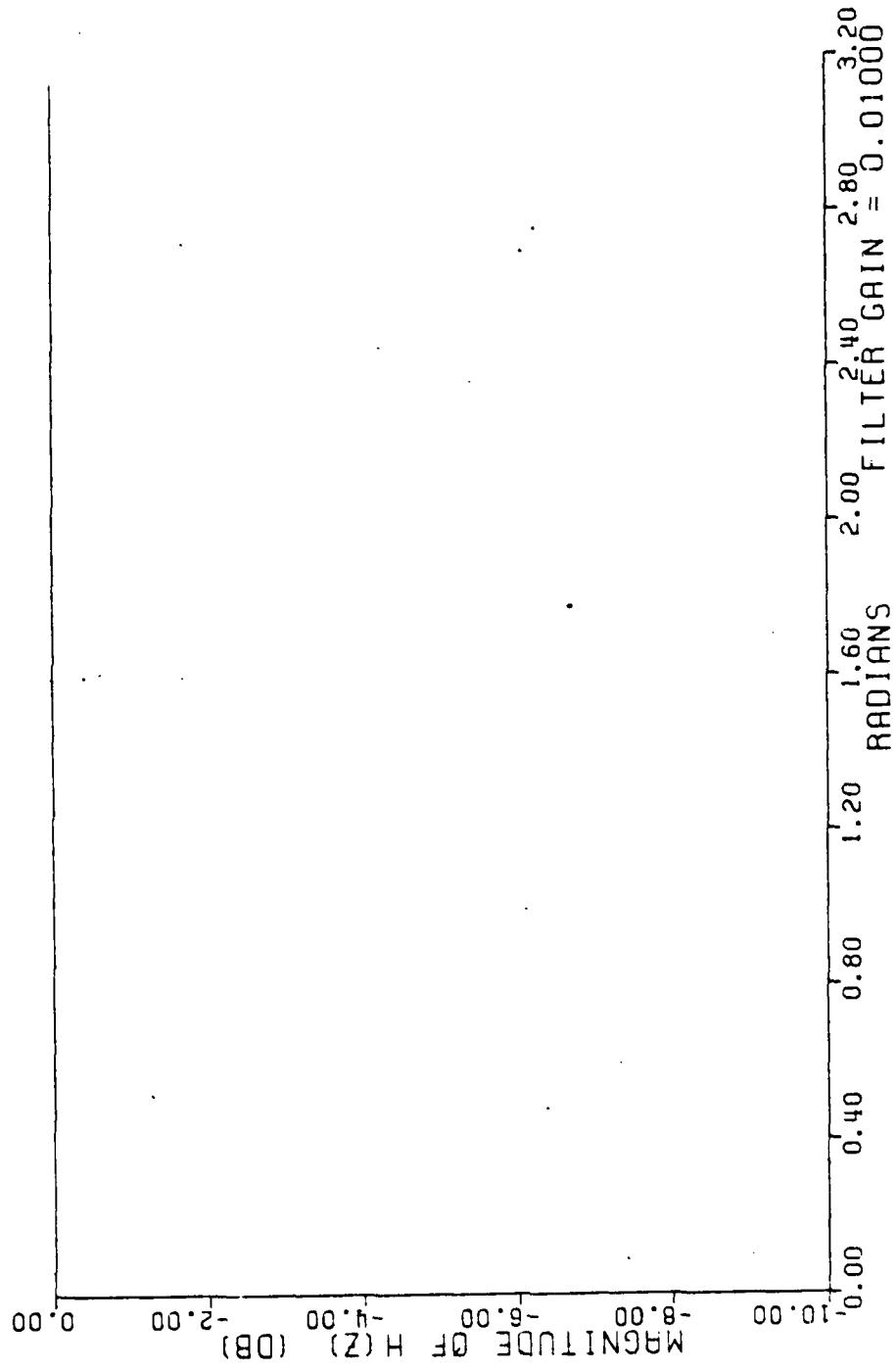


Figure 6-13g Magnitude Of  $H(z)$  In Decibels For Example Three

are close to, but outside, the unit circle. The importance of distinguishing between zeros very near the unit circle, either interior or exterior, rests on the extreme sensitivity of the phase of the frequency response as a zero moves from the interior, onto, and to the exterior of the unit circle.

## VII. ADDITIONAL EXAMPLES

The purpose of this chapter is threefold. The primary objective is to provide the user with a series of plots demonstrating the general form of those types of filters not considered in chapter six. Additionally, this chapter demonstrates the responses generated by poles located at a series of positions within the unit circle. It further provides examples for user comparison when learning to interact with the z-plane.

The filters considered in the examples of chapter six include a fourth-order low-pass filter and a second-order all-pass filter. The sequence of figures 7-1a through 7-1g shows the general pole zero placements for a high-pass filter, and associated responses. Similarly, figure 7-2a through 7-2g show the responses for a band-pass filter. Figures 7-3a through 7-3g show a band-reject or notch filter.

The secondary purpose of the chapter is to show the user the general forms of time and frequency responses as the filter poles move in the z-plane. The sequence of figures 7-4 through 7-11 shows the responses for a real pole at various locations on the real axis. Figures 7-12 through 7-19 similarly show the responses of a complex pole pair moving across the z-plane. Frequency responses are not

shown for poles on, or outside of, the unit circle since the frequency response is not defined for these cases. Figures 7-17, 7-20, and 7-21 show the change in responses for a pair of complex poles which move away from the real axis.

The final intent of the chapter is to provide the user with additional figures for comparison should he need further practice in manipulating poles and zeros in the z-plane. It is important to note that the ASDF program will not allow the user to position poles on or outside the unit circle. This limitation results in several plots which can not be reproduced by the user.

AD-A093 252

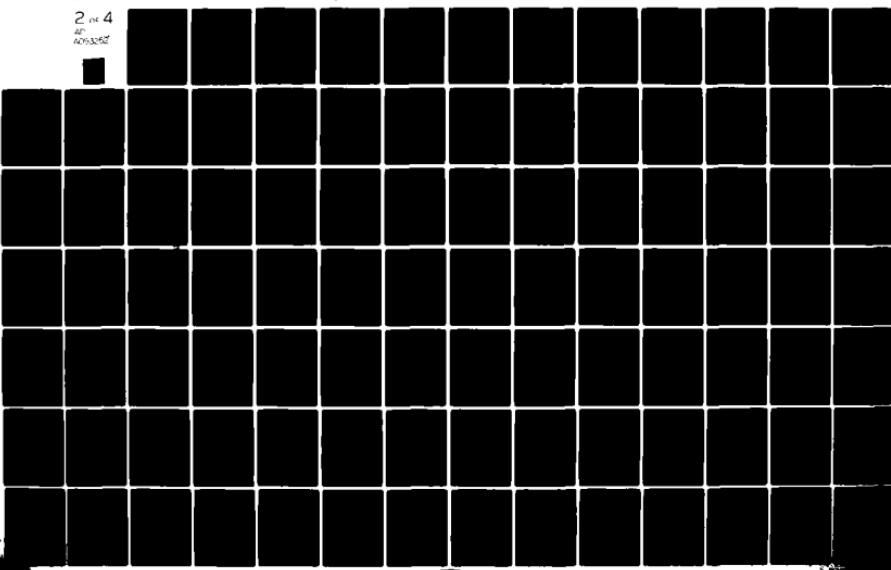
NAVAL POSTGRADUATE SCHOOL MONTEREY CA  
ADVANCED SIMULATION OF DIGITAL FILTERS. (U)  
SEP 80 G S DOYLE

F/6 9/3

UNCLASSIFIED

NL

2 of 4  
40  
REF ID: A65252



```

Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z
Z REAL          Z IMAGINARY       Z RHO           Z RT    Z
Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z
Z 1.4694920   Z 0.0            Z 1.4694920   Z RZ   Z
Z 0.6805066   Z 0.0            Z 0.6805066   Z RZ   Z
Z ****Z****Z  *Z ****Z****Z  *Z ****Z****Z  *Z ****Z****Z
Z *****Z*****Z *****Z*****Z *****Z*****Z *****Z*****Z
Z P P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P
P 0.1697227 P +/_ 0.3893862 P 0.4247673 P +/_ 1.1597509 P C P P
P *****P*****P *****P*****P *****P*****P *****P*****P
P P P P P P P P P P P P P P P P P P P P P P P P P P P P P P P

```

```

NUMBER OF REAL ZEROES: 2
NUMBER OF COMPLEX ZERO PAIRS: 0
NUMBER OF REAL POLES: 0
NUMBER OF COMPLEX POLE PAIRS: 1
FILTER GAIN: 0.36697245

```

Figure 7-1a Pole Zero Locations For A Second-Order High-Pass Filter

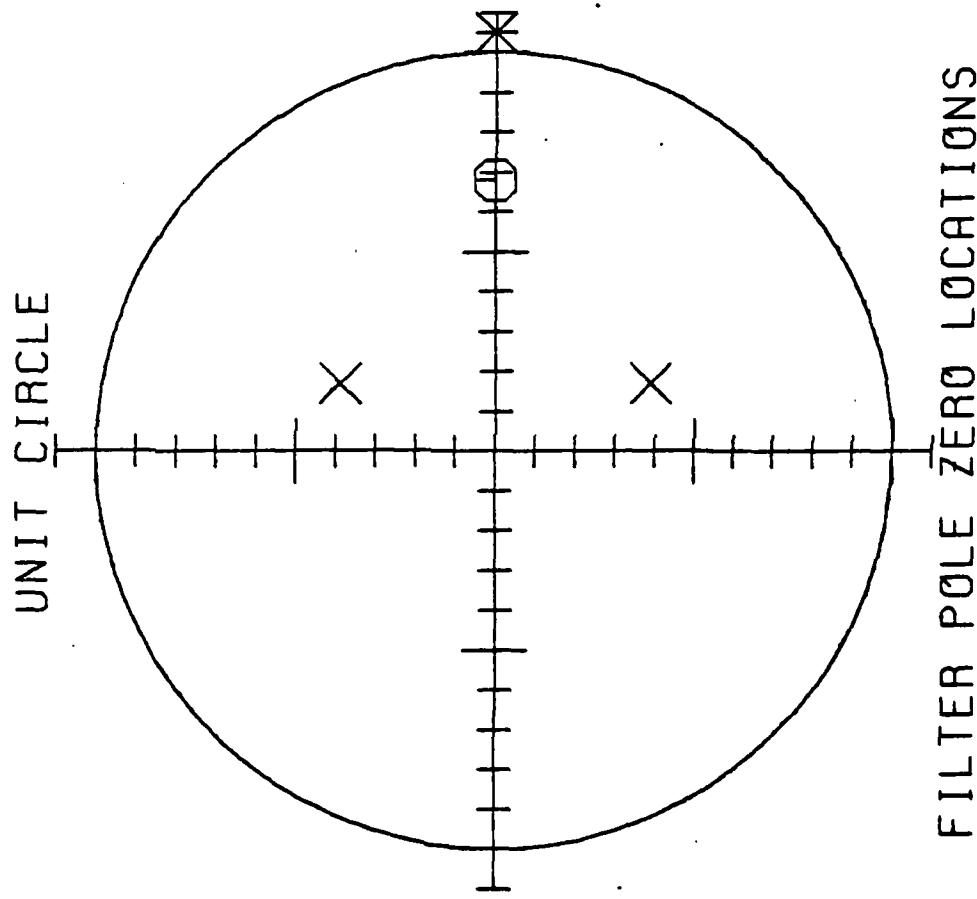


Figure 7-1b Plot Of Pole Zero Locations For A Second-Order High-Pass Filter

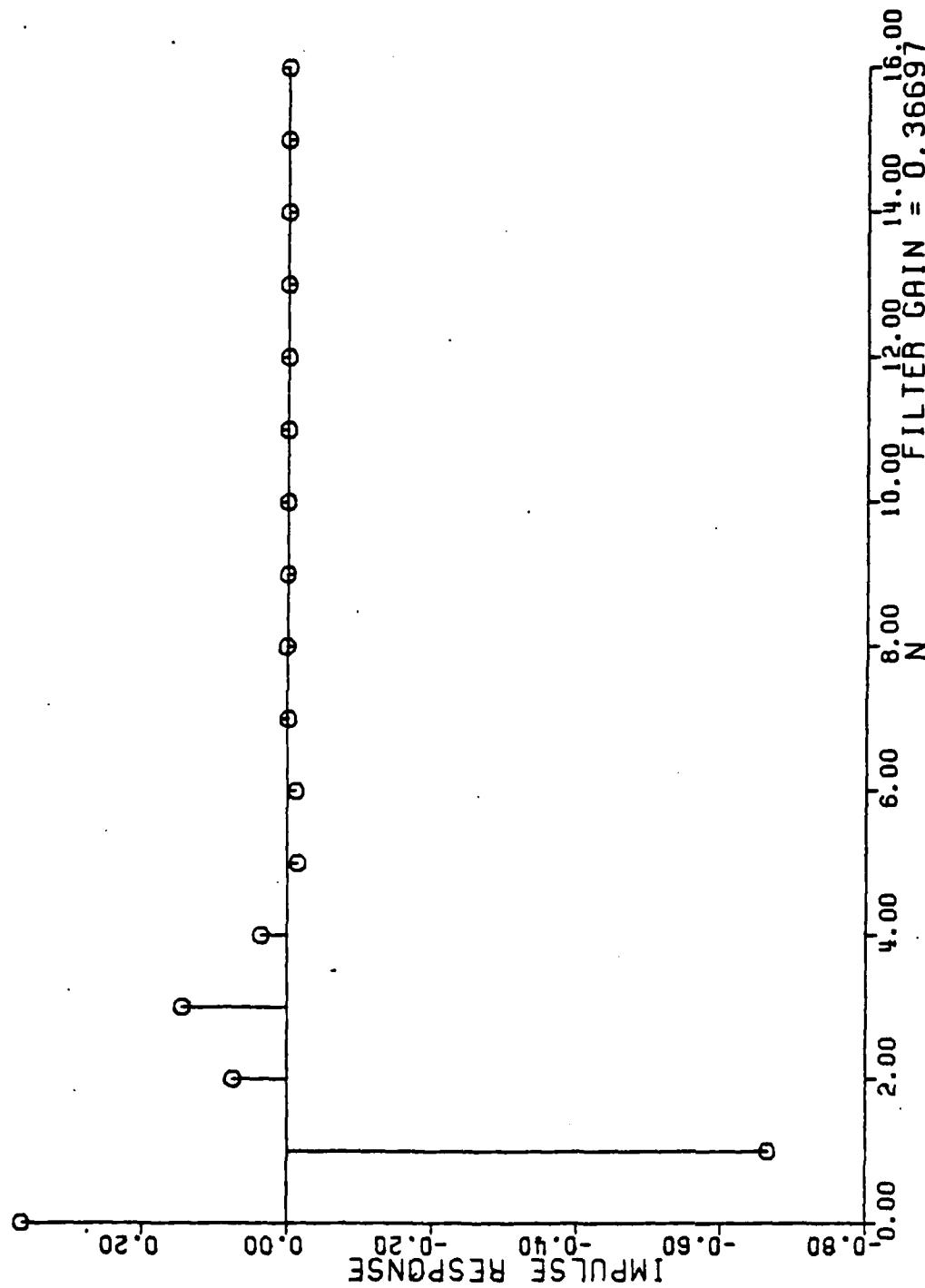


Figure 7-1c Unit Sample Response For A Second-Order High-Pass Filter

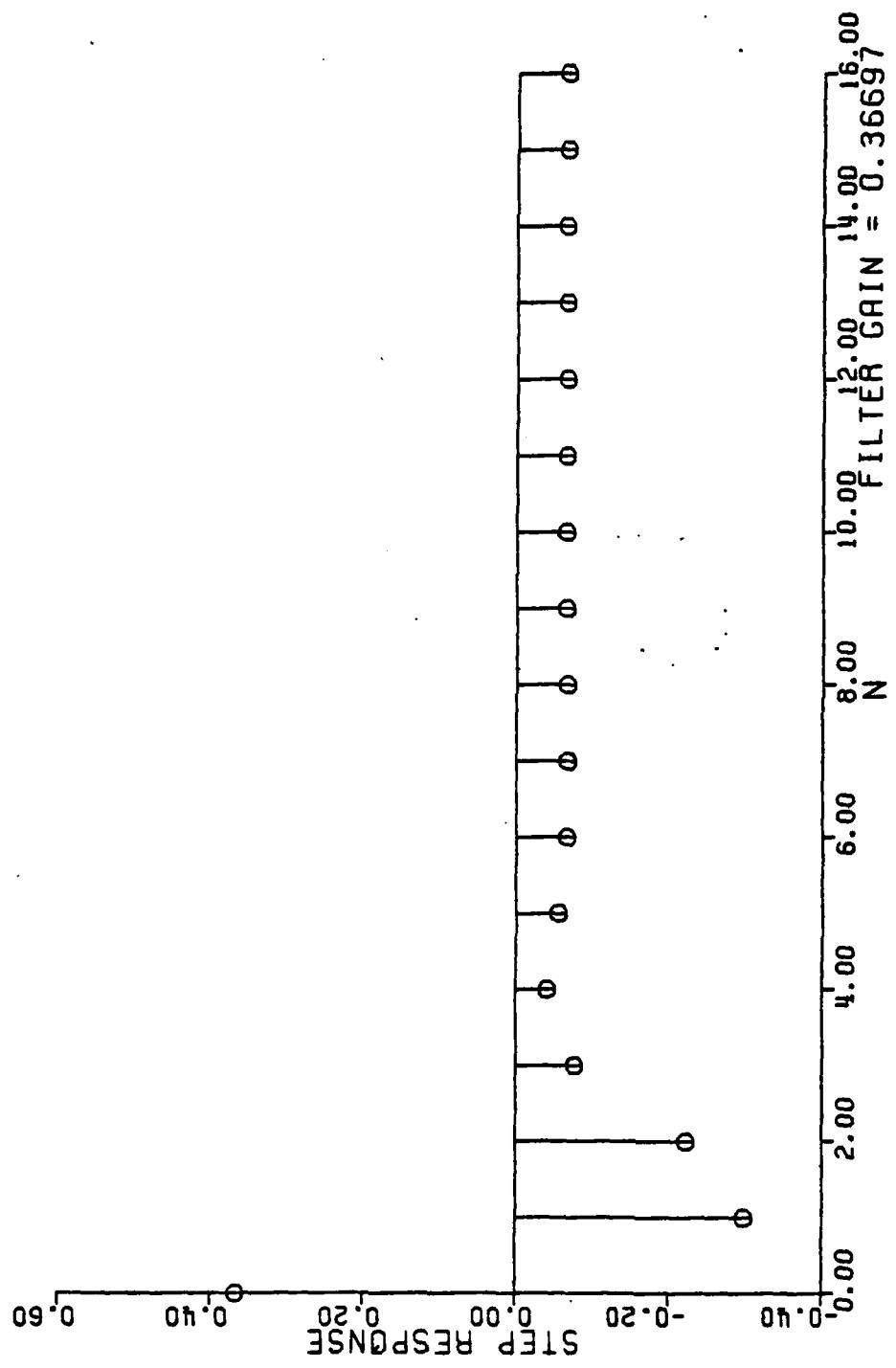


Figure 7-1d Unit Step Response For A Second-Order High-Pass Filter

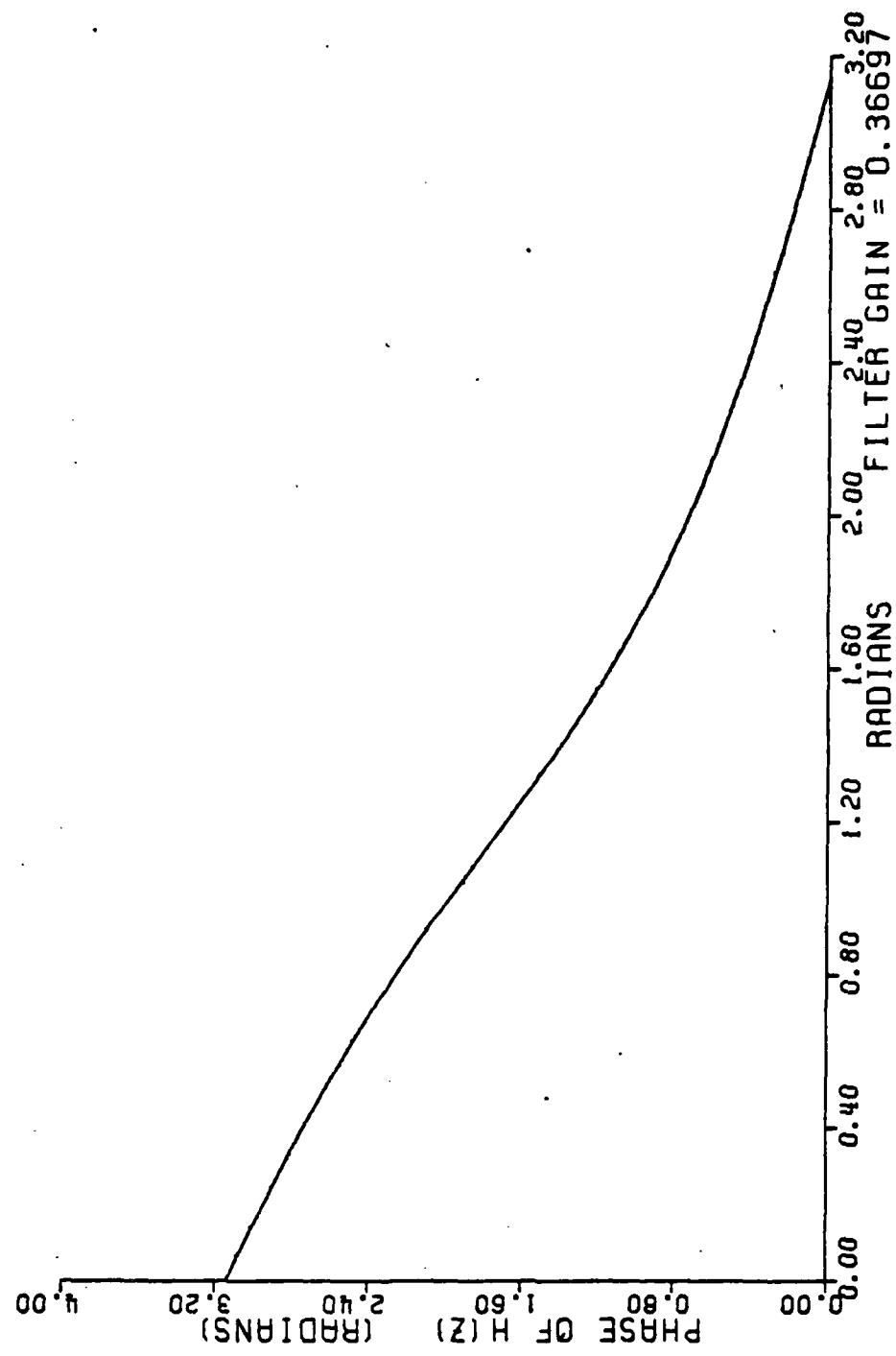


Figure 7-1e Phase Response For A Second-Order High-Pass Filter

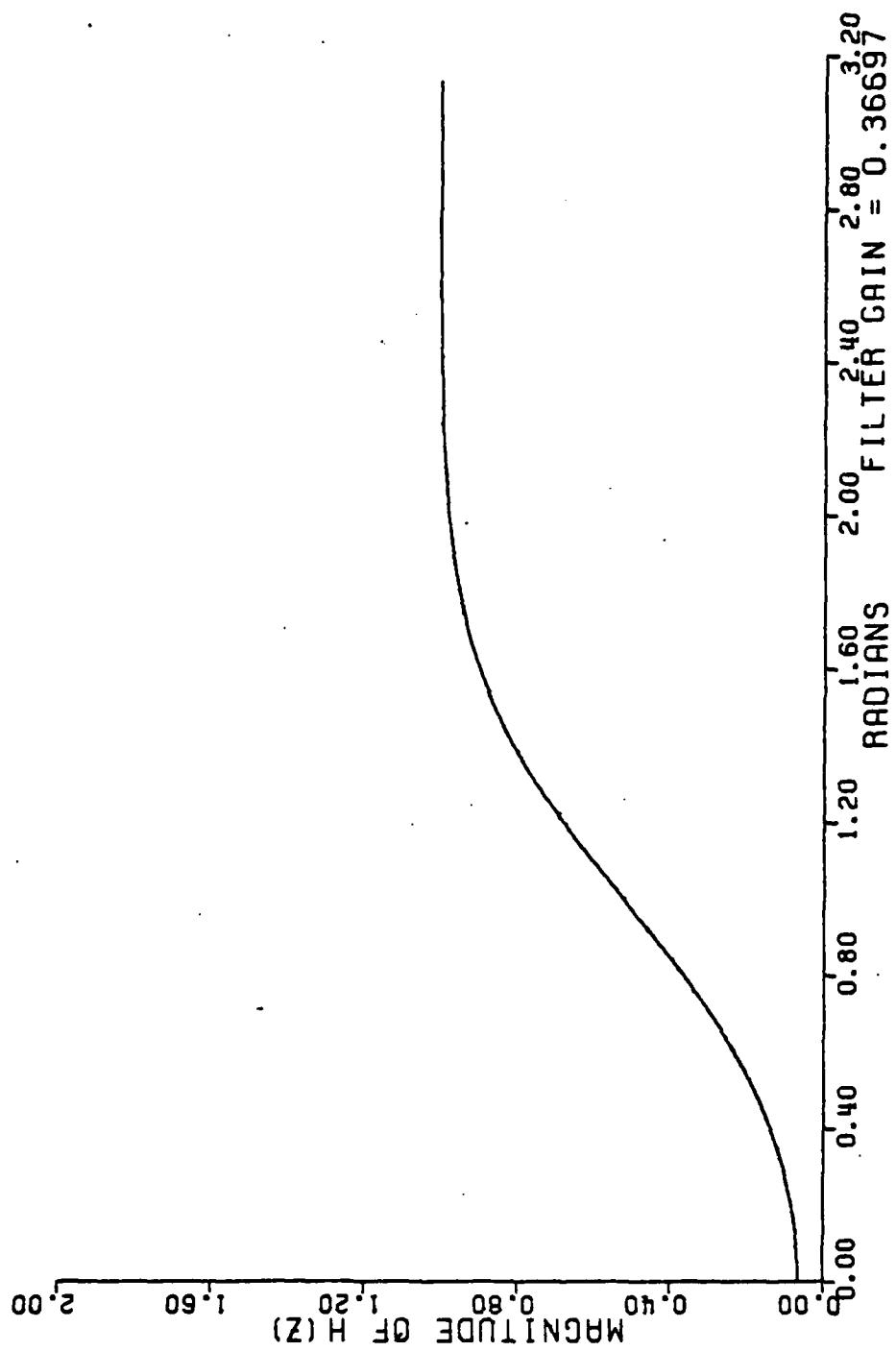


Figure 7-1f Magnitude Of  $H(z)$  For A Second-Order High-Pass Filter

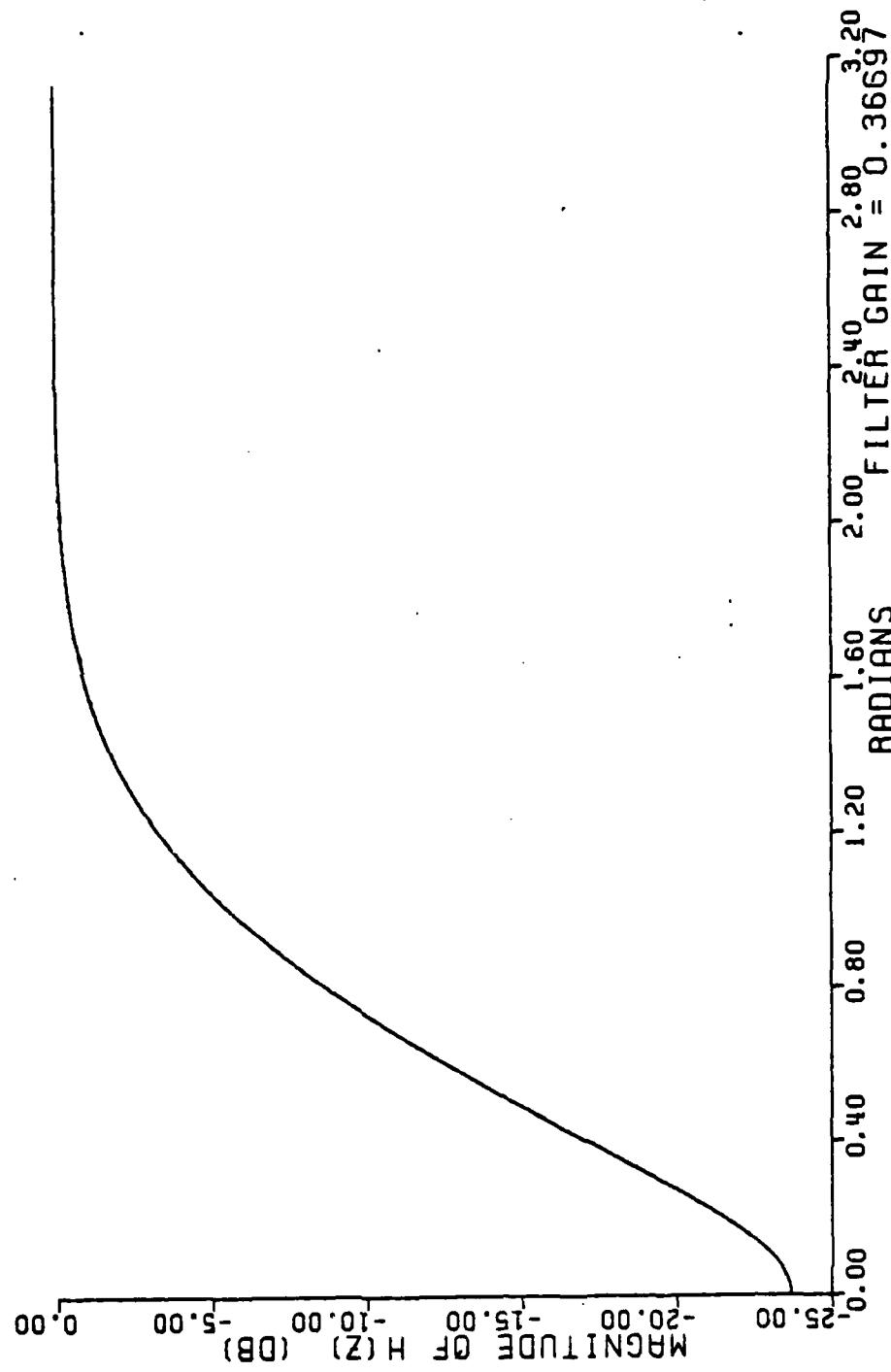


Figure 7-1g Magnitude Of  $H(z)$  In Decibels For A Second-Order High-Pass Filter

Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z  
 Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z  
 Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z  
 Z REAL Z IMAG INARY Z RHO Z ETA Z  
 Z 0.3459291 Z 0.0 Z 0.3459291 Z 0.0 Z  
 Z -0.3459291 Z 0.0 Z 0.3459291 Z 0.0 Z  
 Z -2.8907642 Z 0.0 Z 2.8907642 Z 0.0 Z  
 Z 2.8907642 Z 0.0 Z -2.8907642 Z 0.0 Z  
 Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\*  
 Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\*  
 Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\*  
 Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\*  
 Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\*  
 Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\*  
 Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\*  
 Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\* Z \*\*\* \* \*\*\*  
 Z P P Z P P Z P Z P Z P Z P Z P Z P Z P Z P Z P  
 P 0.1797063 P +/- 0.7802912 P 0.8007175 P +/-
 P -0.1797063 P +/- 0.7802912 P 0.8007175 P +/-
 P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\*  
 P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\*  
 P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\*  
 P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\*  
 P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\*  
 P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\*  
 P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\* P \*\*\* \* \*\*\*

NUMBER OF REAL ZEROES: 4 PAIRS: 0  
 NUMBER OF COMPLEX ZERO PAIRS: 0  
 NUMBER OF REAL POLES: 0 PAIRS: 2  
 NUMBER OF COMPLEX POLE PAIRS: 2  
 FILTER GAIN: 0.02473500

Figure 7-2a Pole Zero Locations For A Fourth-Order Band-Pass Filter

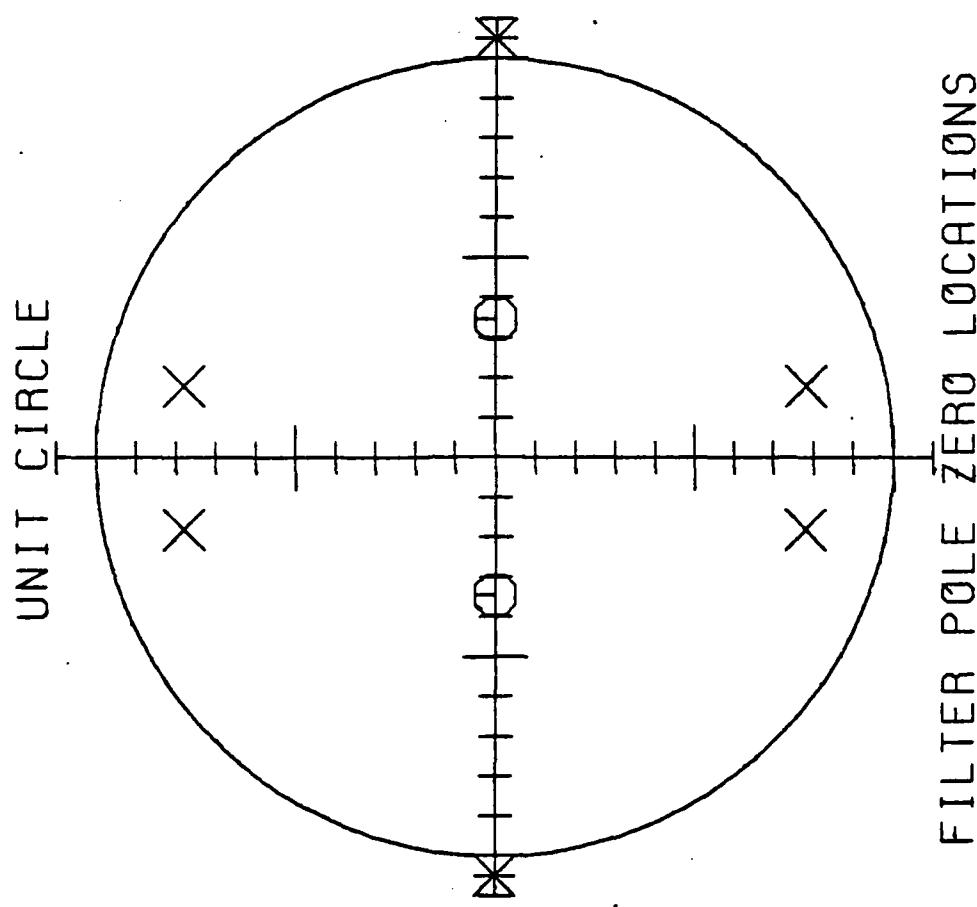


Figure 7-2b Plot Of Pole Zero Locations For A Fourth-Order Band-Pass Filter

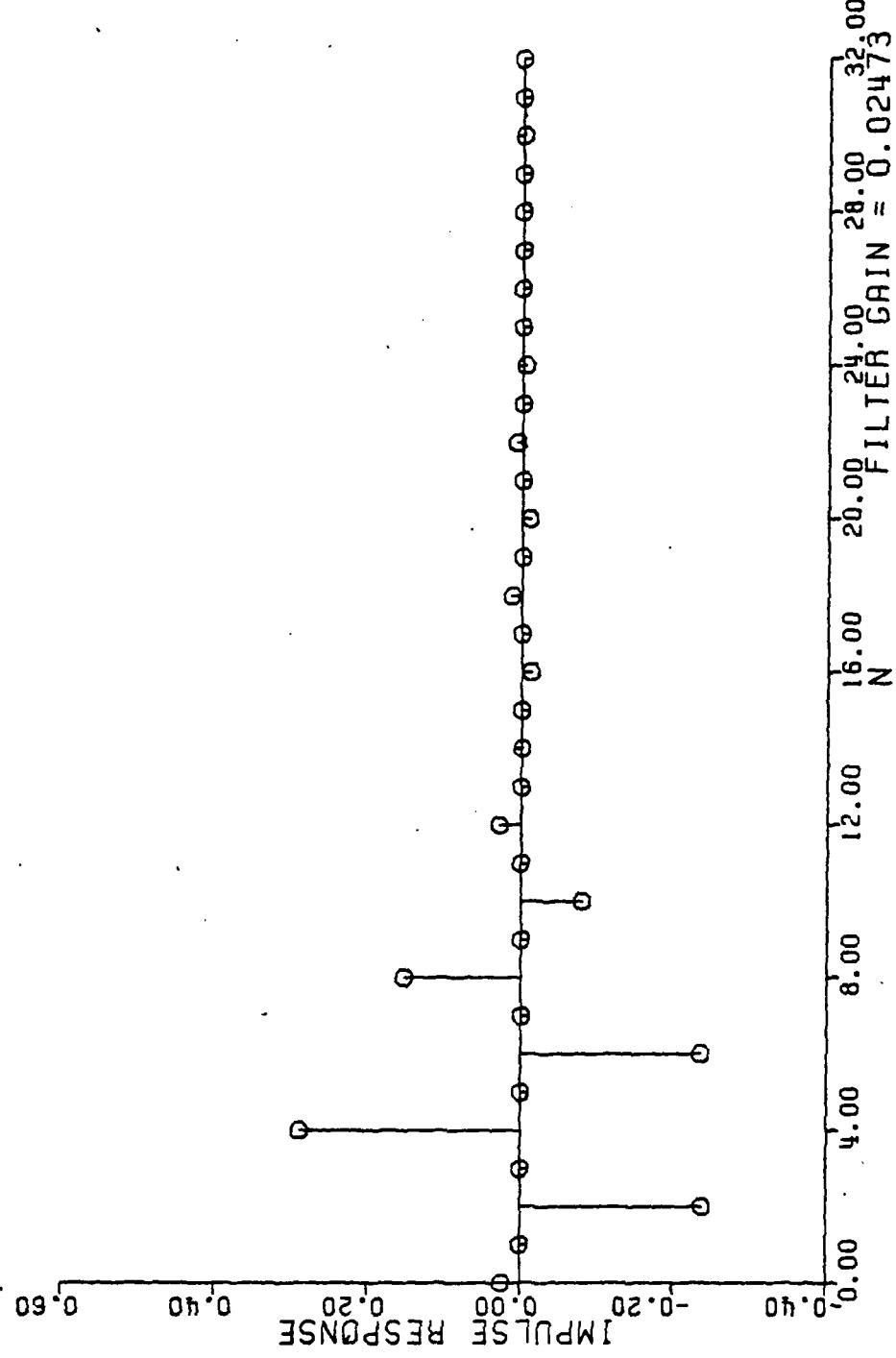


Figure 7-2c Unit Sample Response For A Fourth-Order Band-Pass Filter

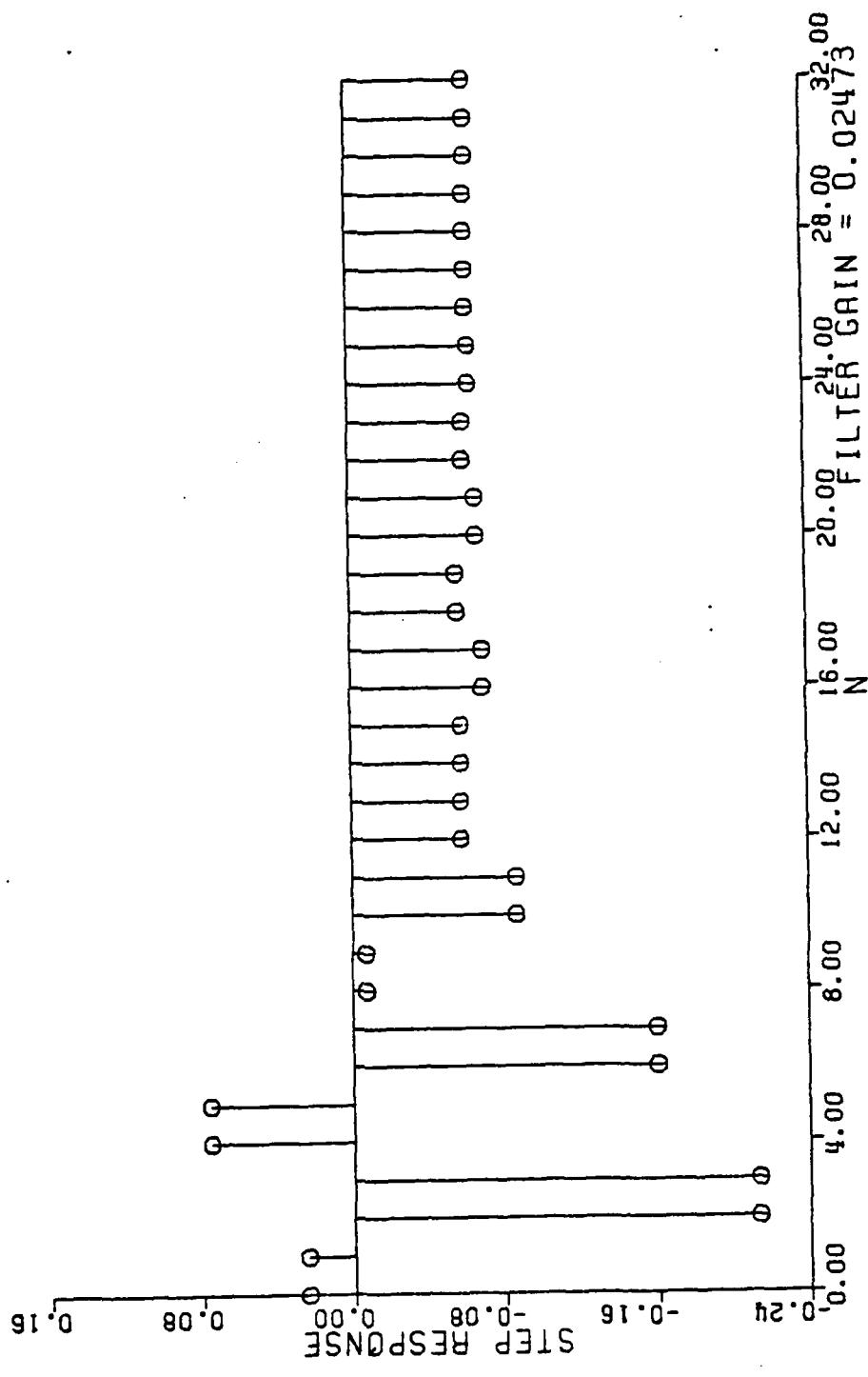


Figure 7-2d Unit Step Response For A Fourth-Order Band-Pass Filter

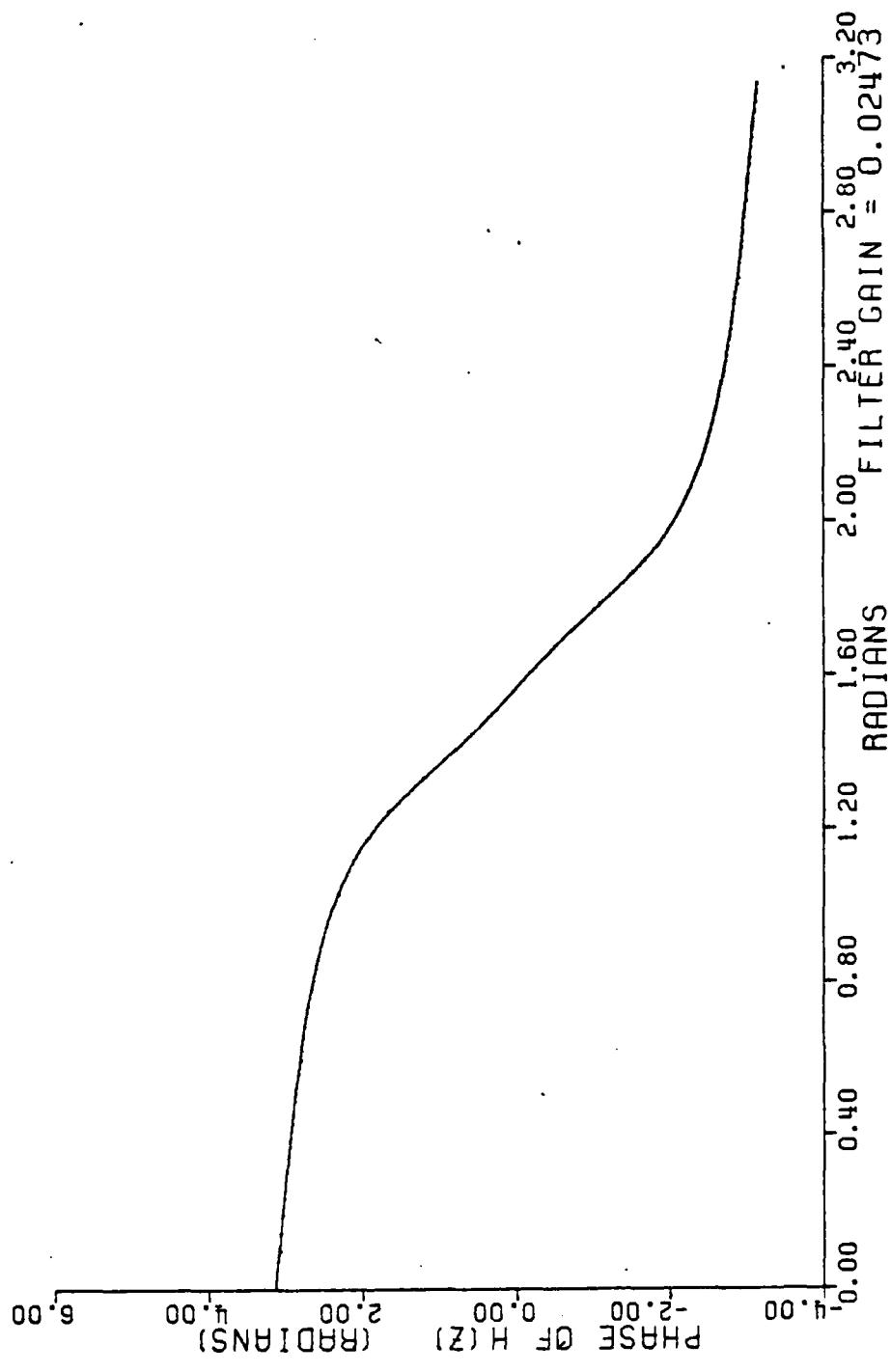


Figure 7-2e Phase Response For A Fourth-Order Band-Pass Filter

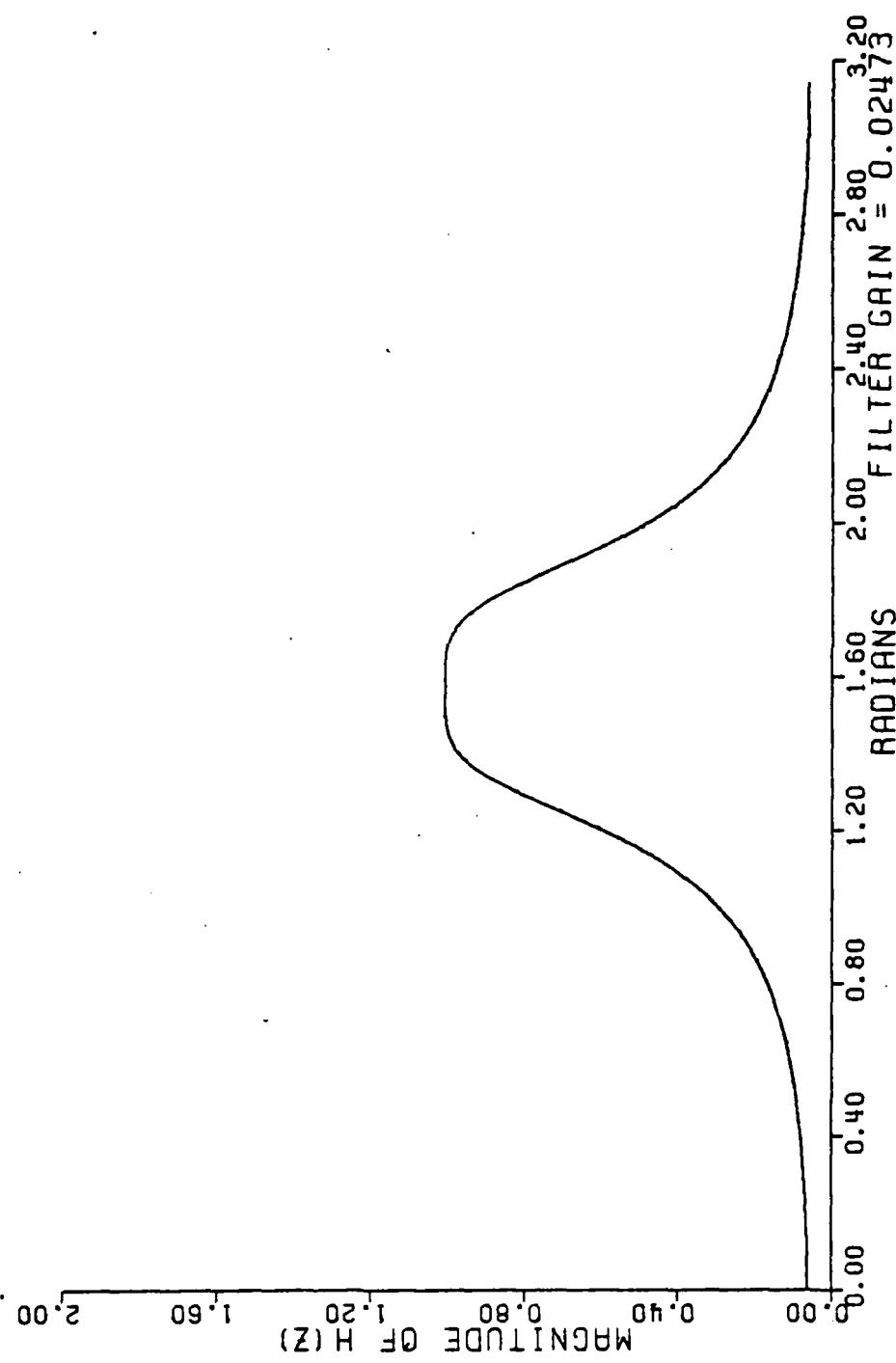


Figure 7-2f Magnitude Of  $H(z)$  For a Fourth-Order Band-Pass Filter

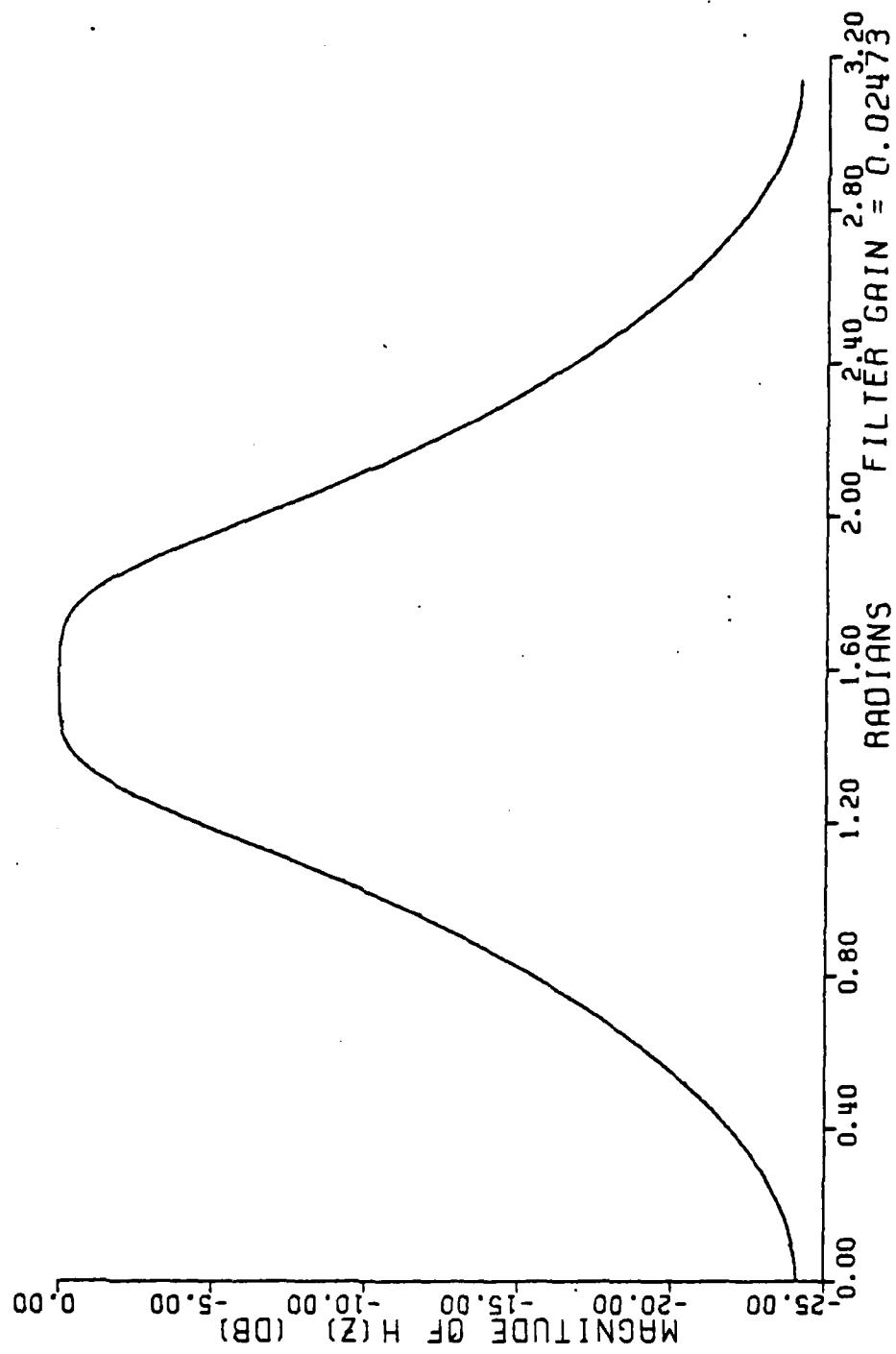


Figure 7-2g Magnitude Of  $H(z)$  For A Fourth-Order Band-Pass Filter

```

Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z
REAL           INAGINARY          RHO             THETA
Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z Z
Z +/ - 0.9211732 Z +/ - 0.9211732 Z +/ - 1.5707951 Z C2
Z 0.0          Z +/ - 1.0855713 Z 1.0855713 Z +/ - 1.5707951 Z C2
Z 0.0          Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z * * * * *       Z * * * * *       Z * * * * *
Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P Z P
P -0.1852023 P +/ - 0.7716743 P 0.7935876 P +/ - 1.3352489 P CP
P -0.1852023 P +/ - 0.7716743 P 0.7935876 P +/ - 1.8063431 P CP
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *
P * * * * * P * * * * * P * * * * * P * * * * *

```

NUMBER OF REAL ZEROS: 0  
NUMBER OF COMPLEX ZERO PAIRS: 2  
NUMBER OF REAL POLES: 0  
NUMBER OF COMPLEX POLE PAIRS: 2  
FILTER GAIN: 0.62447256

Figure 7-3a Pole Zero Locations For A Fourth-Order Notch Filter

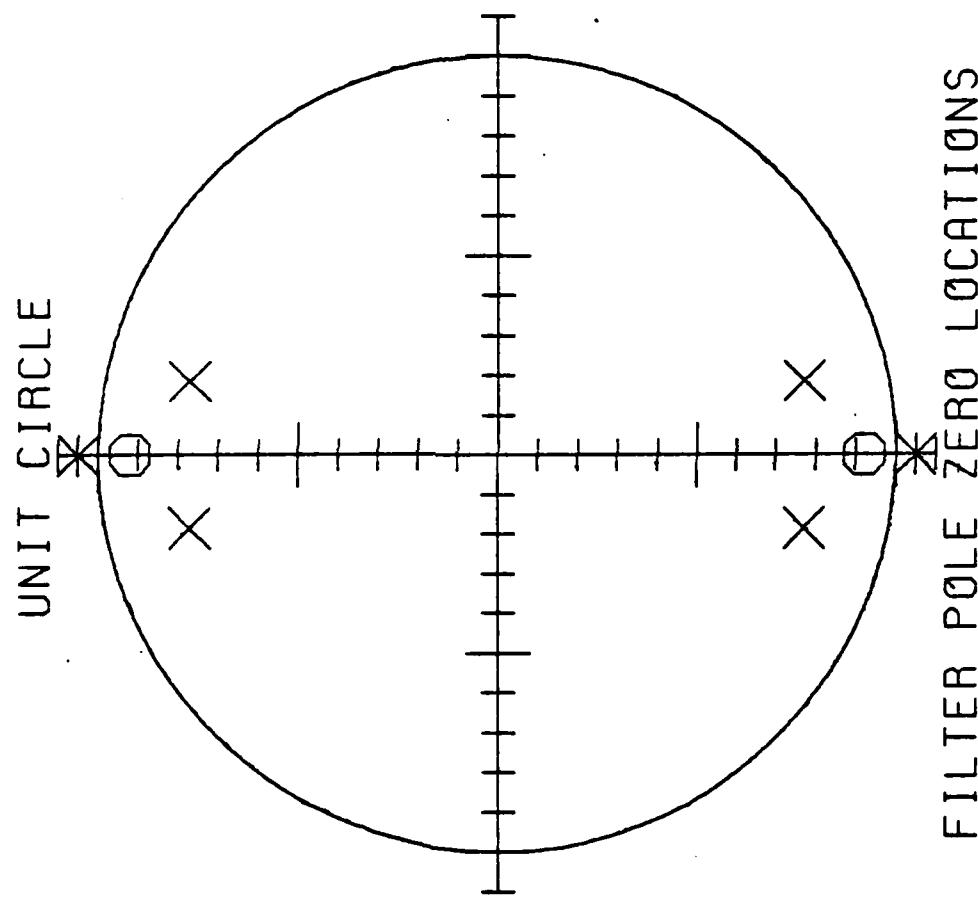


Figure 7-3b Plot Of Pole Zero Locations For A Fourth-Order Notch Filter

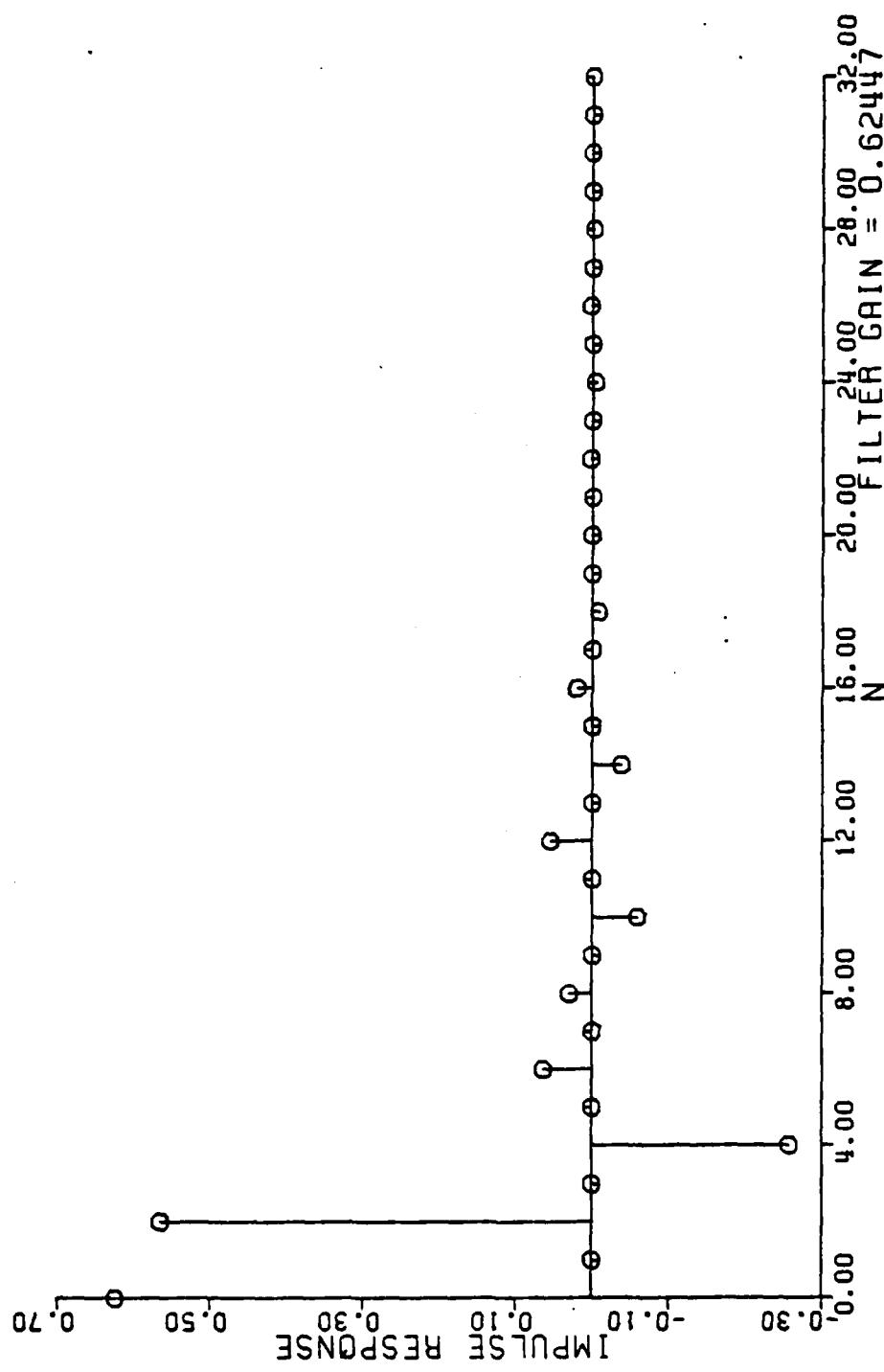


Figure 7-3c Unit Sample Response For A Fourth-Order Notch Filter

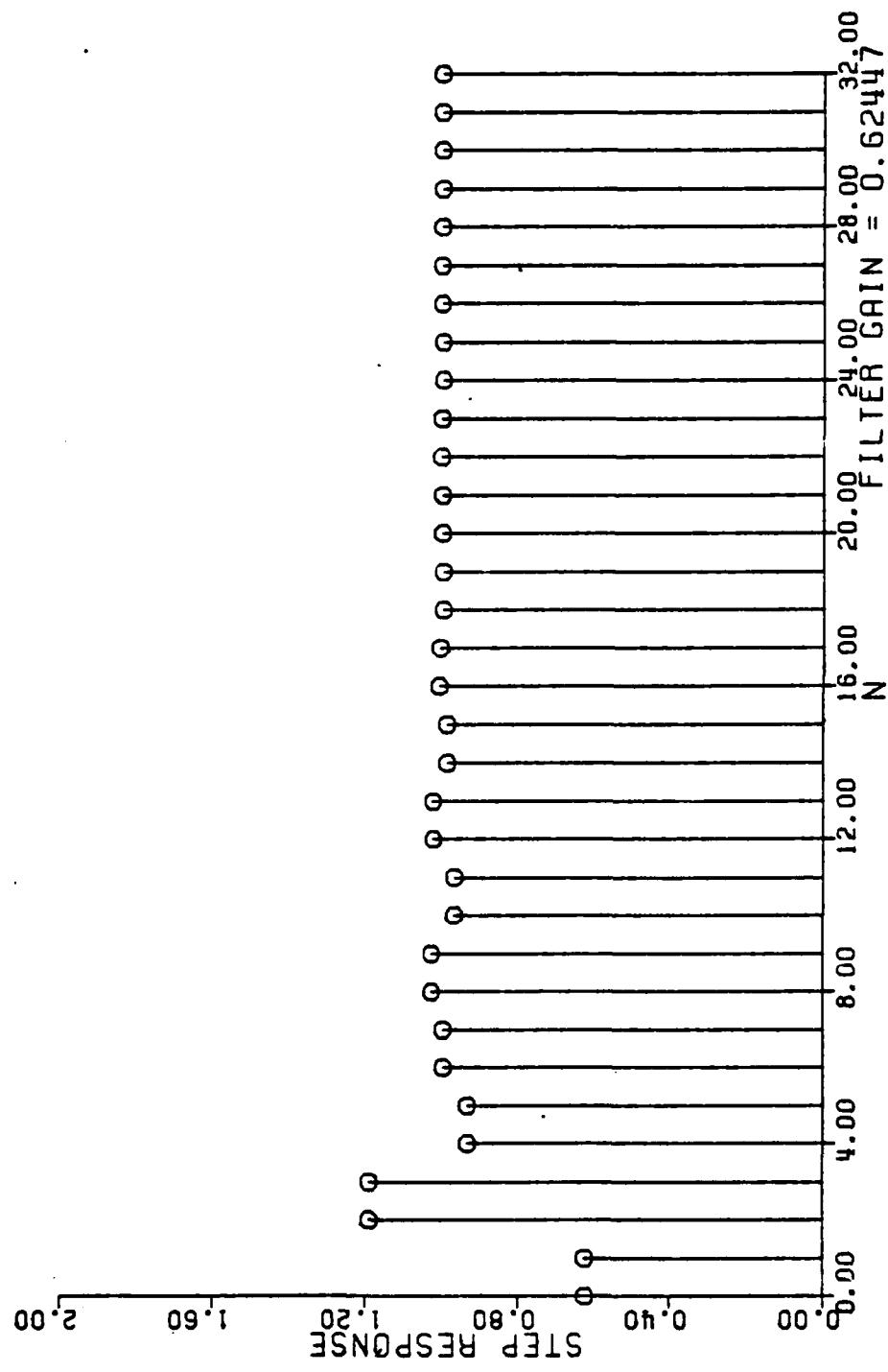


Figure 7-3d Unit Step Response For A Fourth-Order Notch Filter

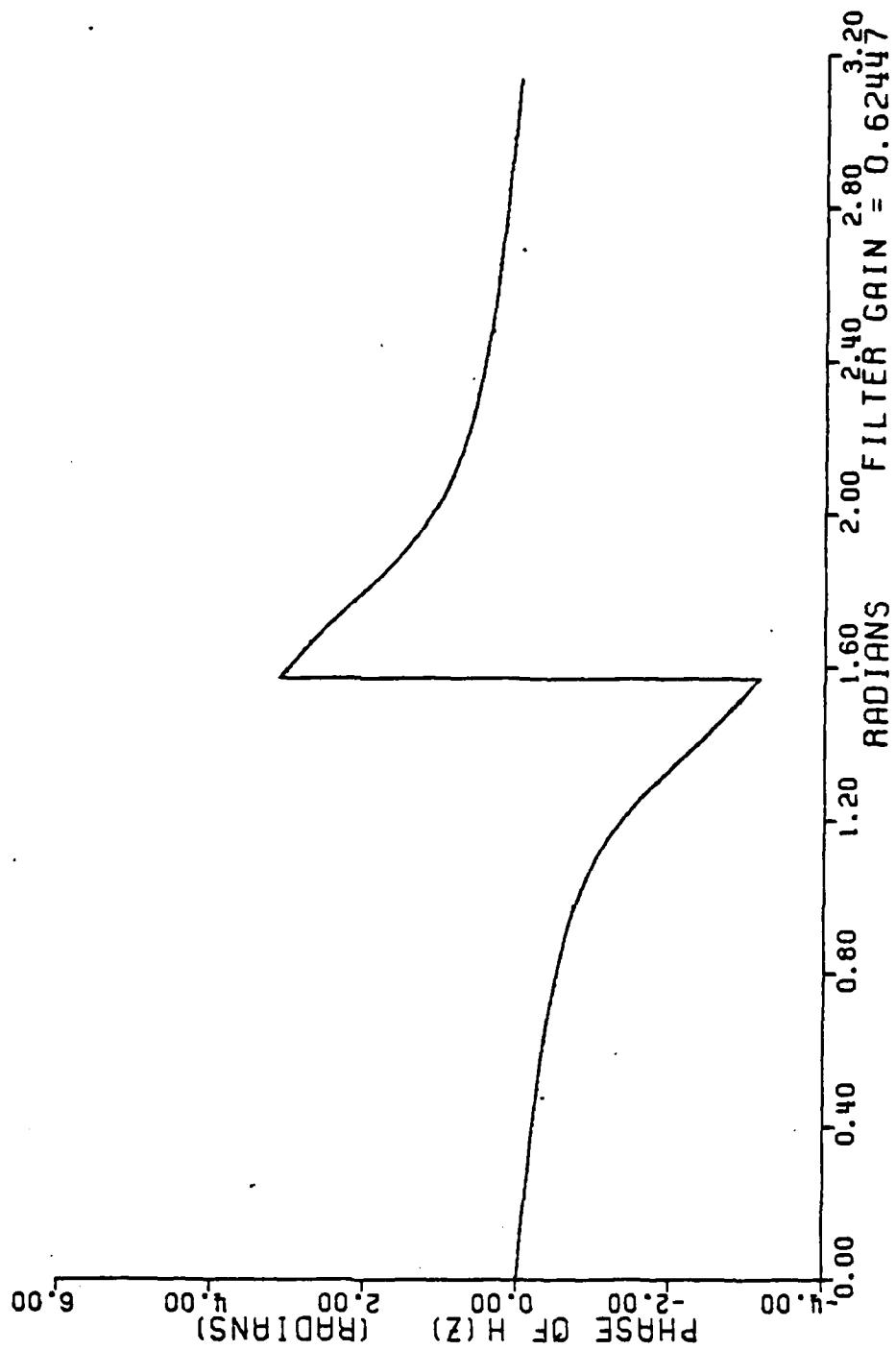


Figure 7-3e Phase Response For a Fourth-Order Notch Filter

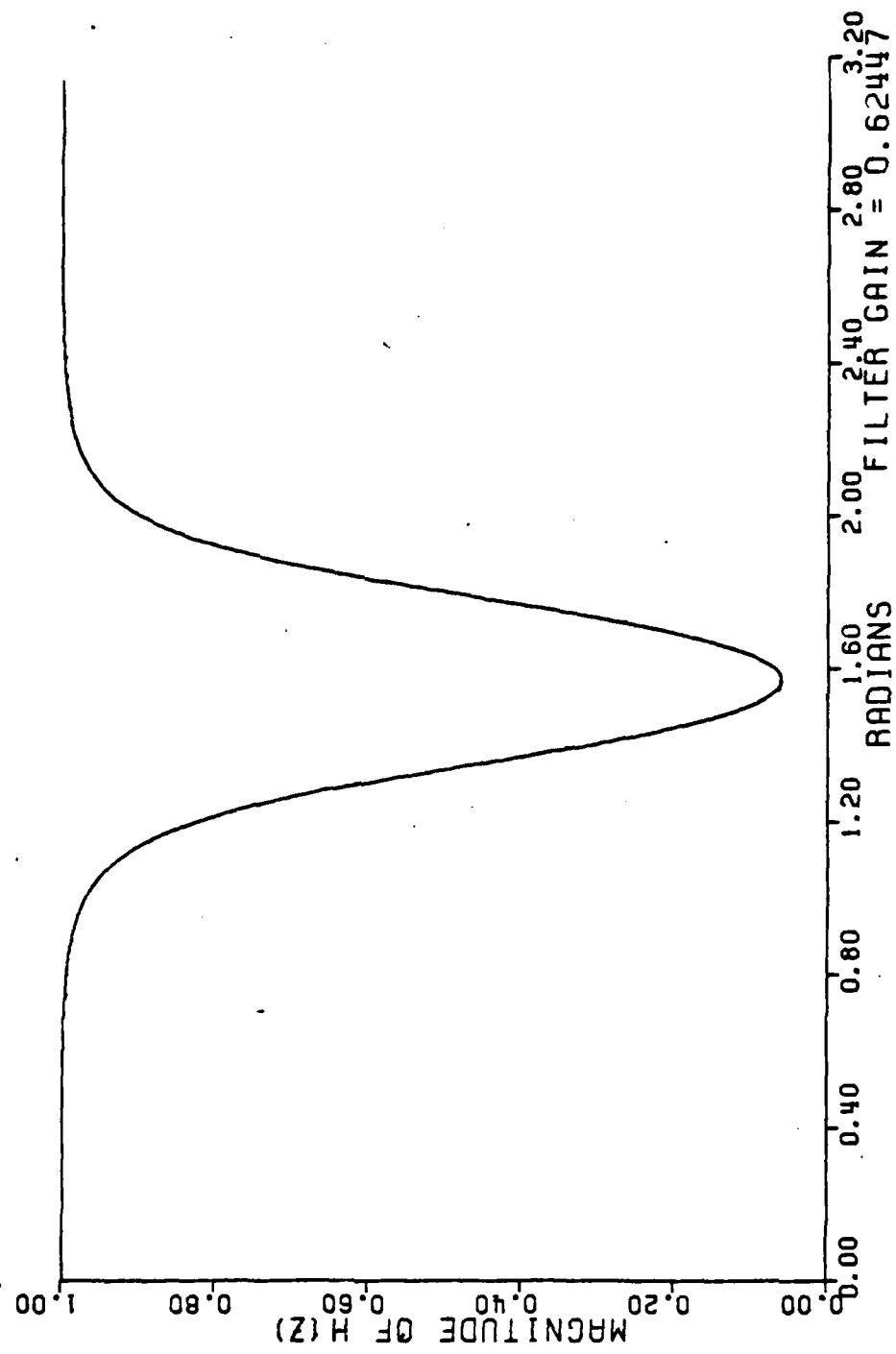


Figure 7-3f Magnitude Of  $H(z)$  For A Fourth-Order Notch Filter

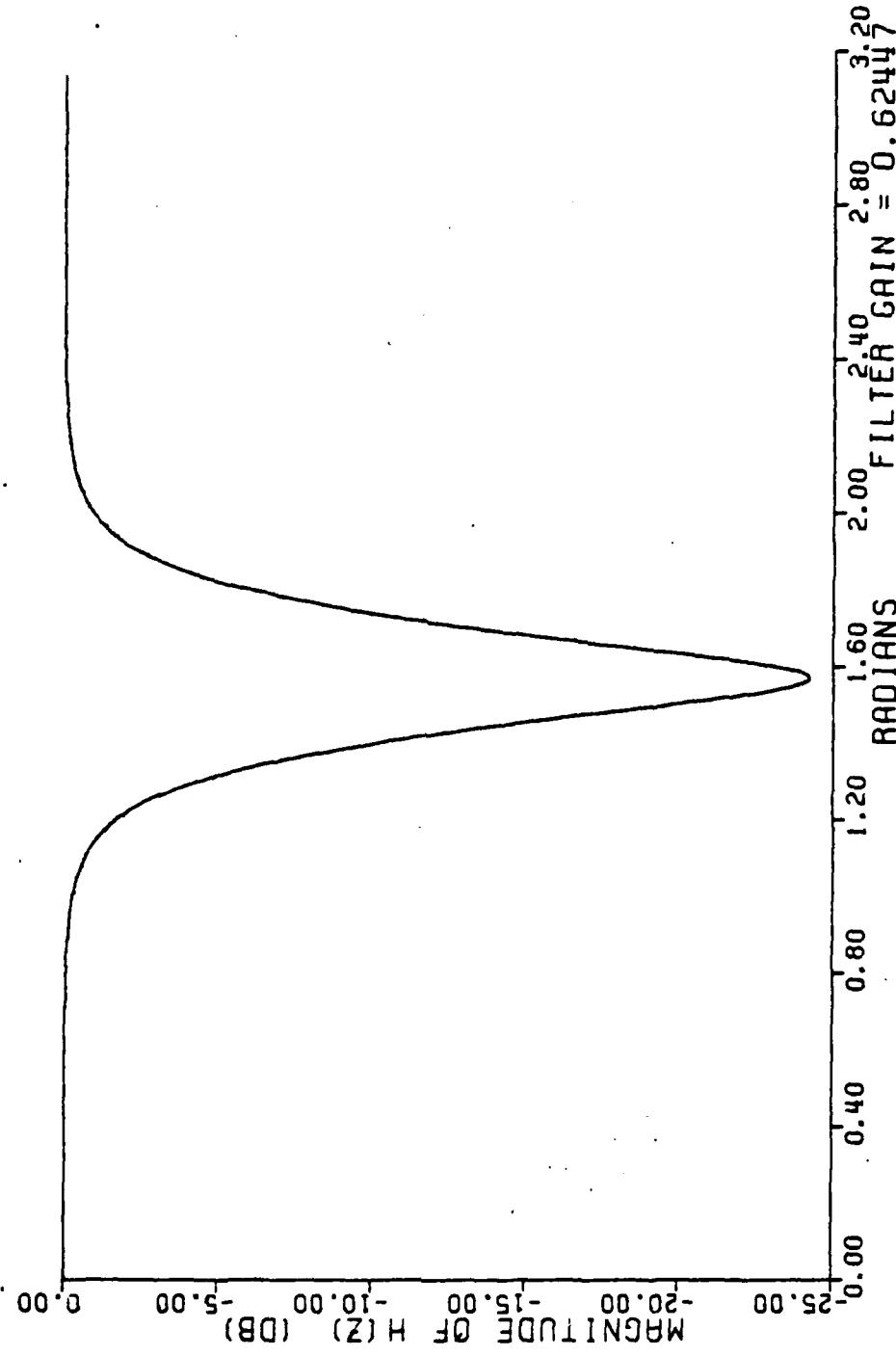


Figure 7-3g Magnitude In Decibels For A Fourth-Order Notch Filter

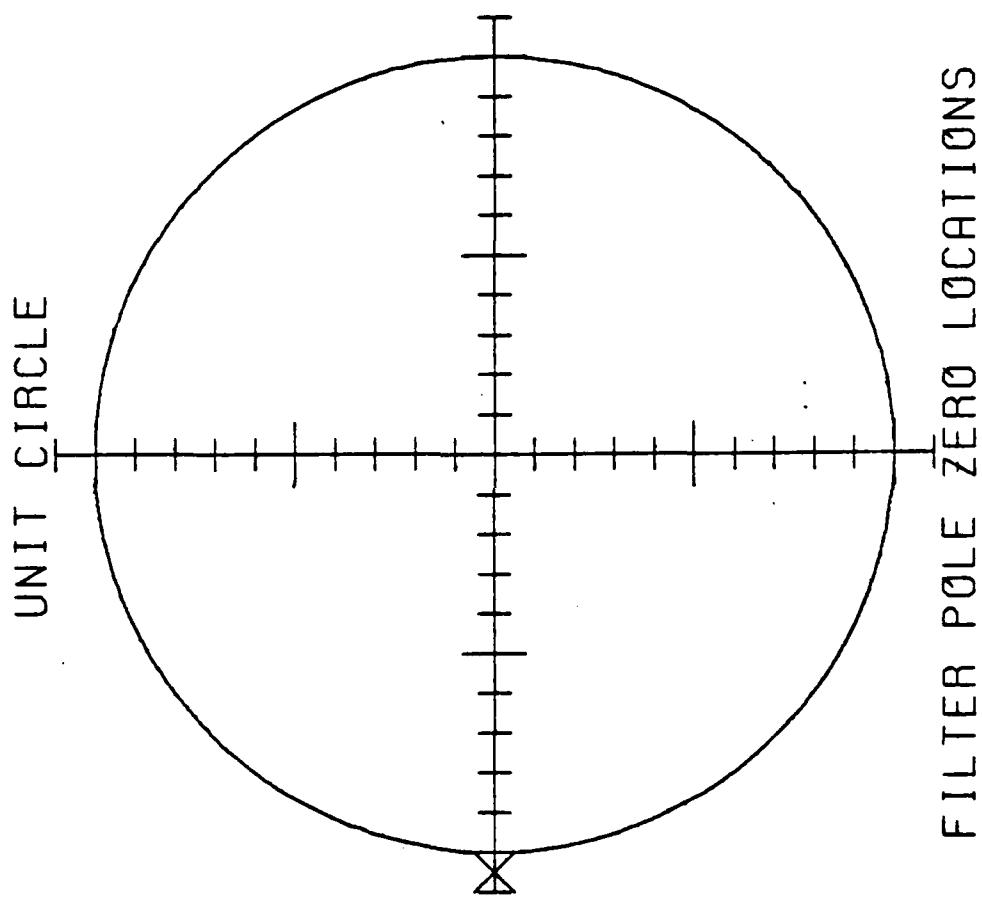


Figure 7-4a Example Of A Single Real Pole Outside The Unit Circle At (-1.05)

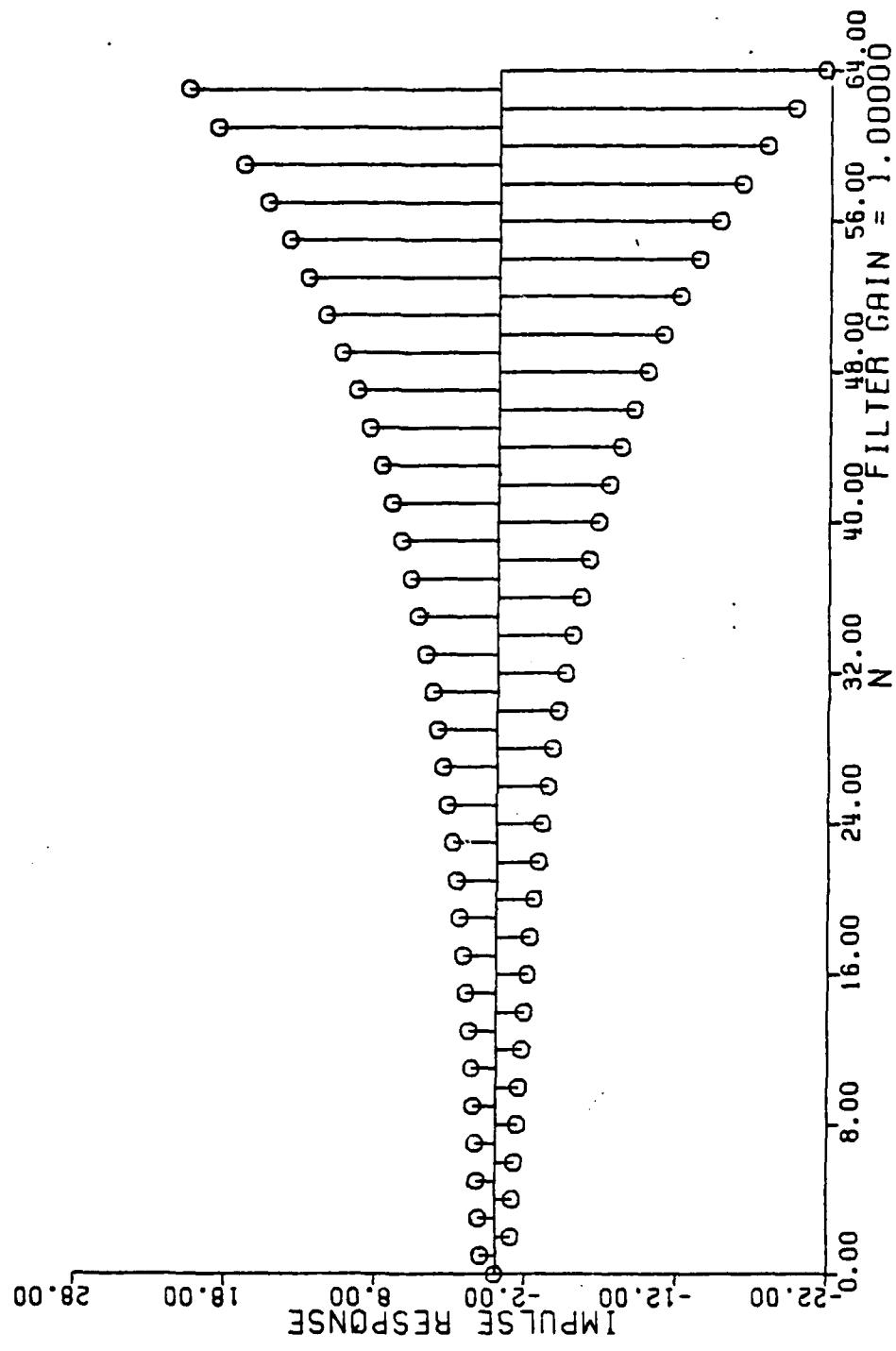


Figure 7-4b Unit Sample Response For A Single Real Pole At (-1.05)

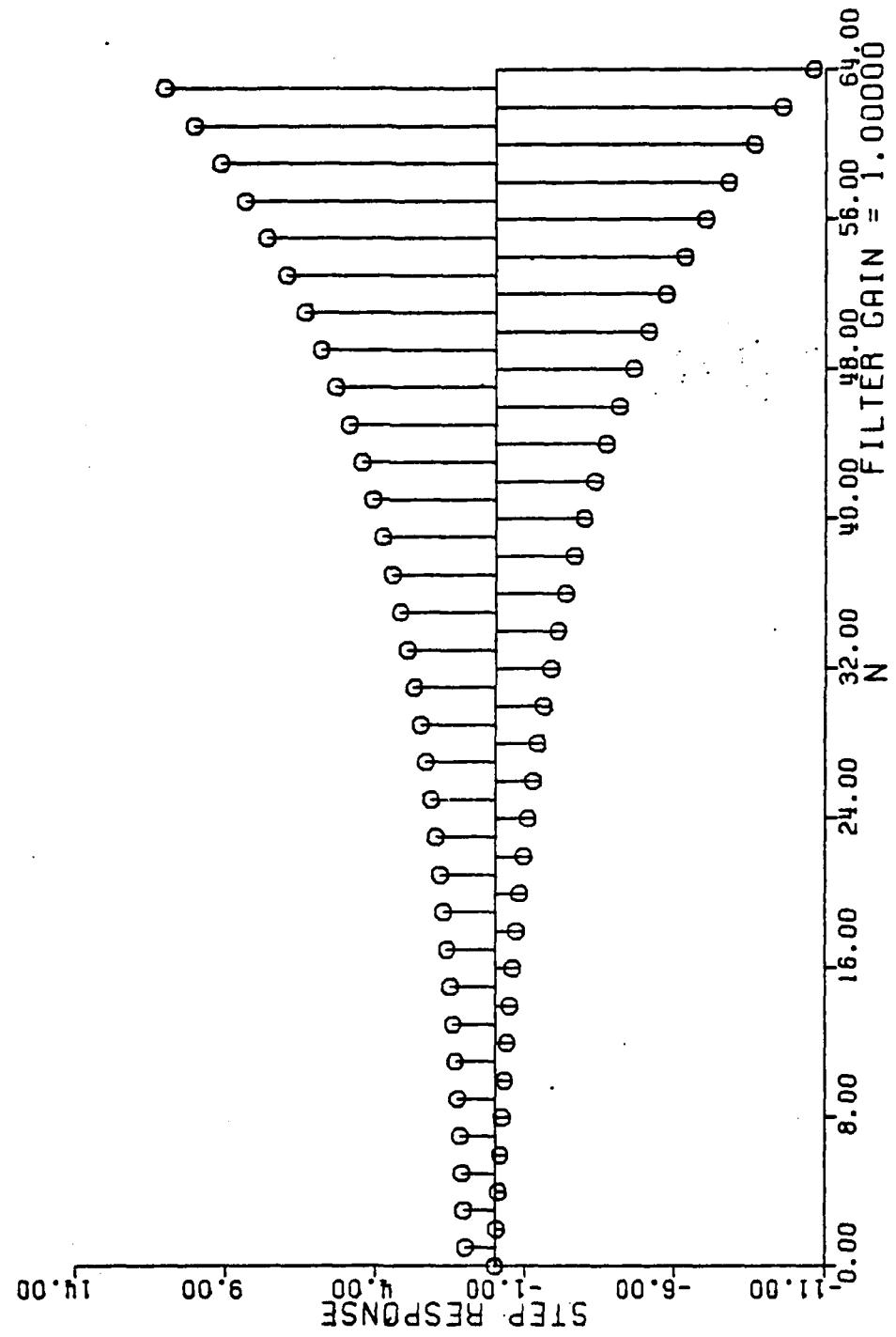


Figure 7-4c Unit Step Response For A Single Real Pole At (-1.05)

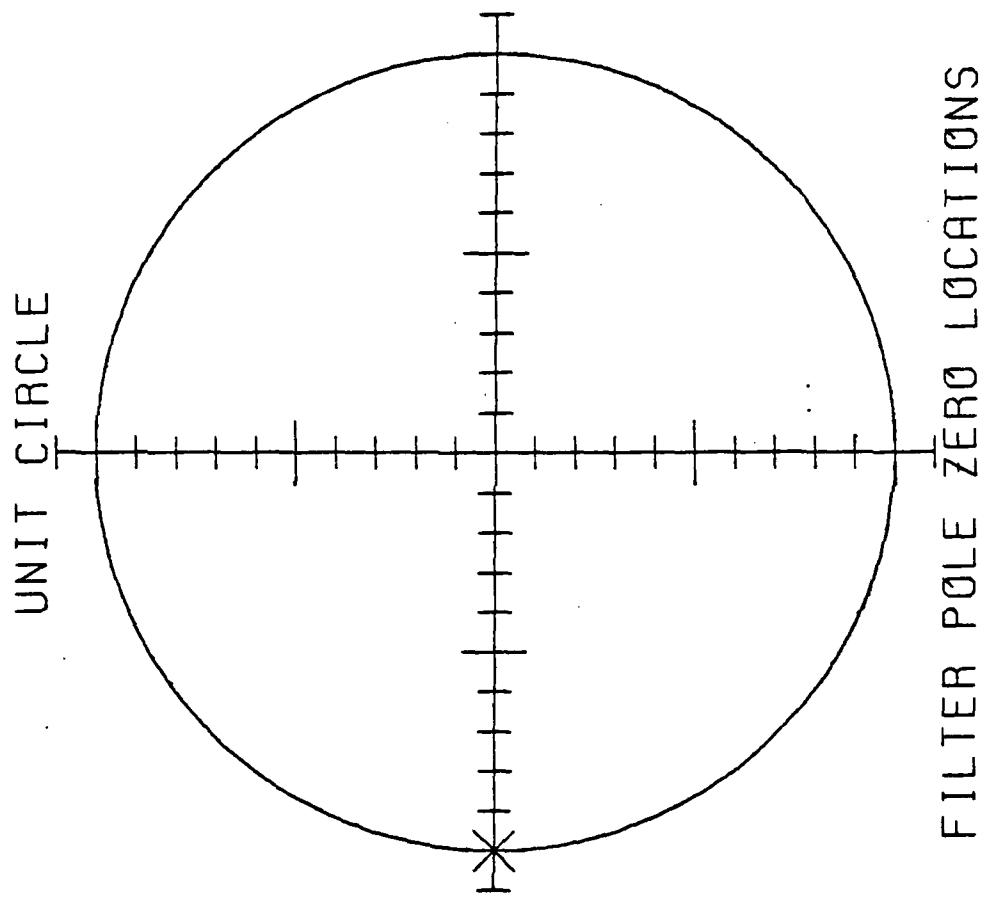


Figure 7-5a Example Of A Single Real Pole On The Unit Circle At (-1.0)

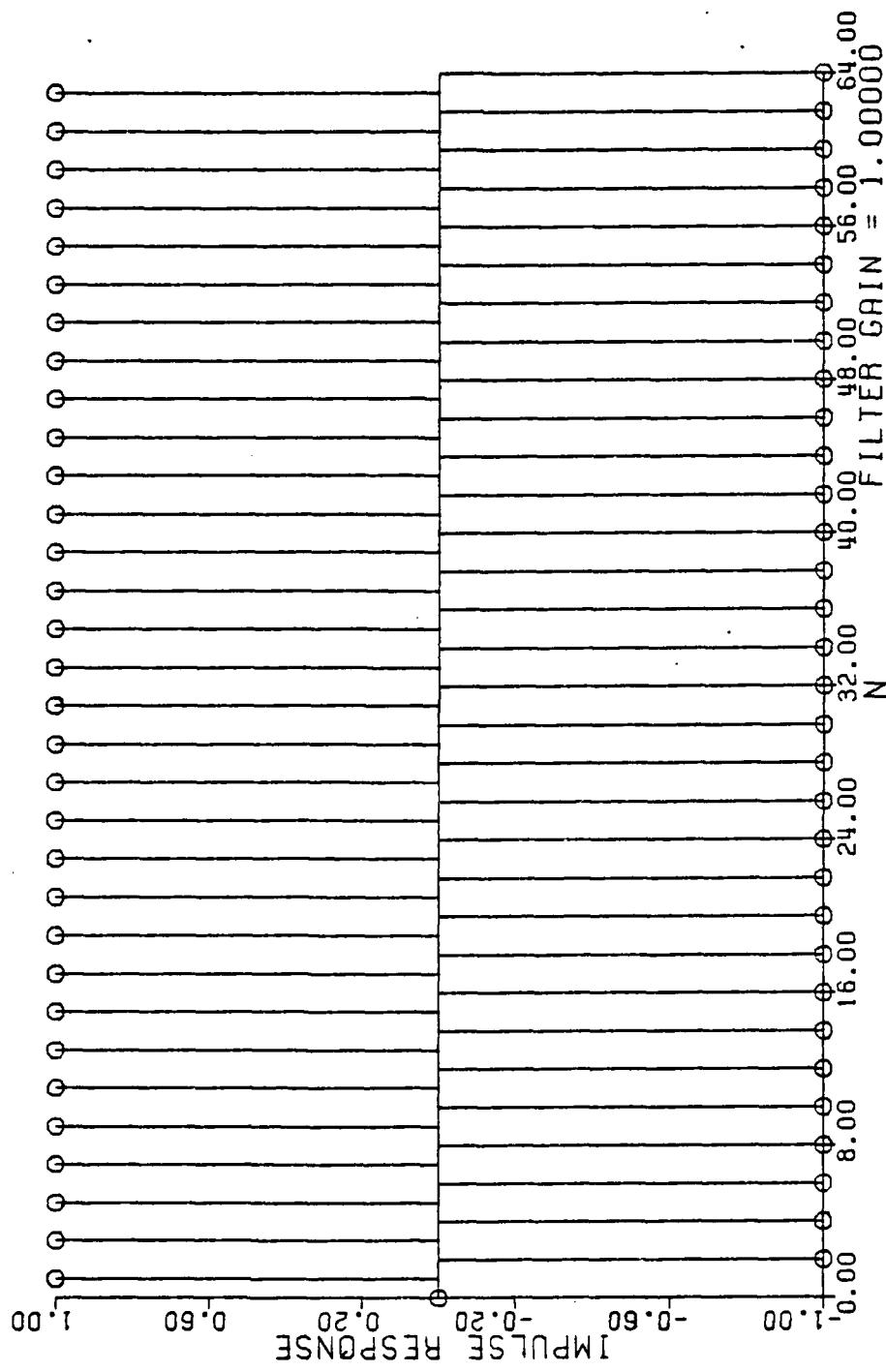


Figure 7-5b Unit Sample Response For A Single Real Pole At (-1.0)

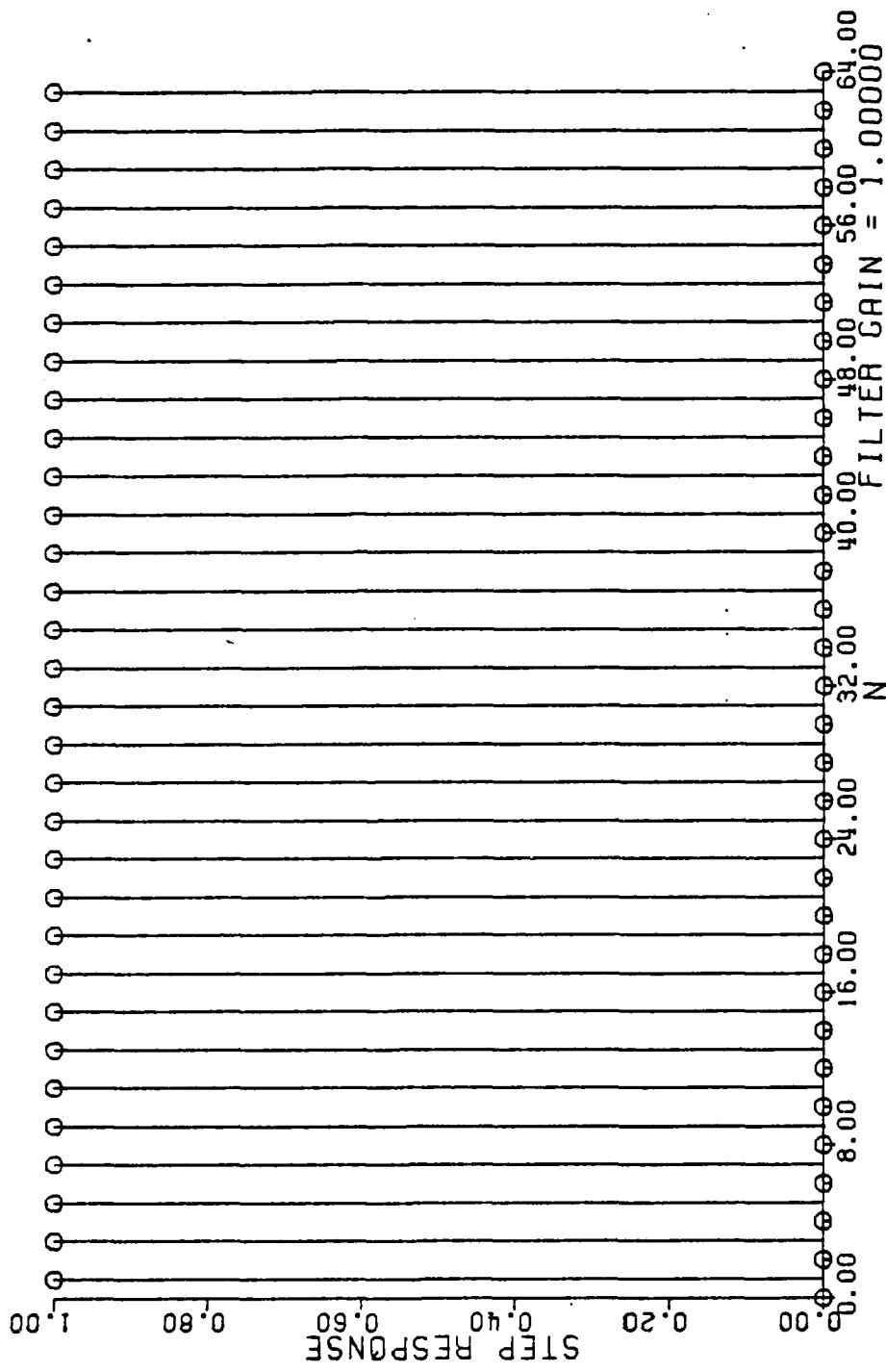


Figure 7-5c Unit Step Response For A Single Real Pole At (-1.0)

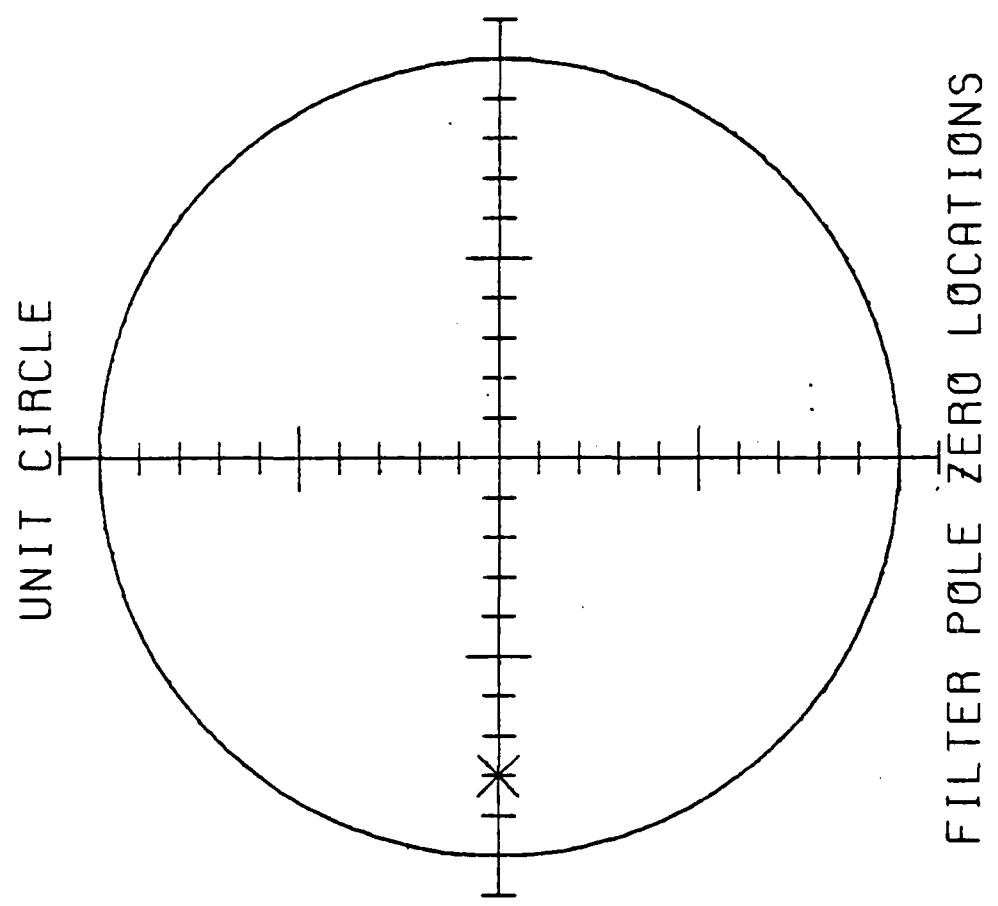


Figure 7-6a Example Of A Single Real Pole At (-0.8)

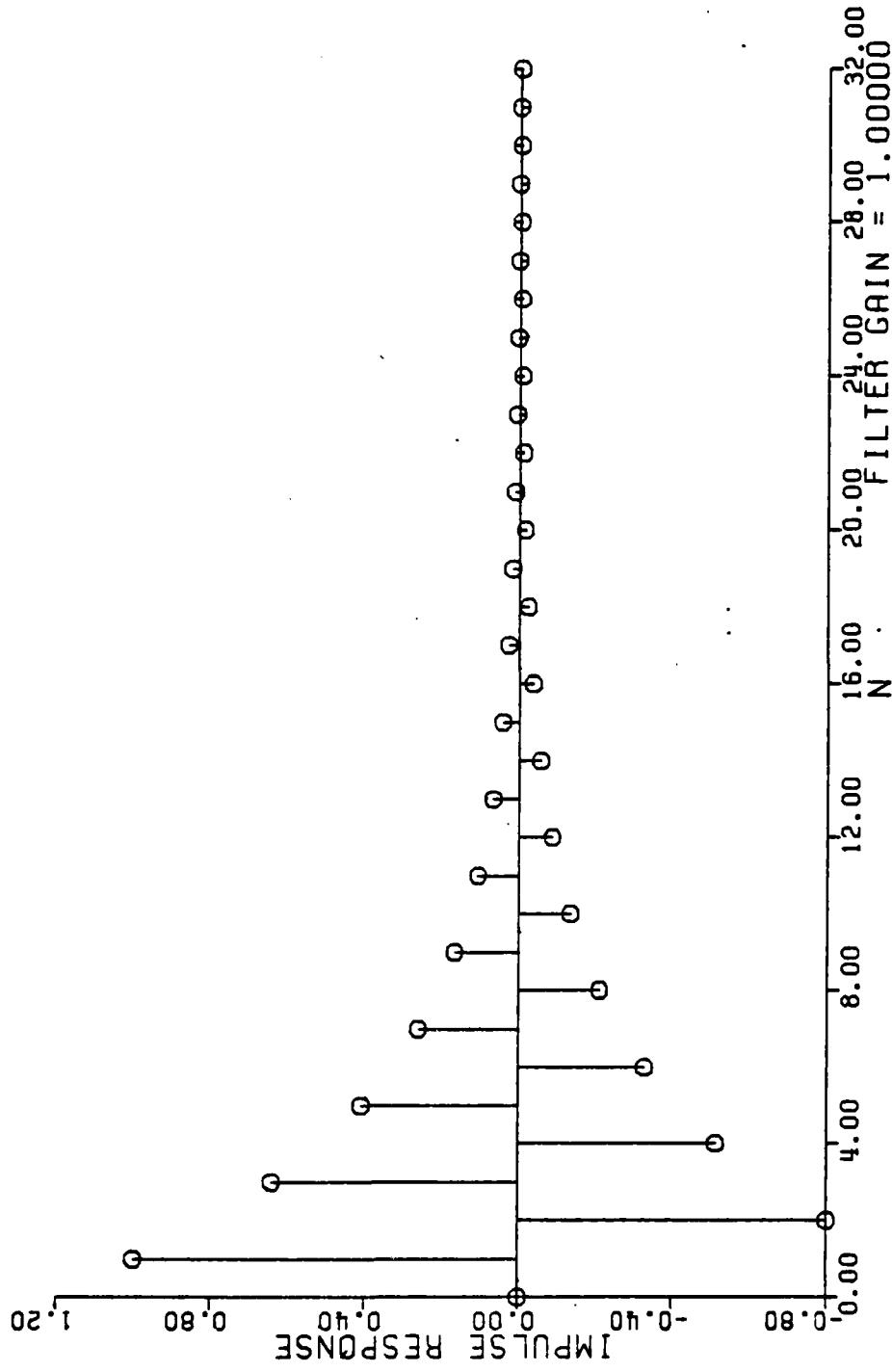


Figure 7-6b Unit Sample Response For A Single Real Pole at  $(-1.0)$

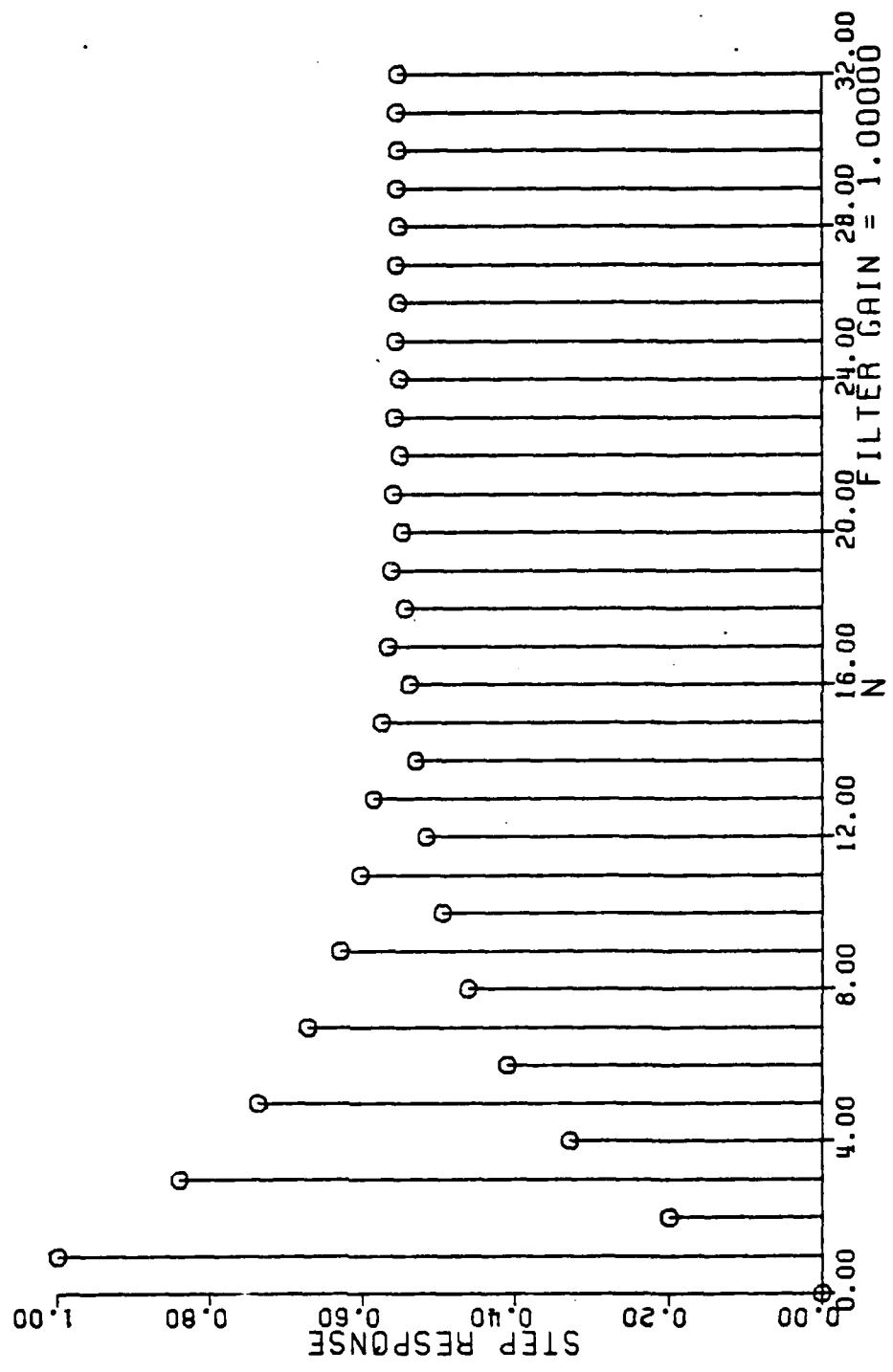


Figure 7-6c Unit Step Response For A Single Real Pole At (-0.8)

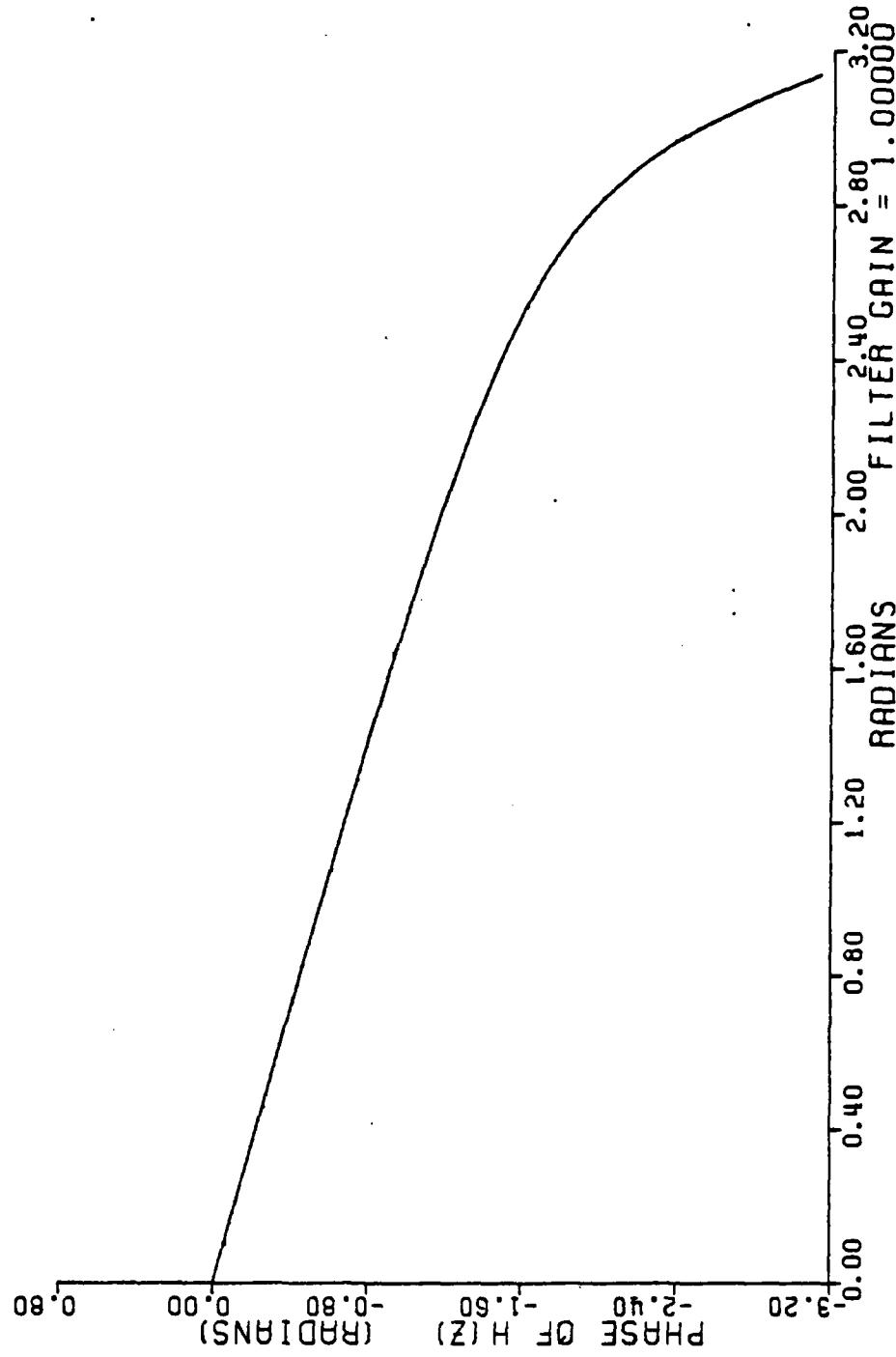


Figure 7-7d Phase Response For A Single Real Pole At (-0.8)

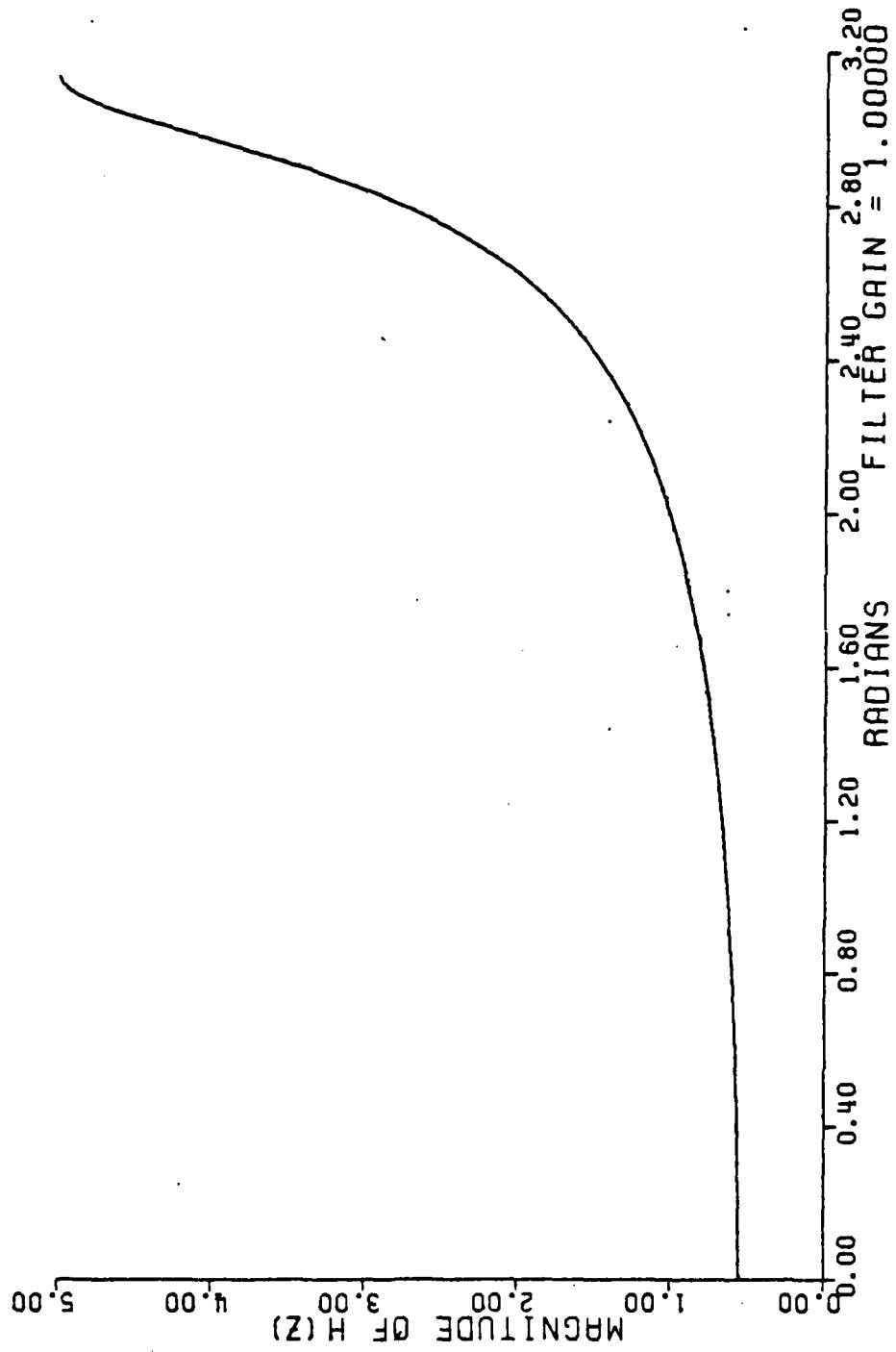


Figure 7-6e Magnitude Of  $H(z)$  For A Single Real Pole At (-0.8)

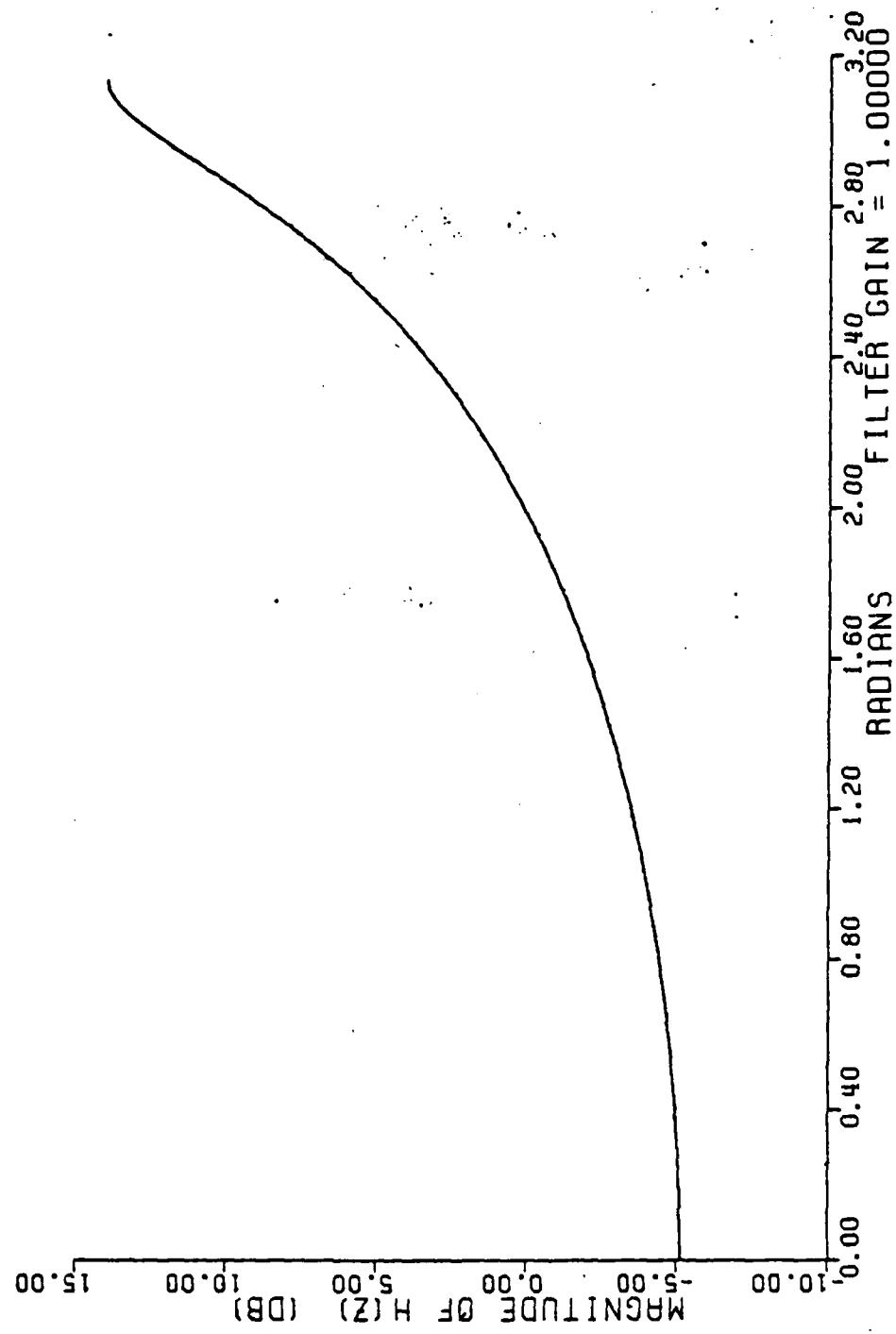


Figure 7-6f Magnitude Of  $H(z)$  In Decibels For a Single Real Pole at (-0.8)

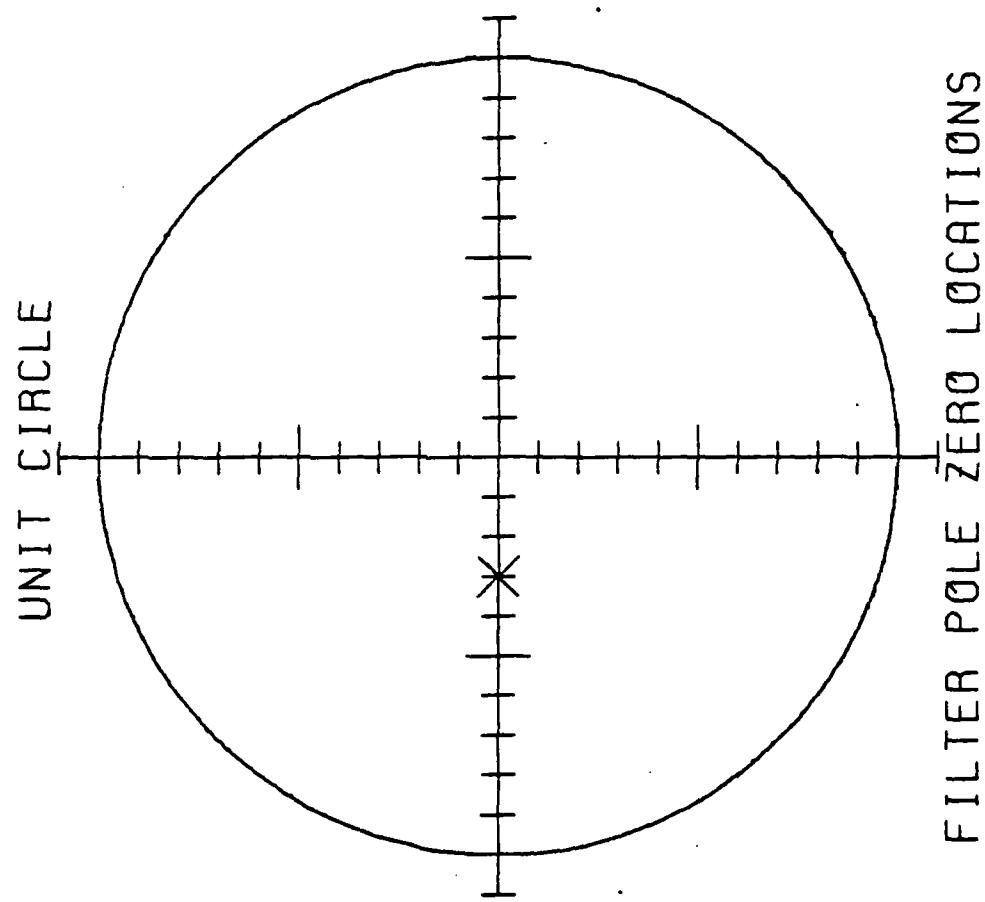


Figure 7-7a Example Of A Single Real Pole At (-0.3)

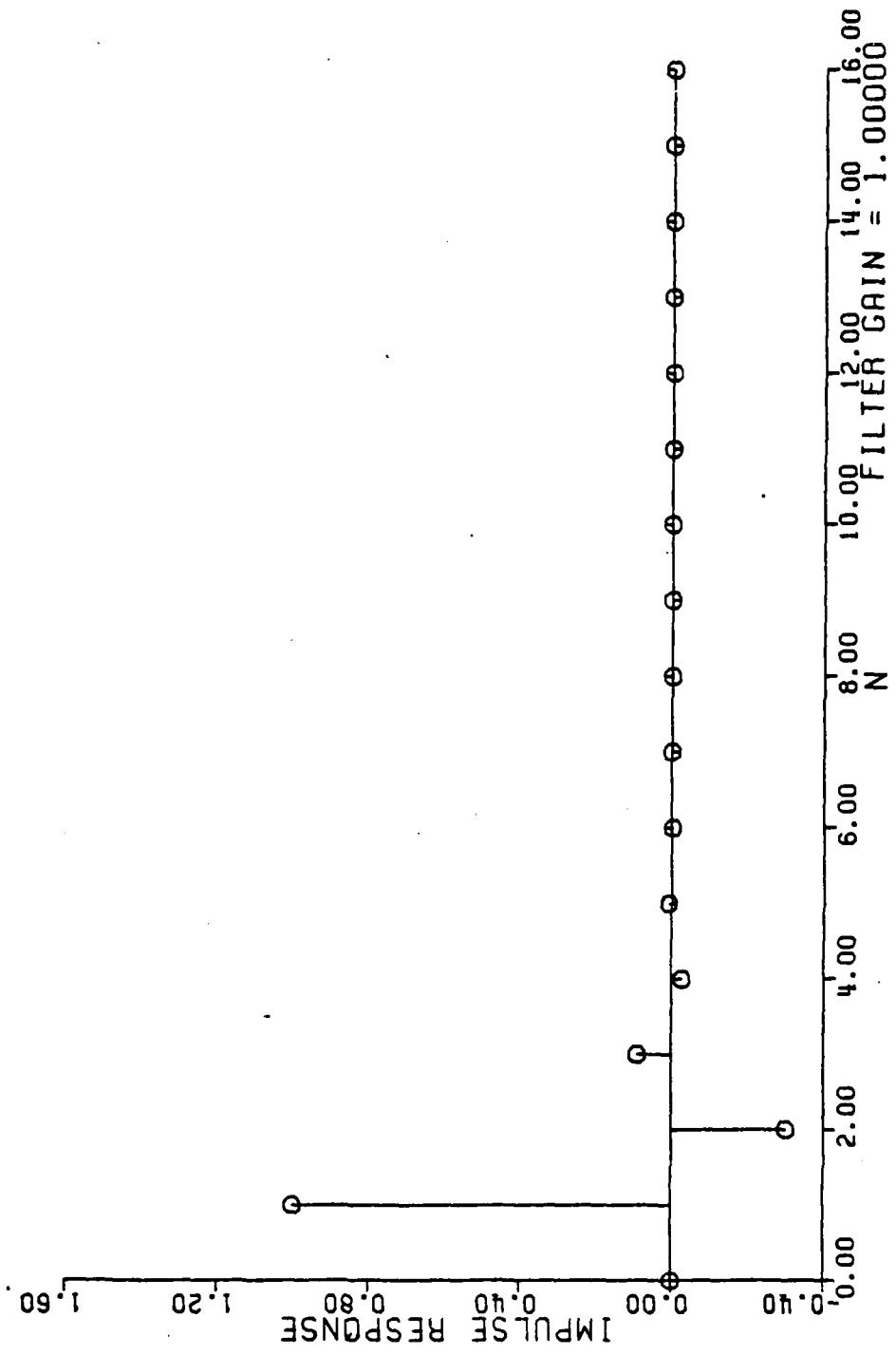


Figure 7-7b Unit Sample Response For A Single Real Pole At (-0.3)

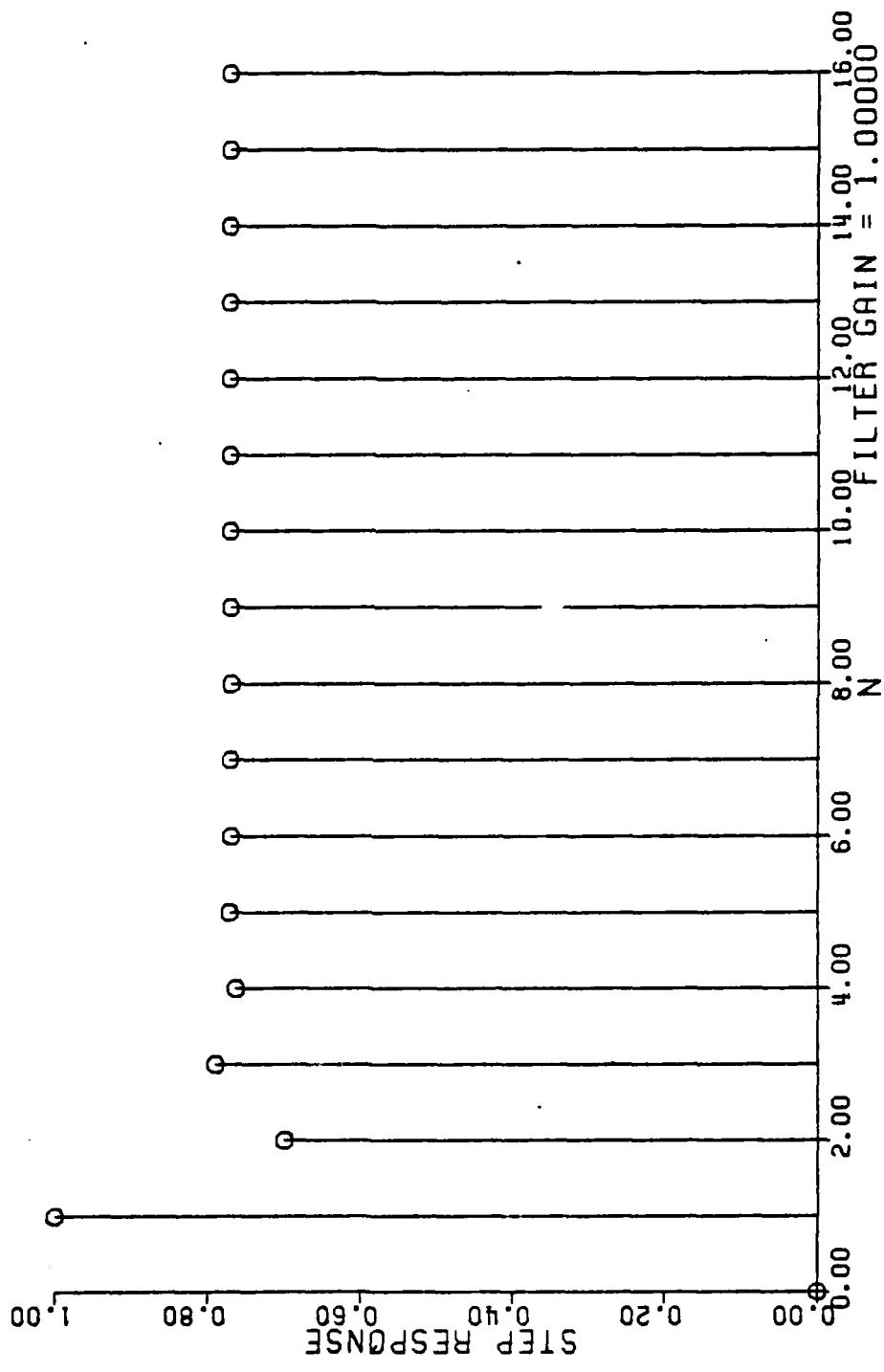


Figure 7-7c Unit Step Response For A Single Real Pole At (-0.3)

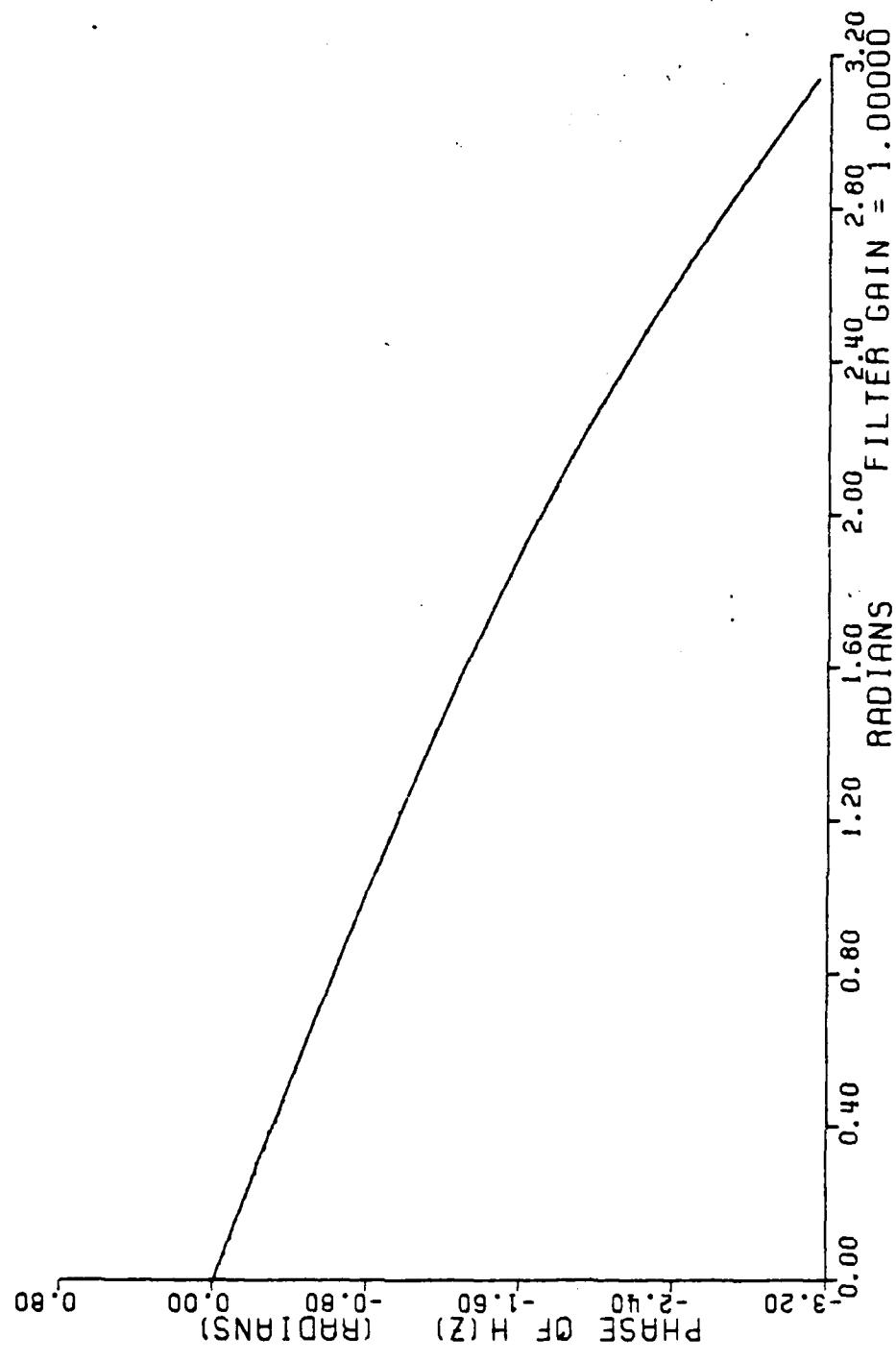


Figure 7-7d Phase Response For A Single Real Pole At  $(-0.3)$

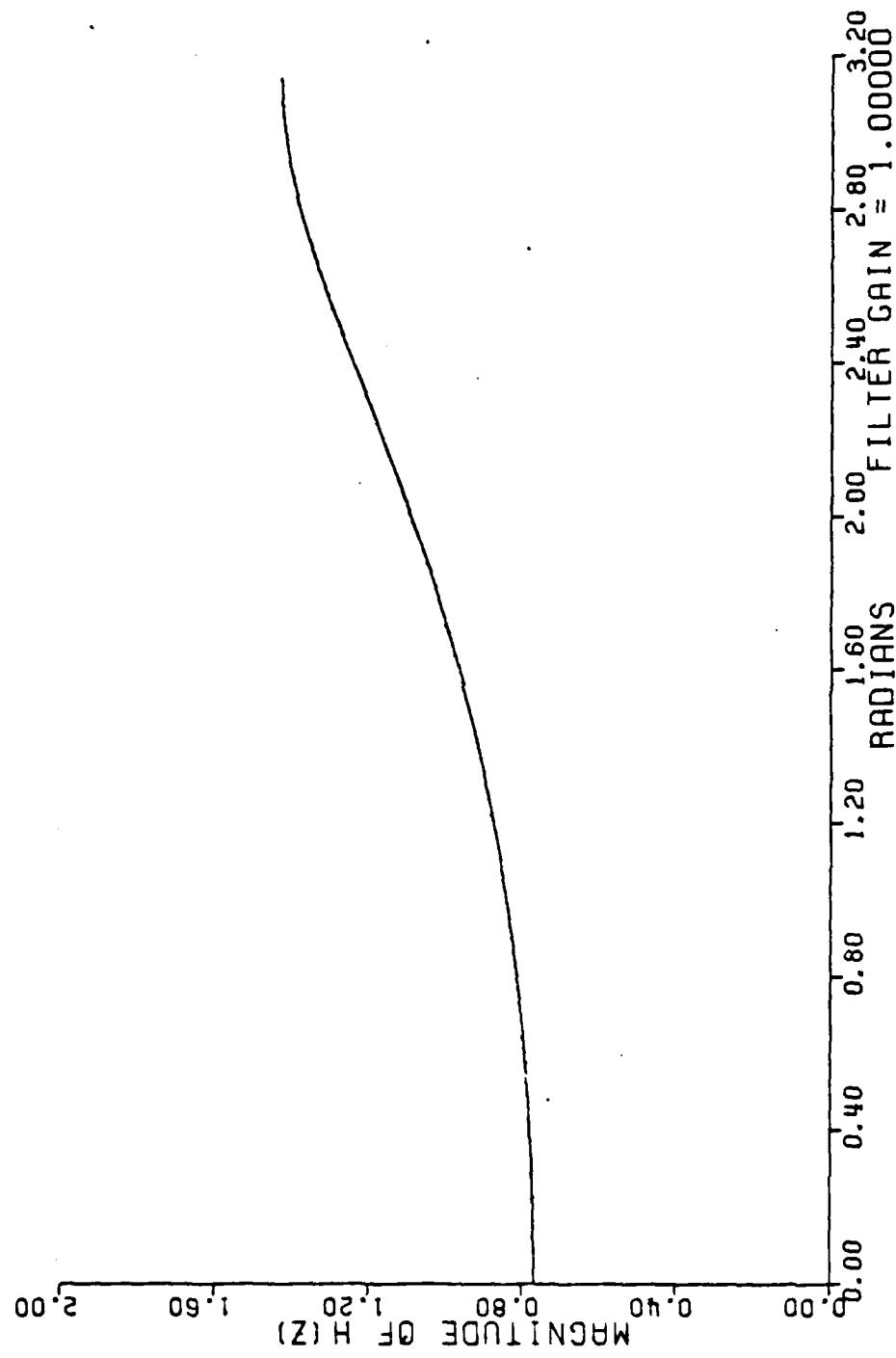


Figure 7-7e Magnitude Of  $H(z)$  For A Single Real Pole At (-0.3)

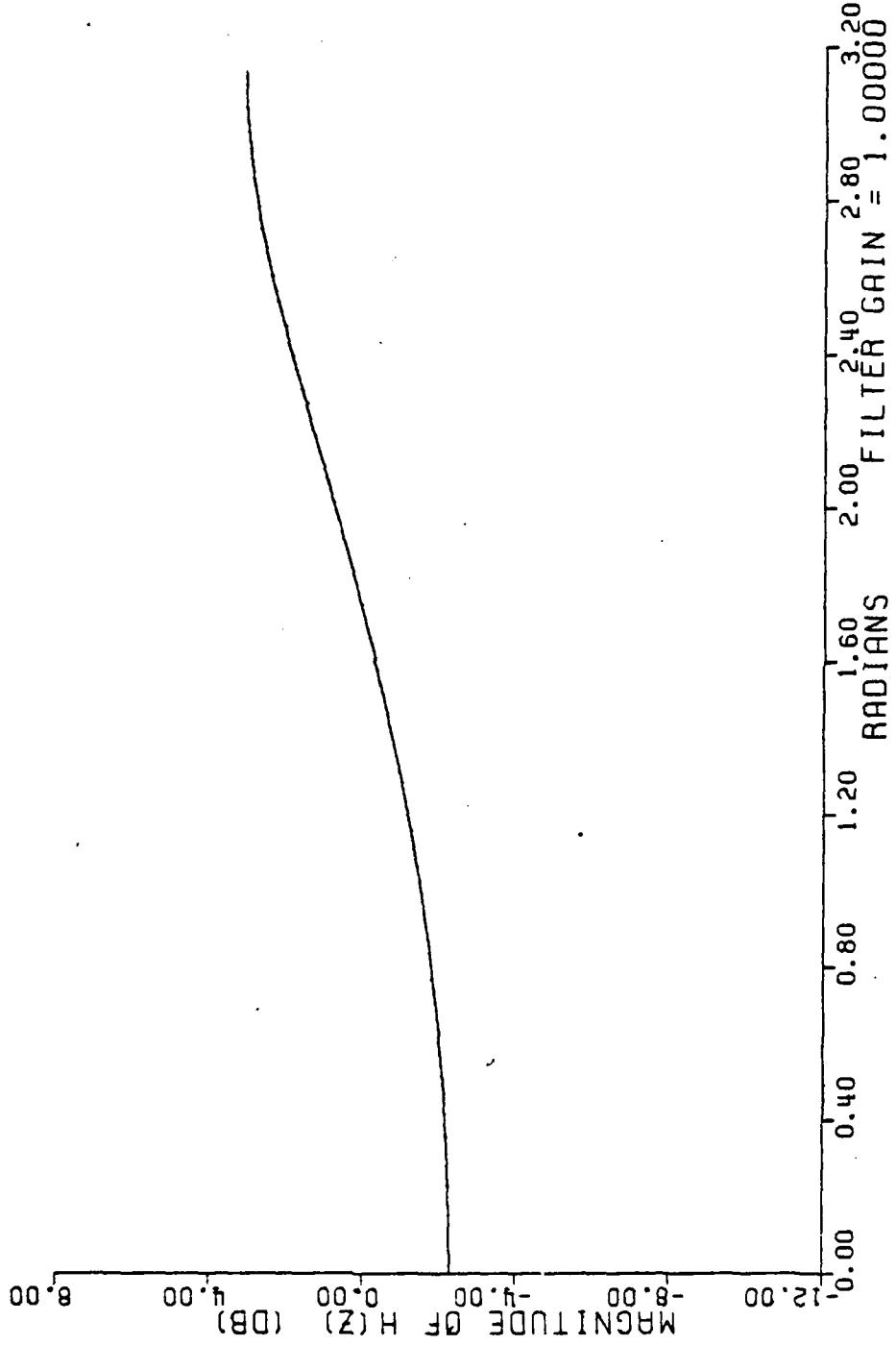


Figure 7-7f Magnitude Of  $H(z)$  For A Single Real Pole At (-0.3)

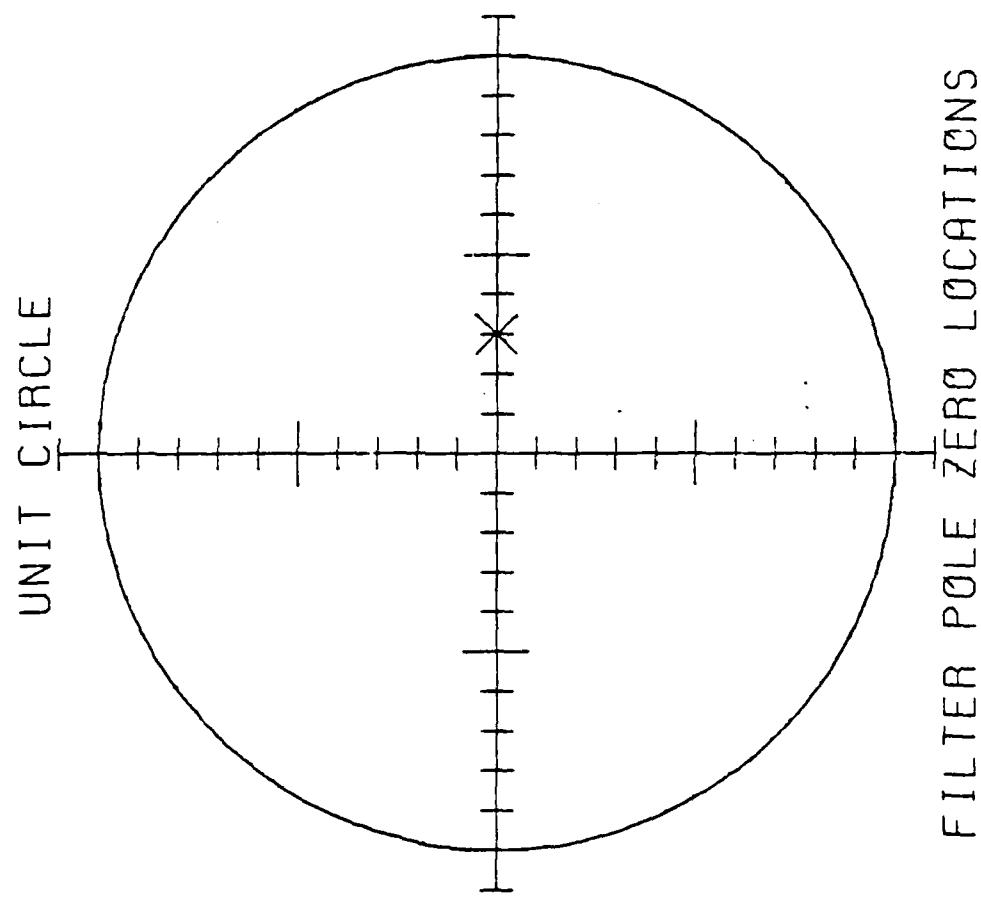


Figure 7-8a Example Of A Single Real Pole At (0,3)

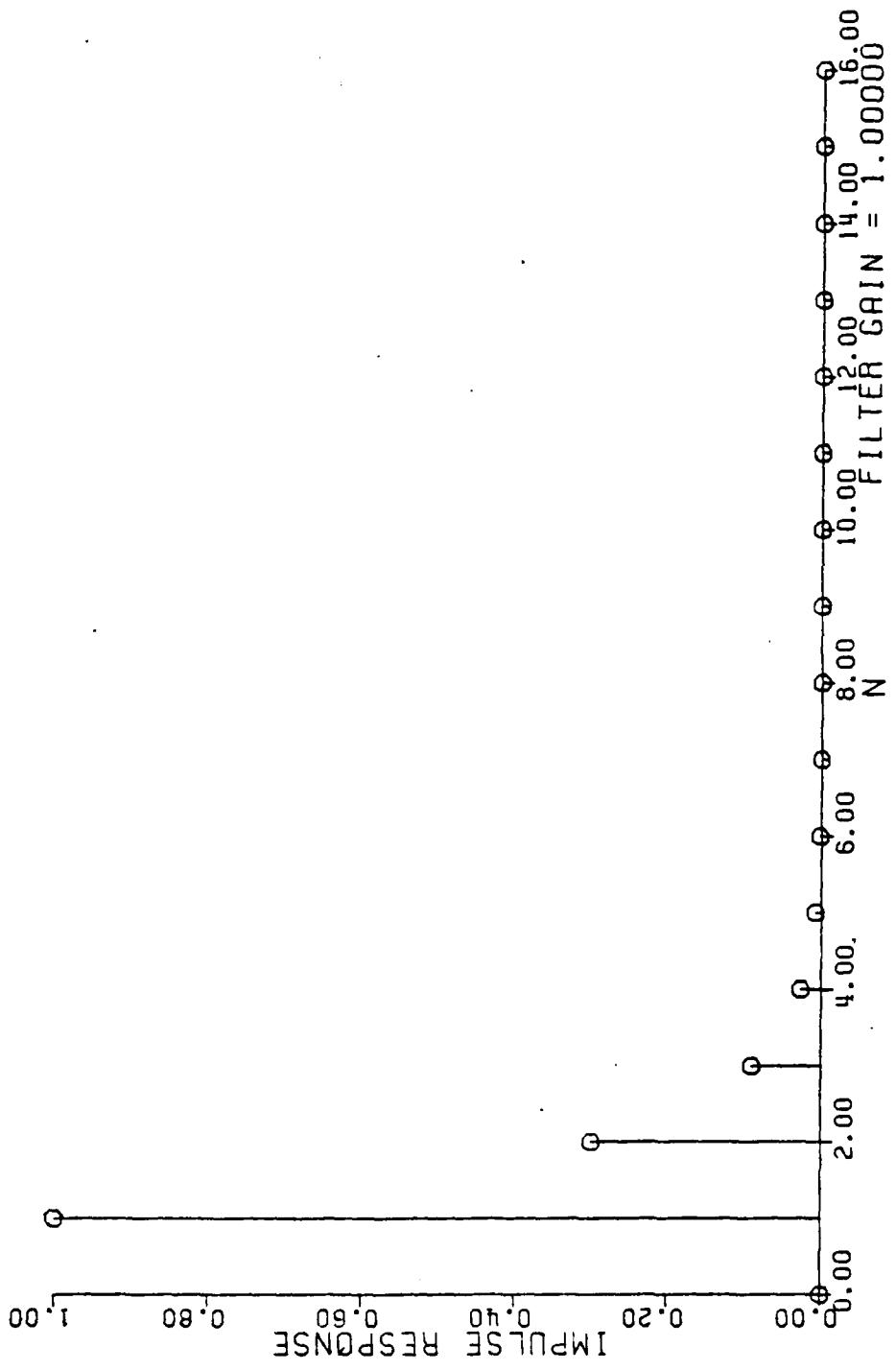


Figure 7-8b Unit Sample Response For A Single Real Pole At (0, 3)

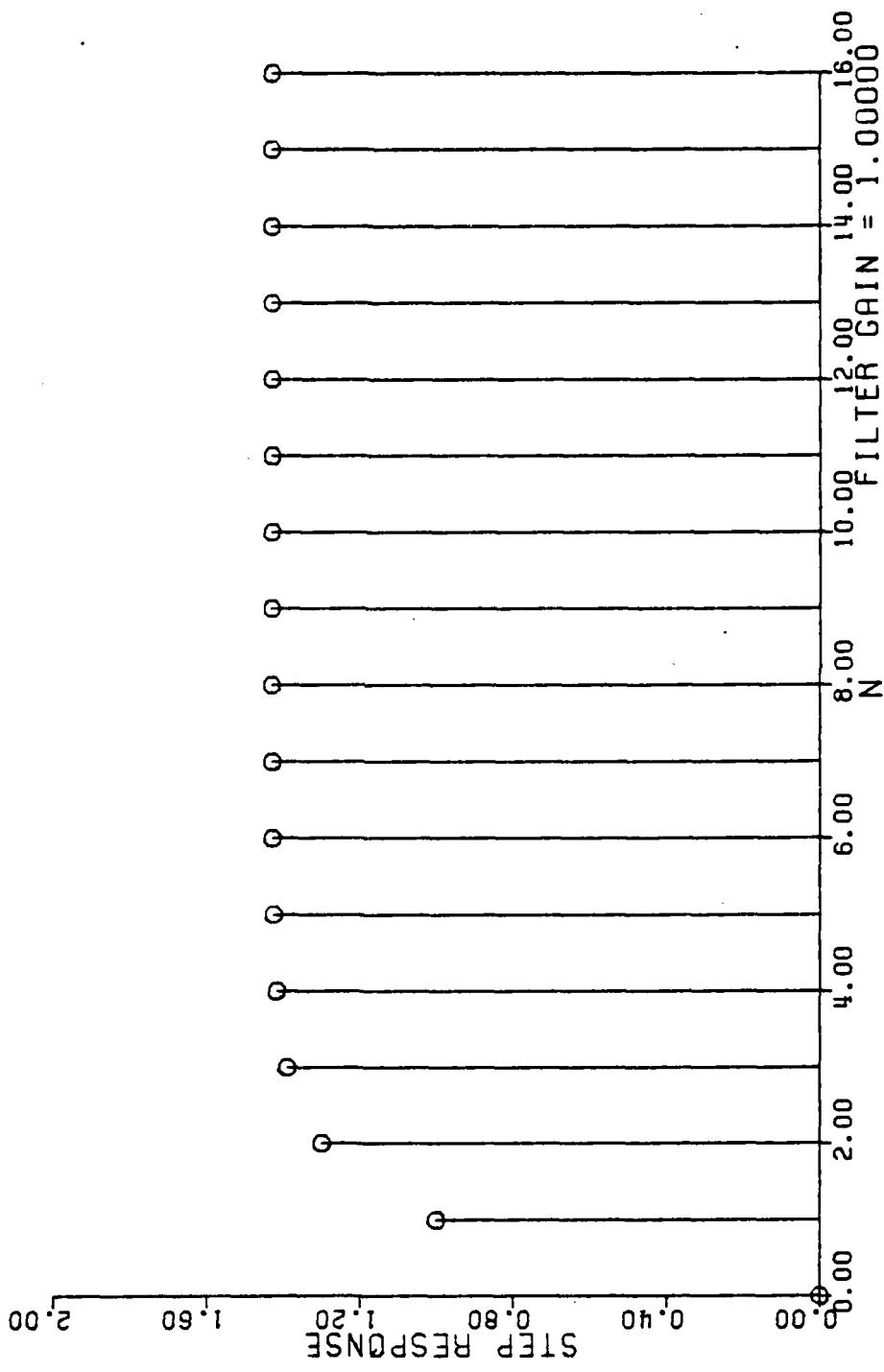


Figure 7-8c Unit Step Response For A Single Real Pole At (0.3)

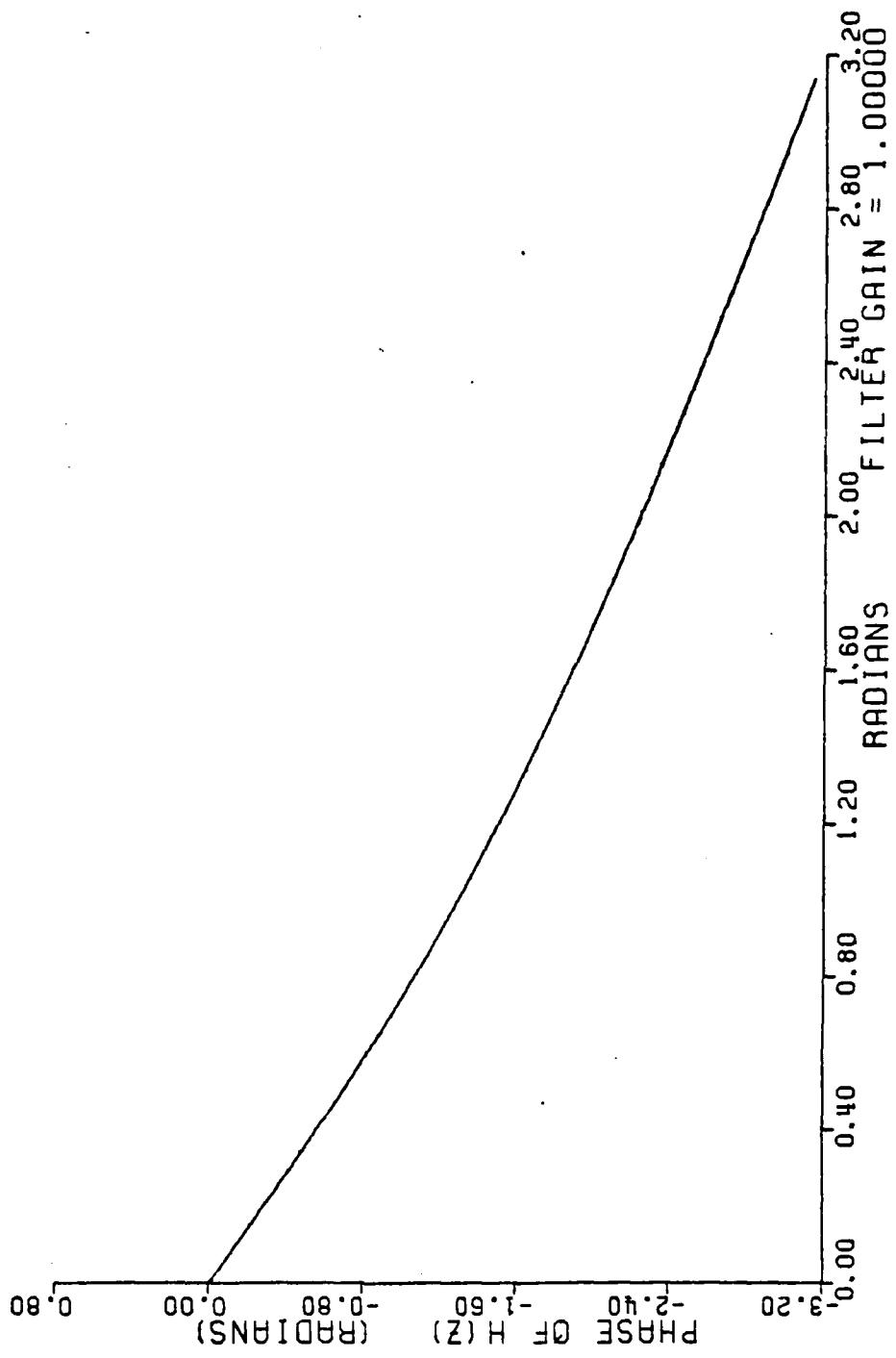


Figure 7-8d Phase Response For A Single Real Pole At (0, 3)

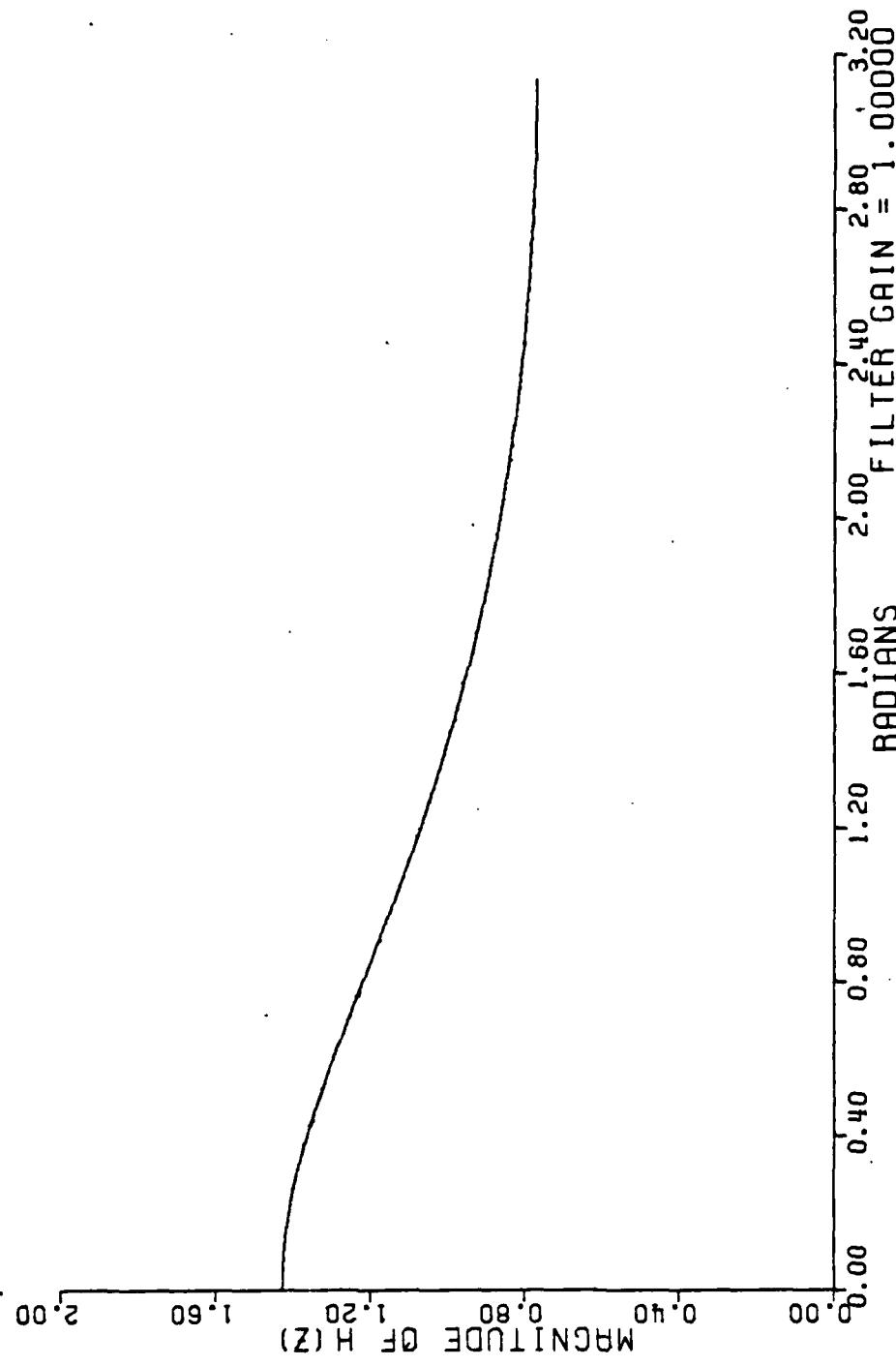


Figure 7-8e Magnitude of  $H(z)$  For A Single Real Pole At (0.3)

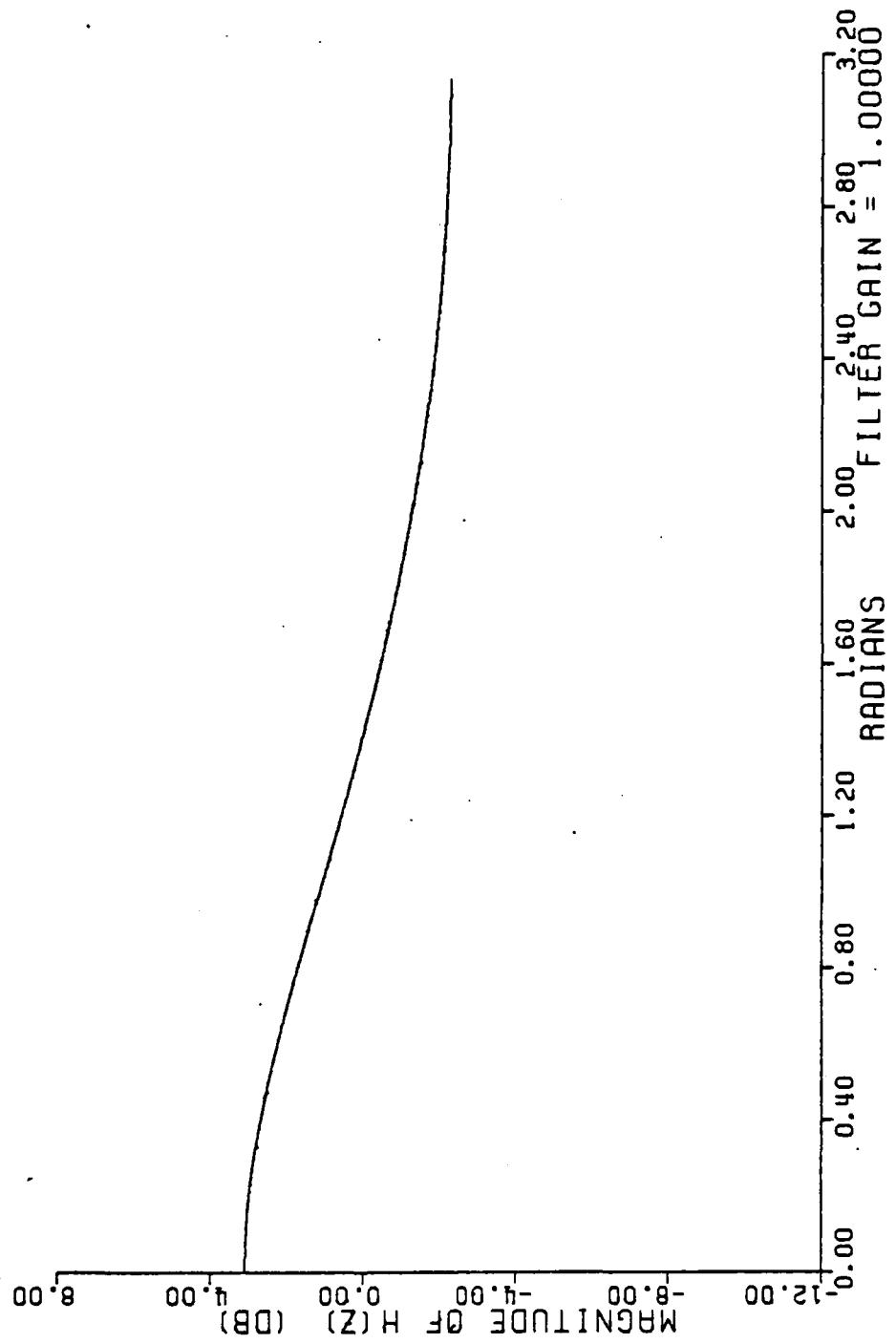


Figure 7-8f Magnitude Of  $H(z)$  In Decibels For A Single Real Pole At (0.3)

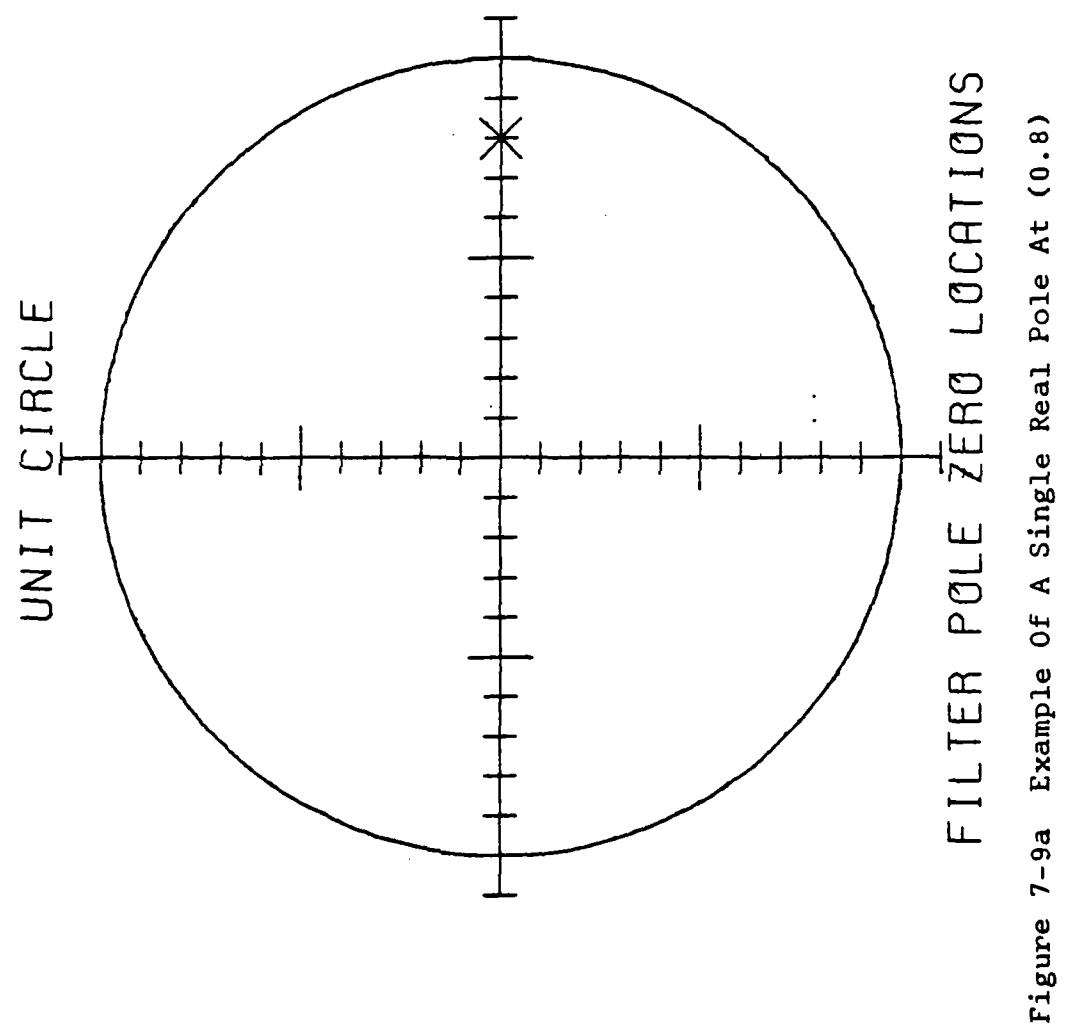


Figure 7-9a Example Of A Single Real Pole At (0.8)

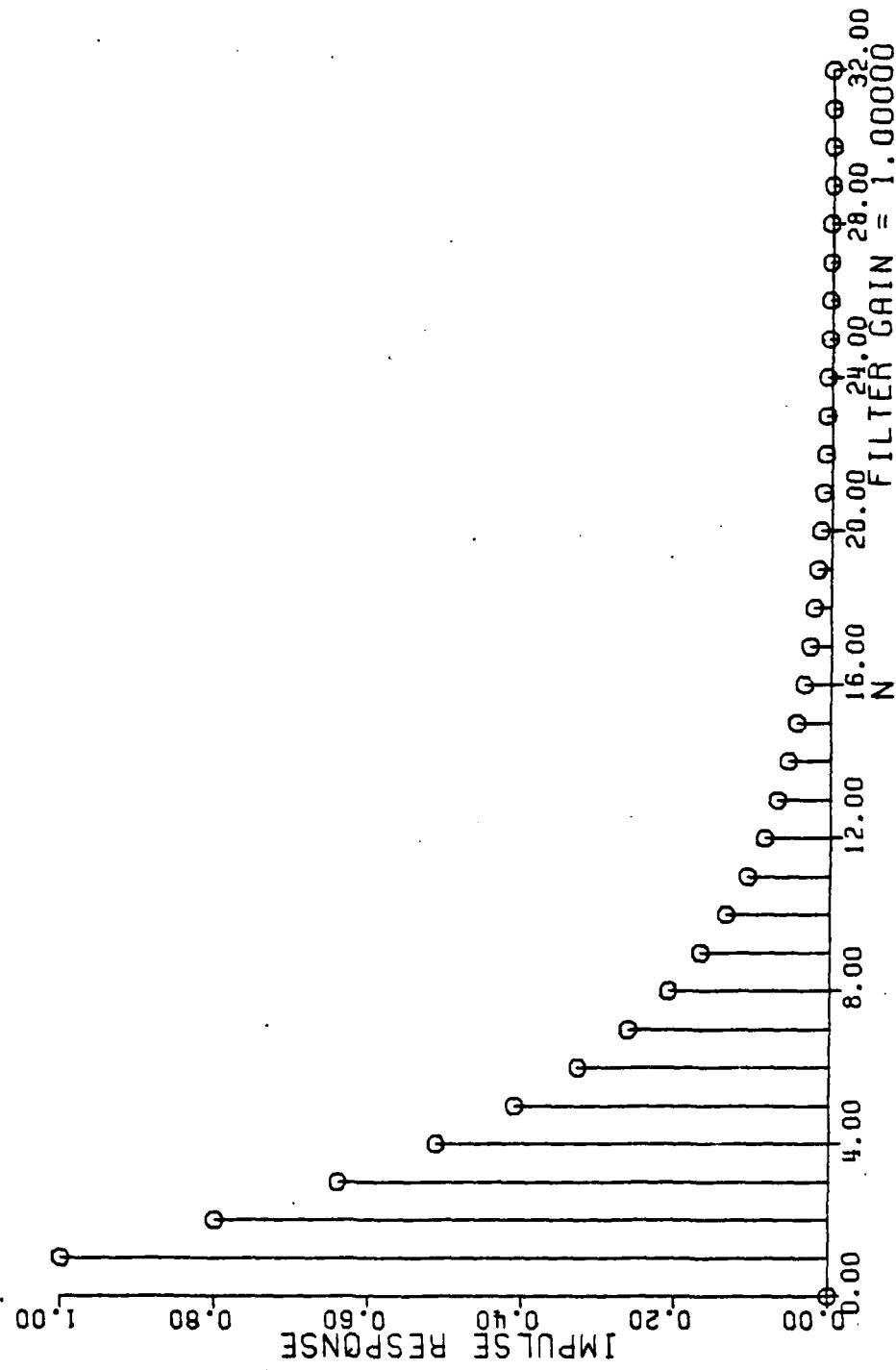


Figure 7-9b Unit Sample Response For A Single Real Pole At (0.8)

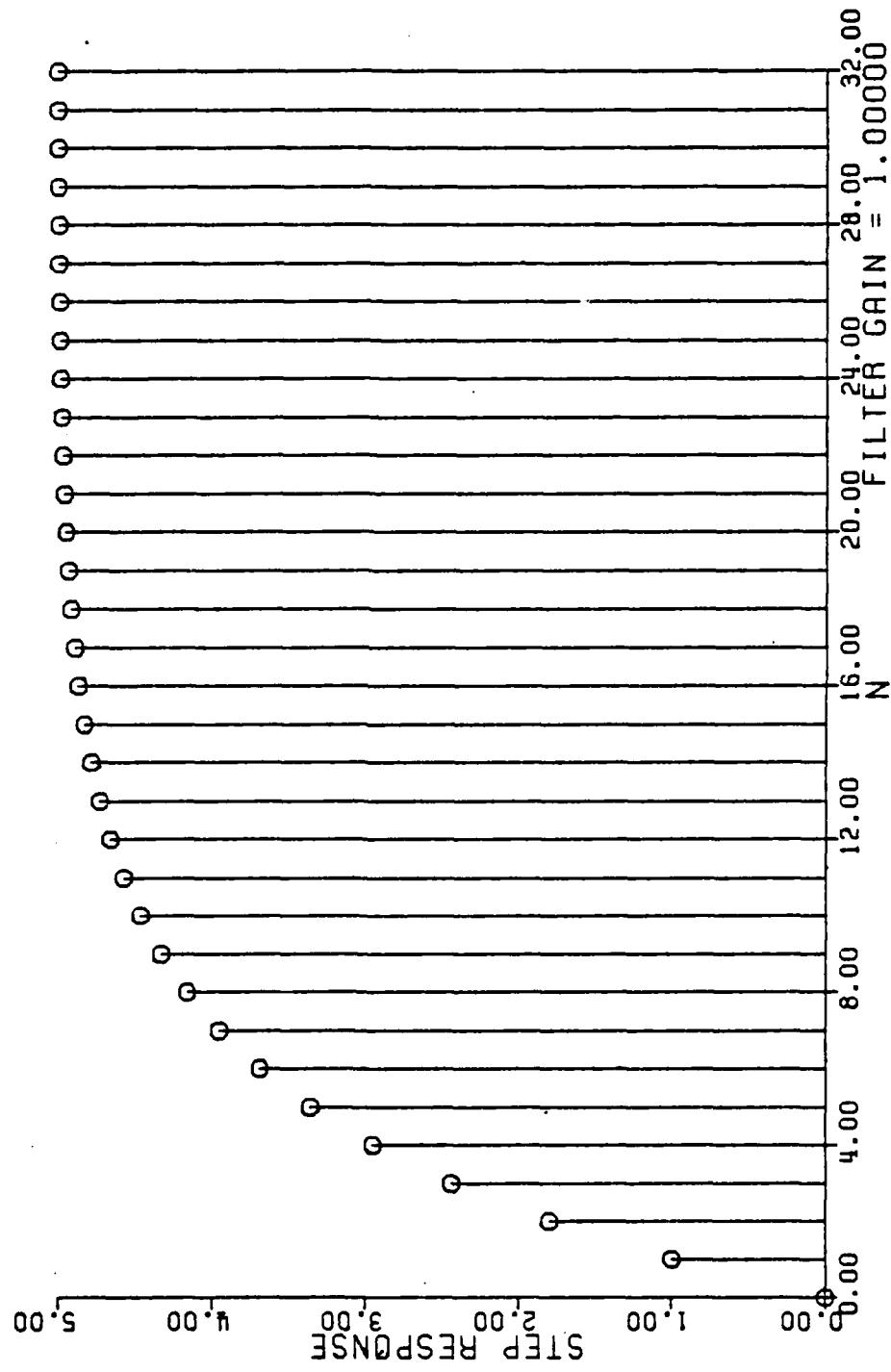


Figure 7-9c Unit Step Response For A Single Real Pole At (0.8)

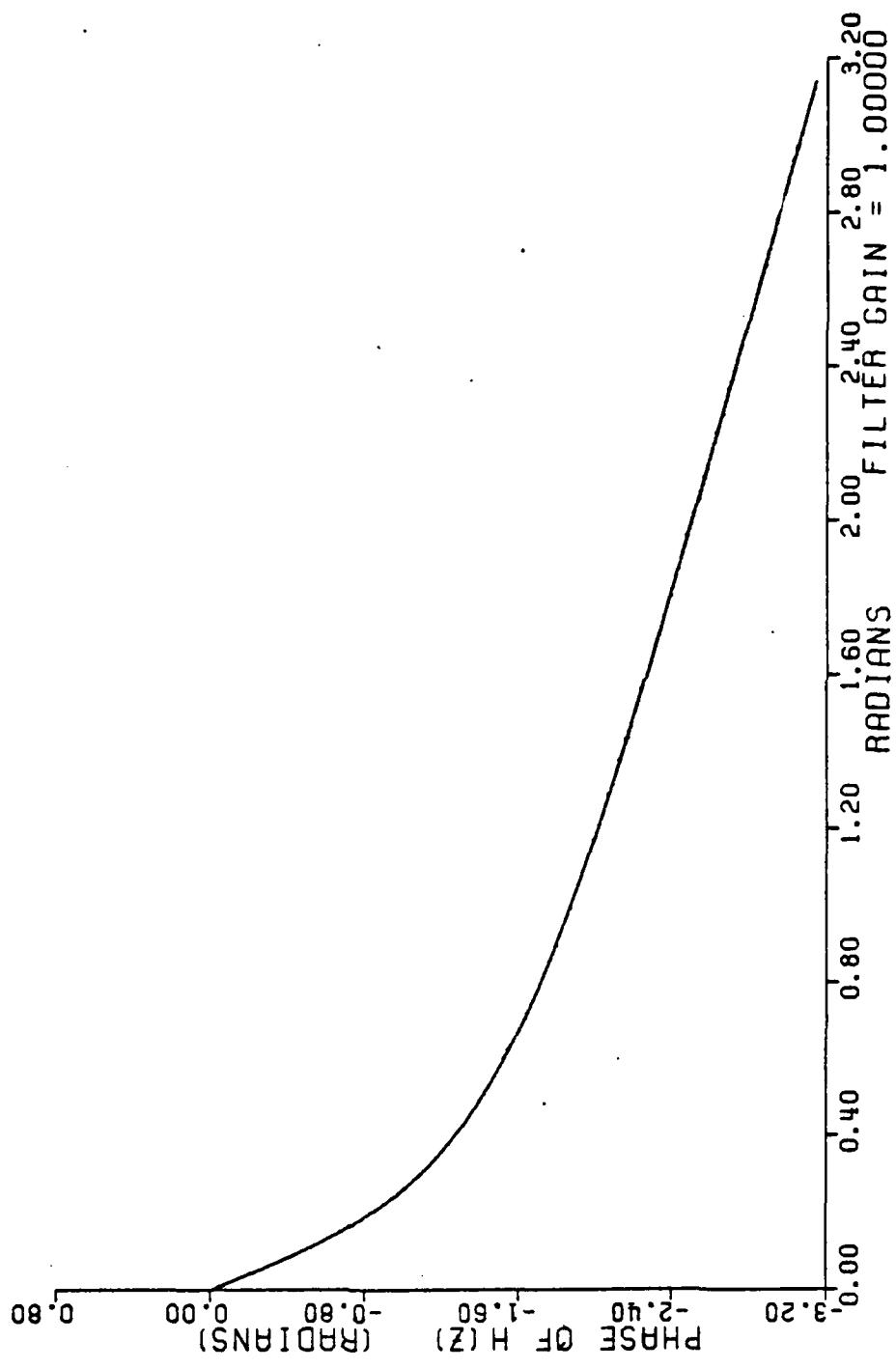


Figure 7-9d Phase Response For A Single Real Pole At (0.8)

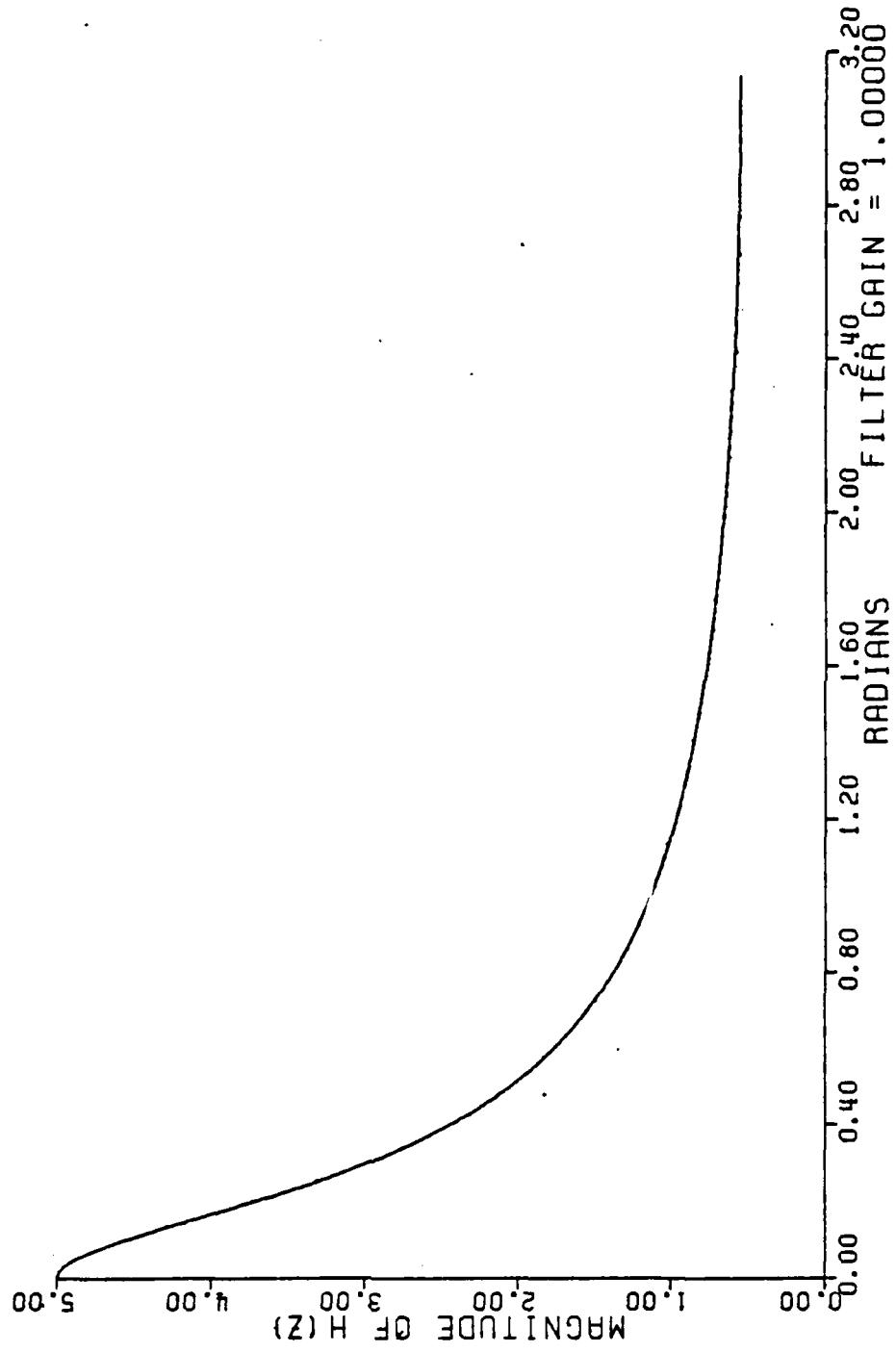


Figure 7-9e Magnitude Of  $H(z)$  For A Single Real Pole At (0.8)

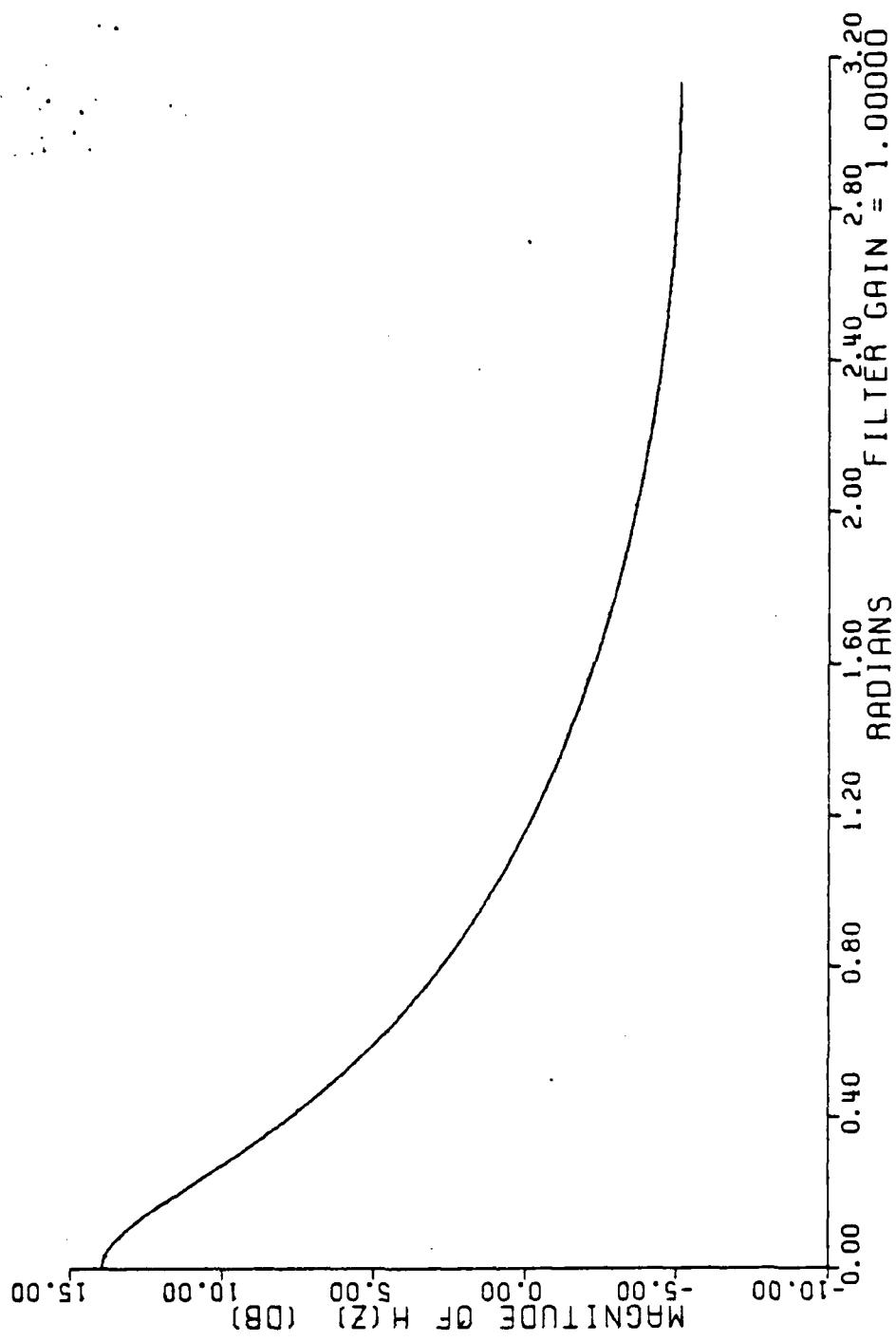


Figure 7-9f Magnitude Of  $H(z)$  For A Single Real Pole At (0.8)

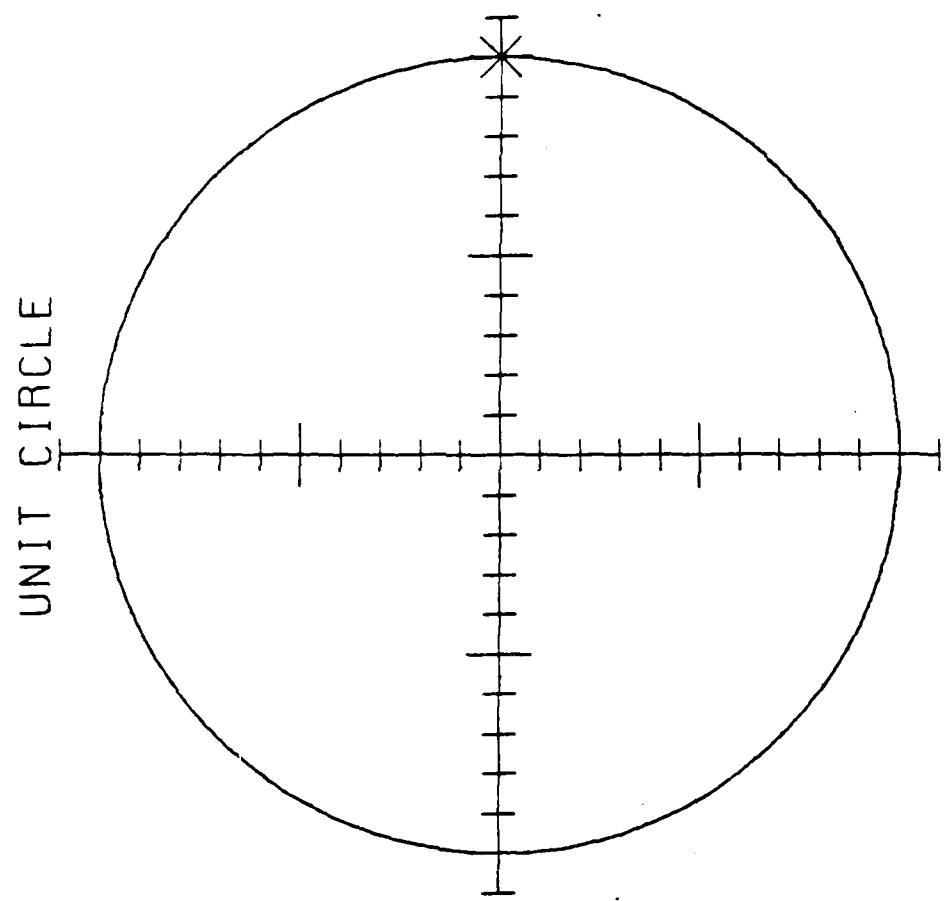


Figure 7-10a Example Of A Single Real Pole On the Unit Circle at (1.0)

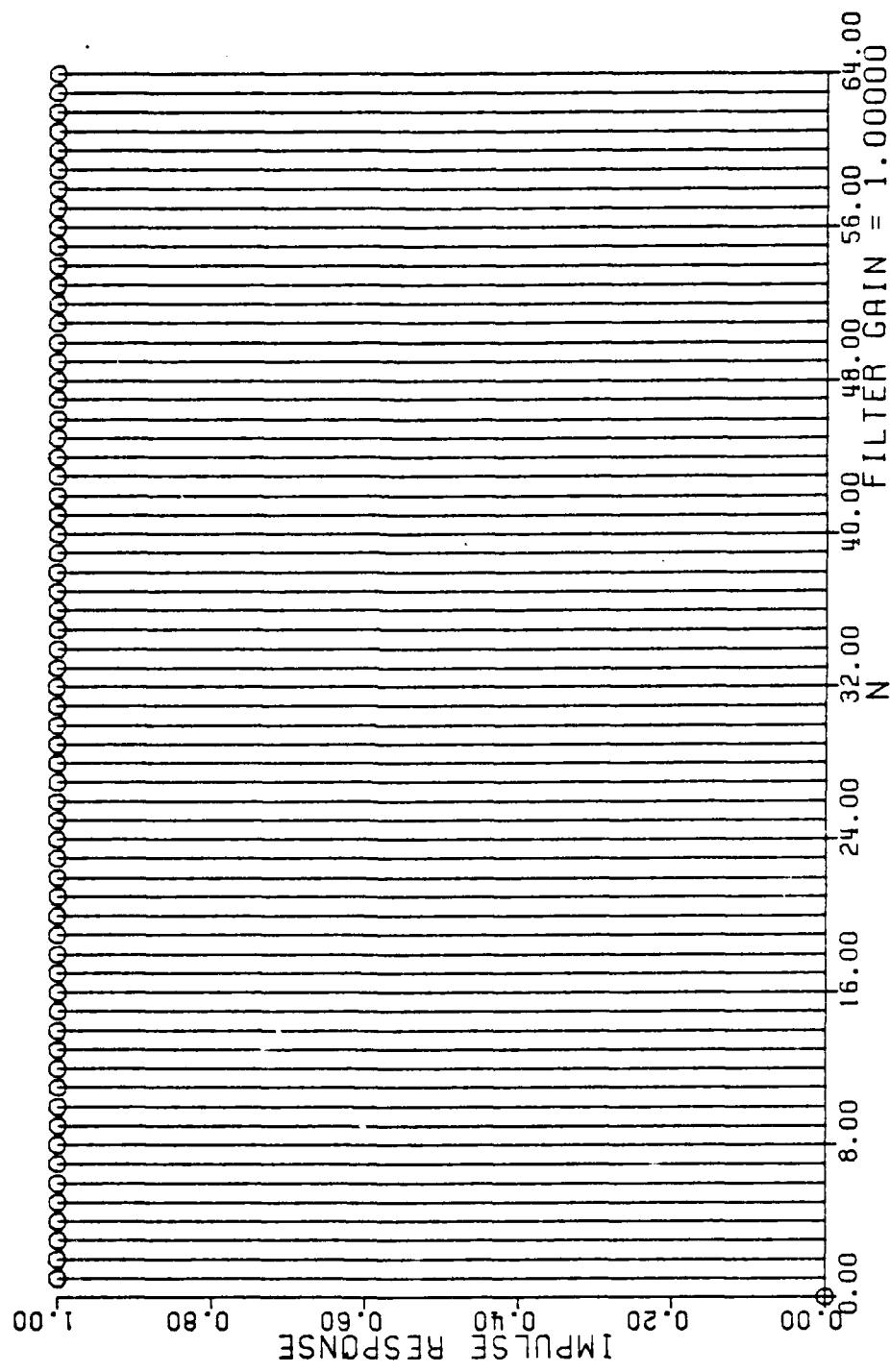


Figure 7-10b Unit Sample Response For A Single Real Pole At (1.0)

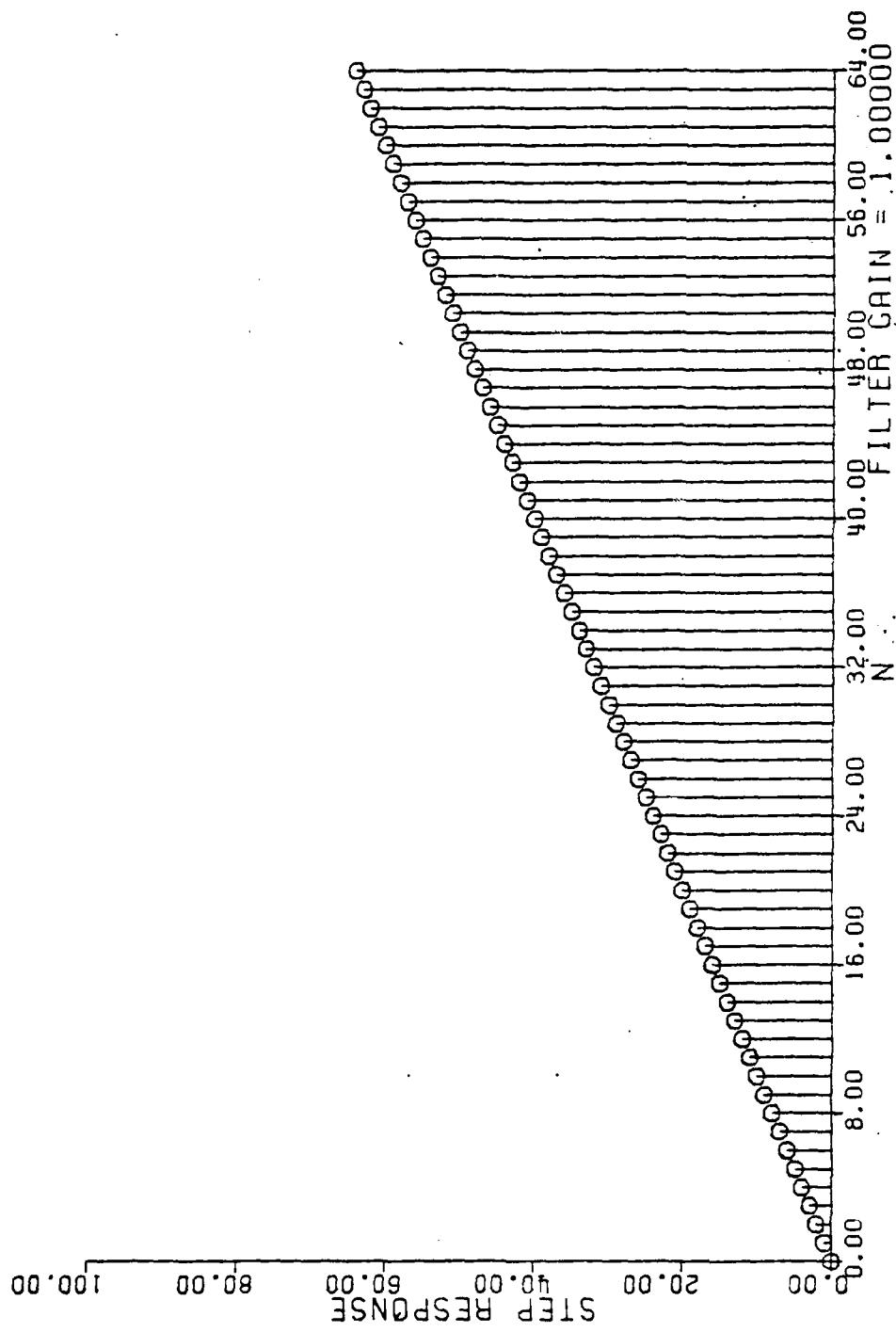


Figure 7-10c Unit Step Response For A Single Real Pole At (1.0)

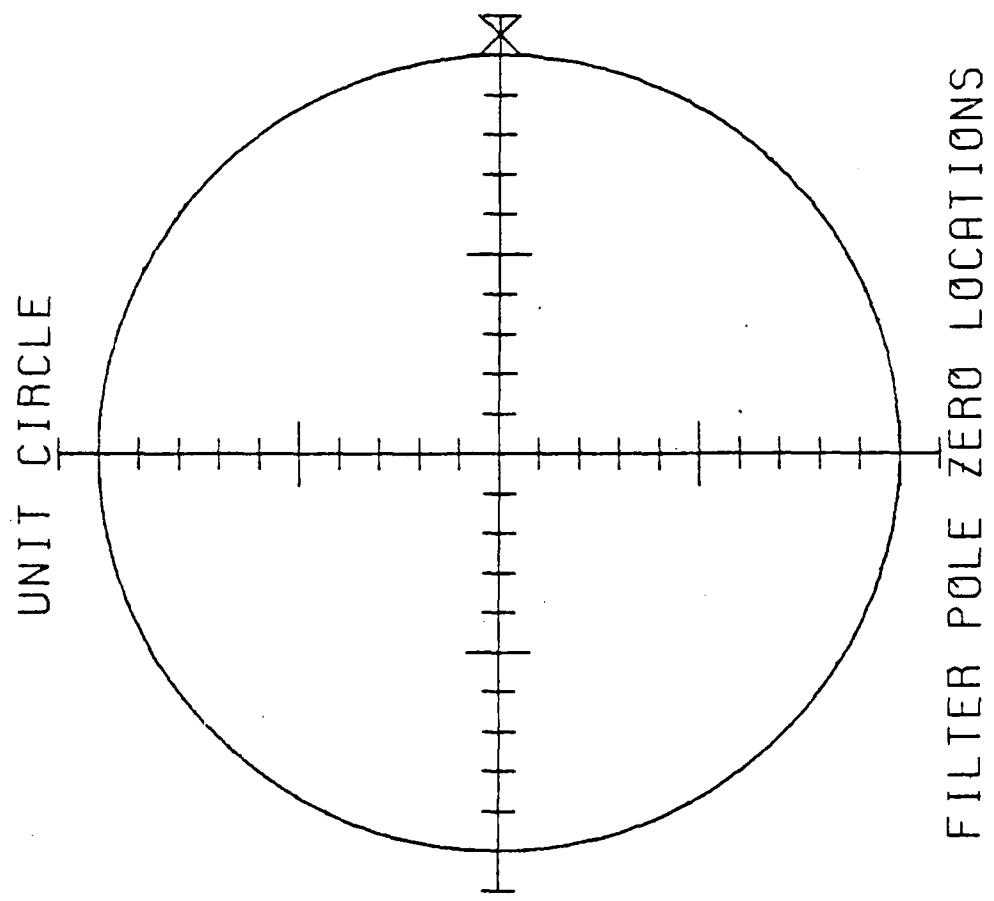


Figure 7-11a Example Of A Single Real Pole Outside The Unit Circle At (1.05)

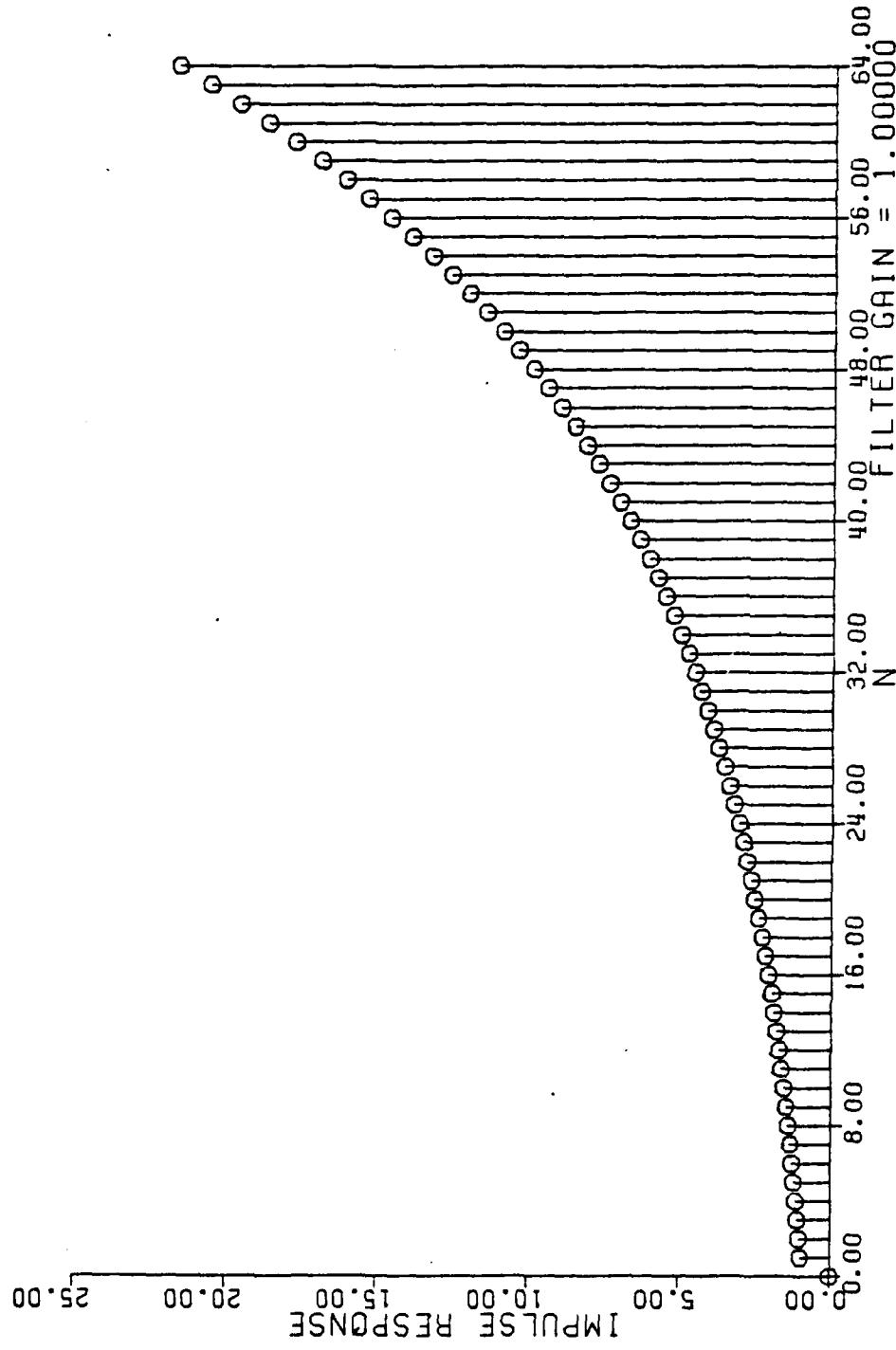


Figure 7-11b Unit Sample Response For A Single Real Pole At  $(1.05)$

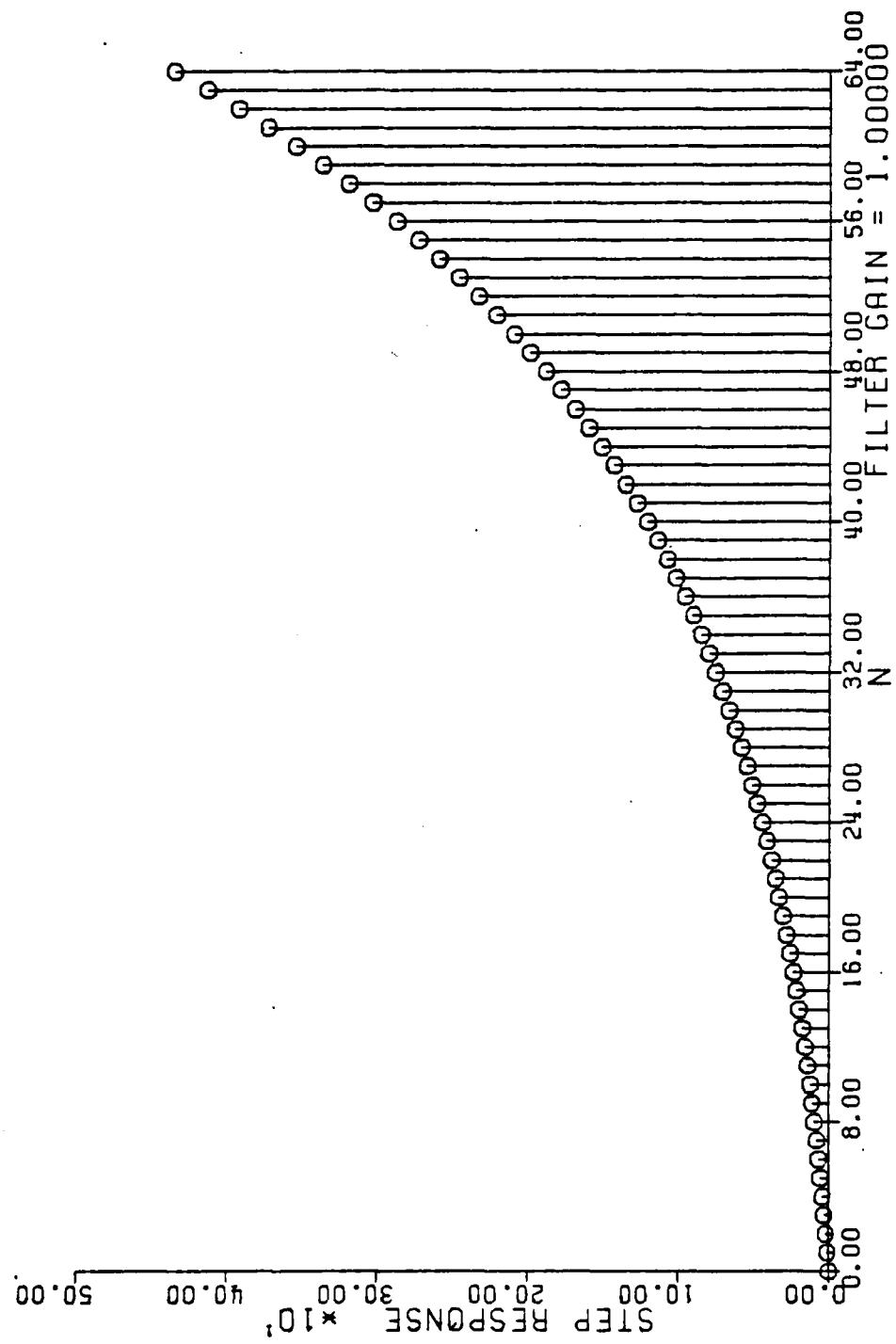


Figure 7-11c Unit Step Response For A Single Real Pole At (1.05)

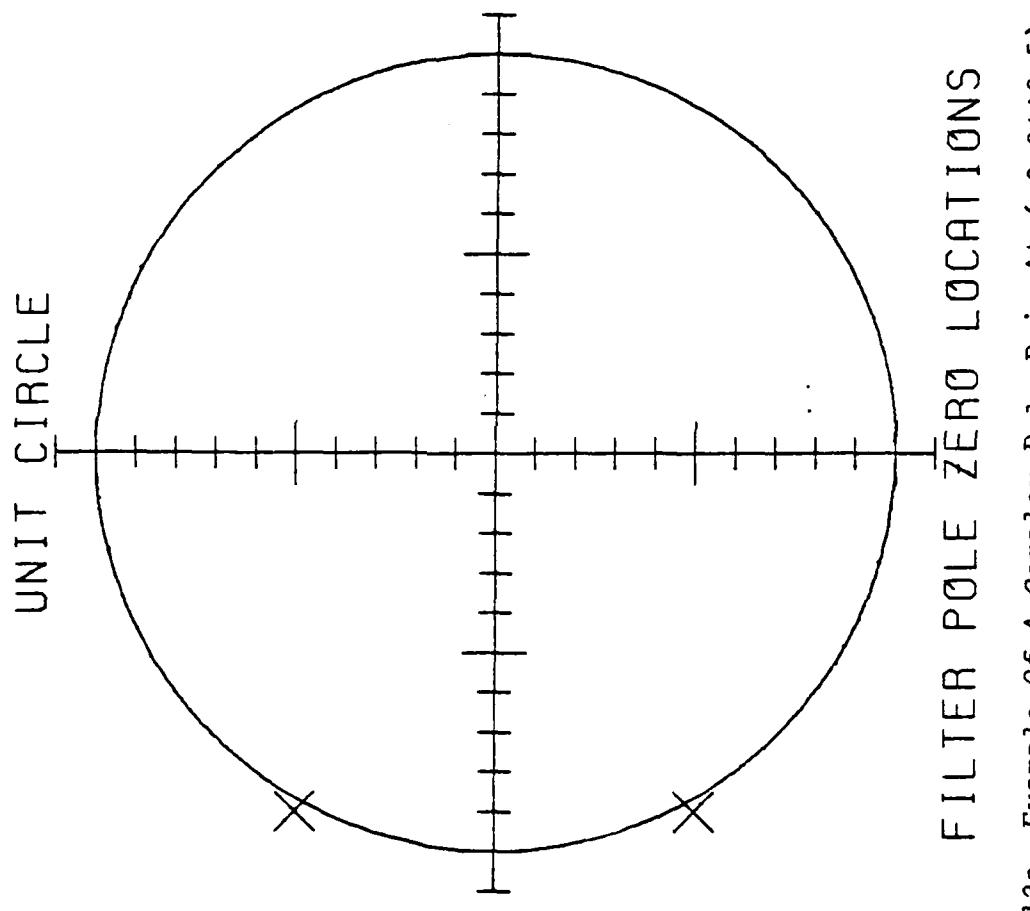


Figure 7-12a Example of A Complex Pole Pair At  $(-0.8 \pm j0.5)$

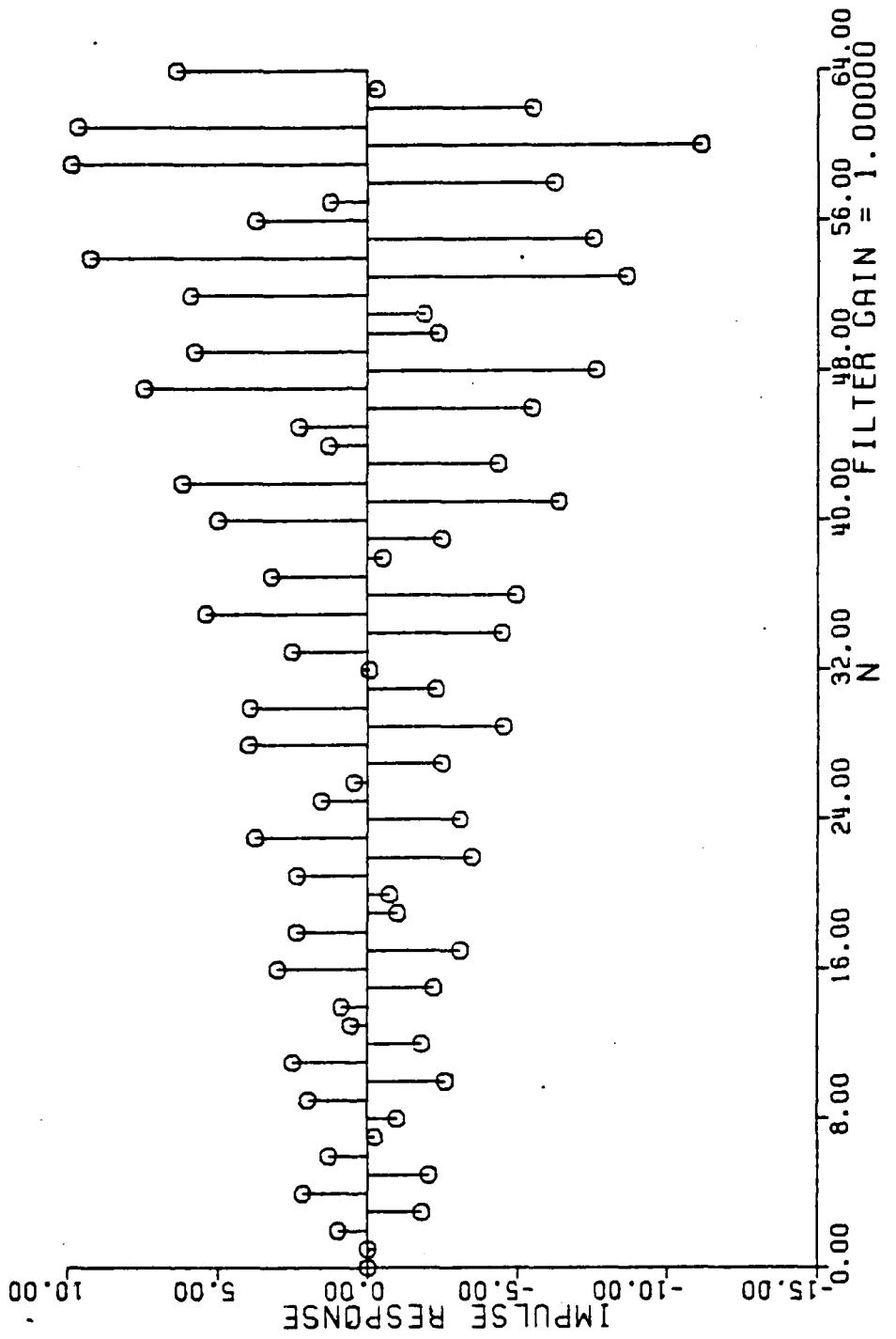


Figure 7-12b Unit Sample Response For A Complex Pole Pair At  $(-0.8 \pm j0.5)$

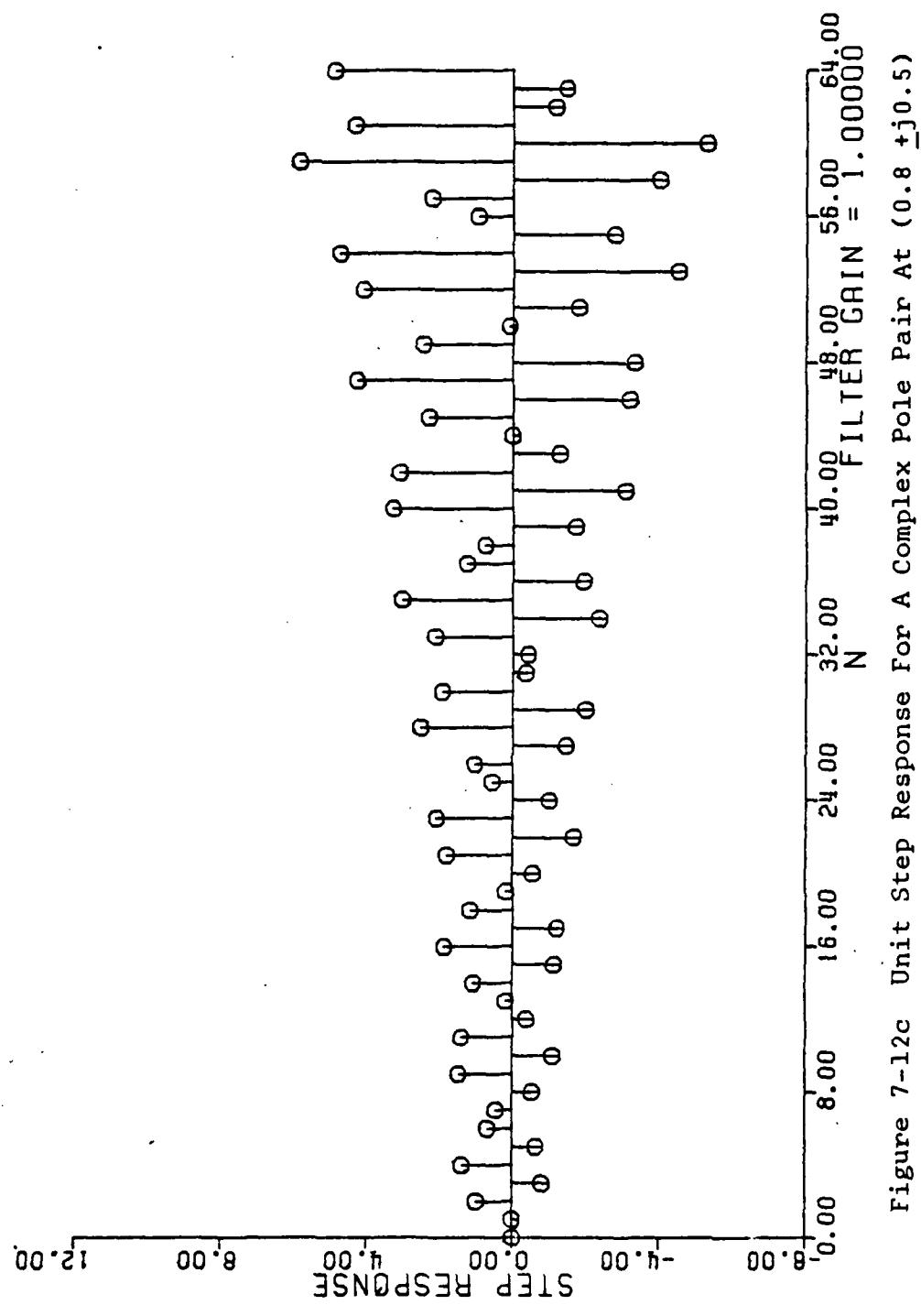


Figure 7-12c Unit Step Response For A Complex Pole Pair At  $(0.8 + j0.5)$

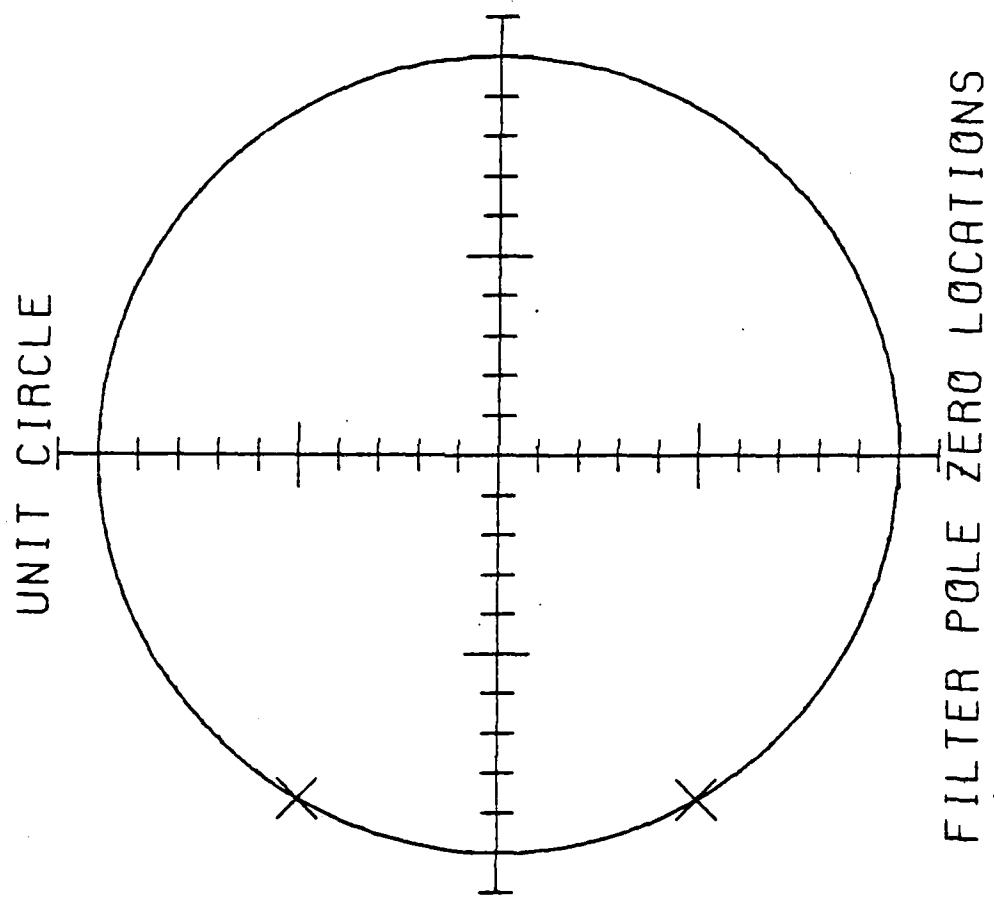


Figure 7-13a Example Of A Complex Pole Pair On The Unit Circle At  
 $(-.866025 \pm j0.5)$

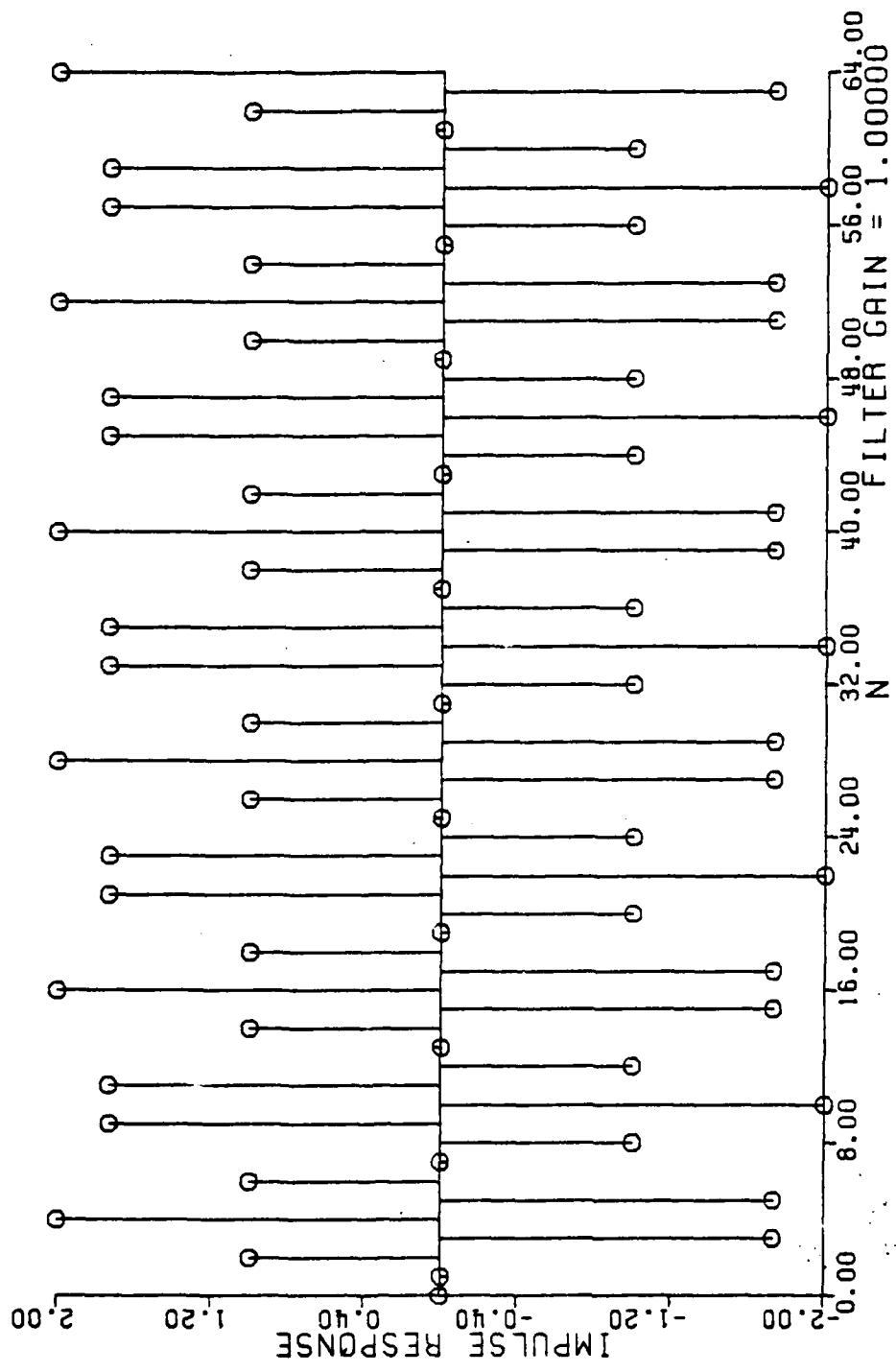


Figure 7-13b Unit Sample Response Of A Complex Pole Pair At  $(-0.866025 \pm j0.5)$

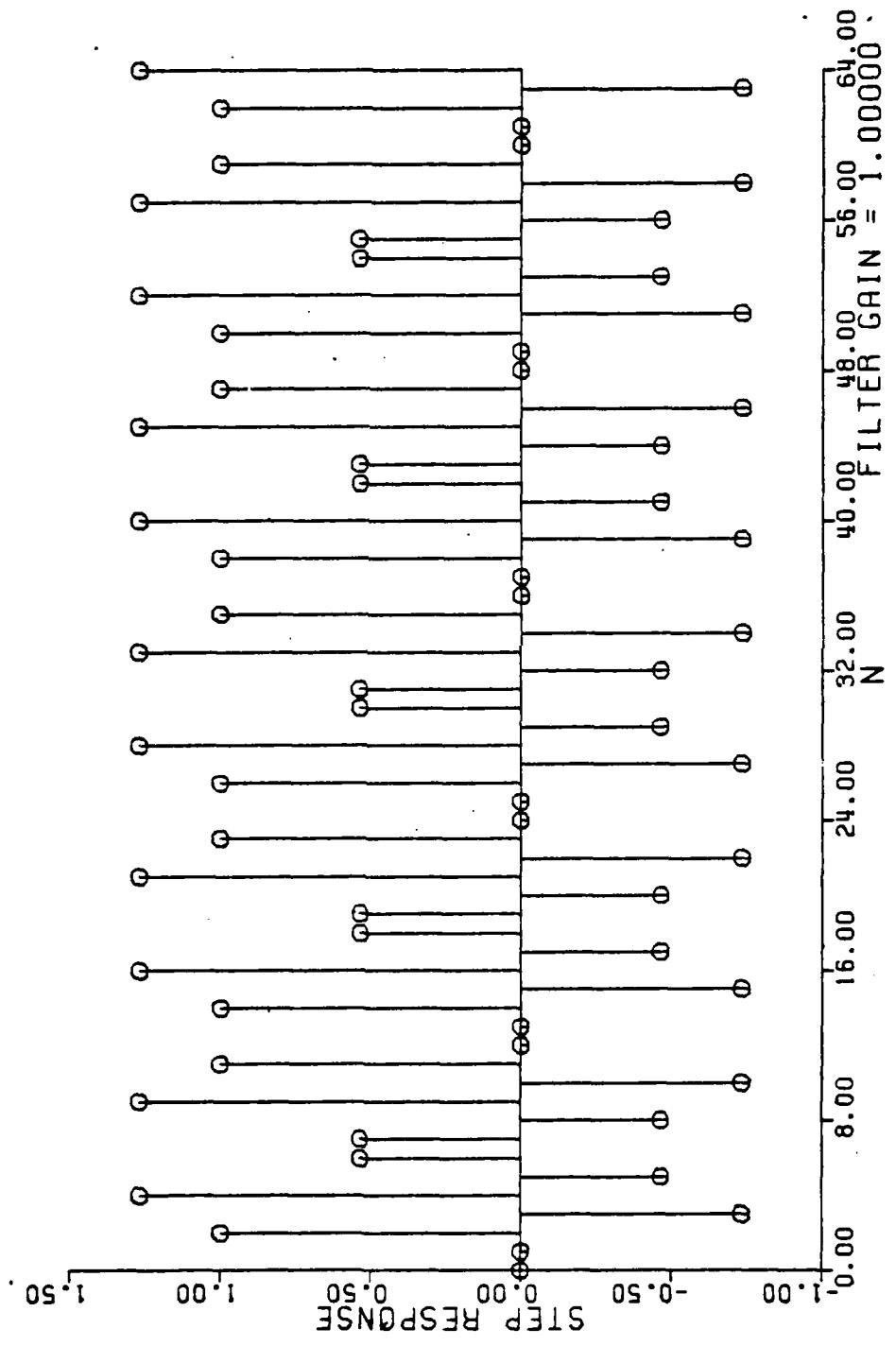


Figure 7-13c Unit Step Response Of A Complex Pole Pair At  $(-0.866025 \pm j0.5)$

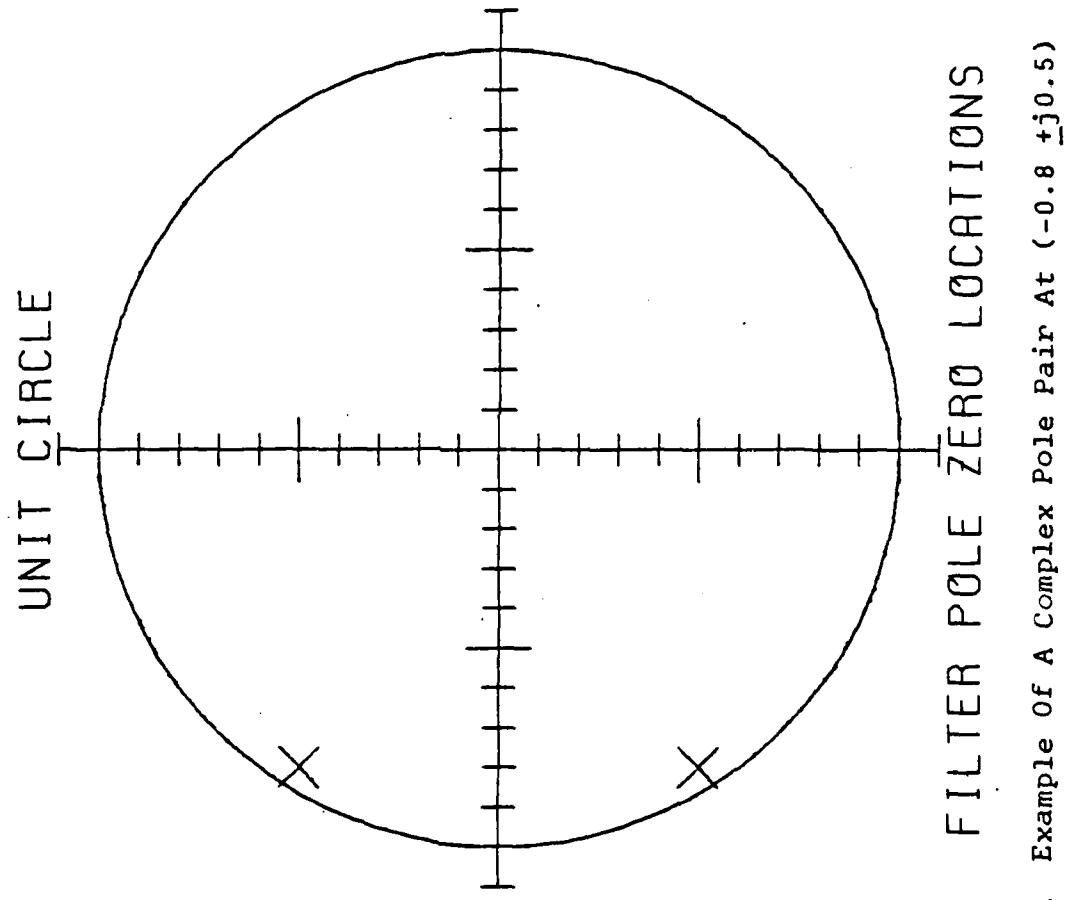


Figure 7-14a Example Of A Complex Pole Pair At  $(-0.8 \pm j0.5)$

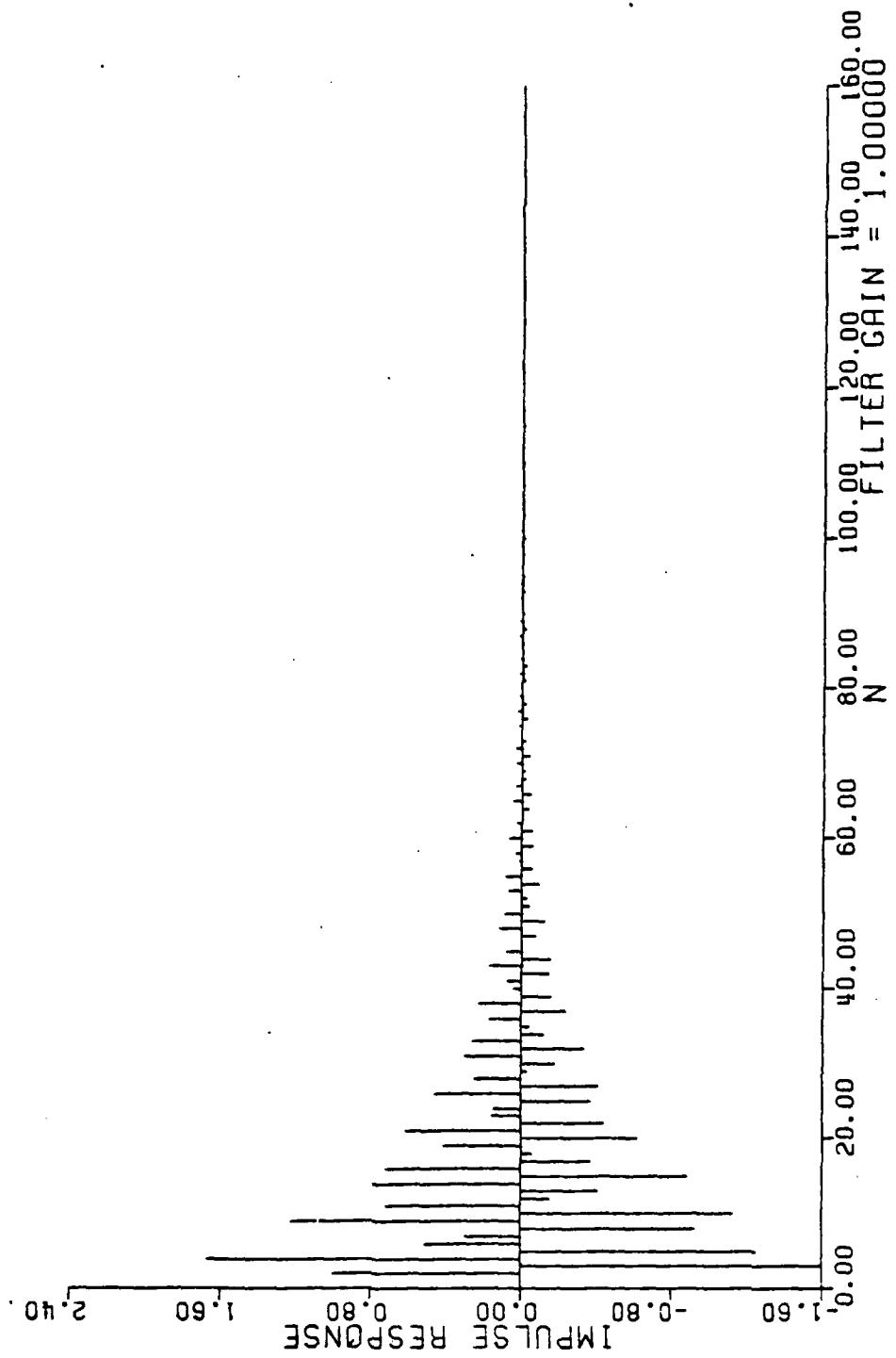


Figure 7-14b Unit Sample Response For A Complex Pole Pair At (-0.8 +j0.5)

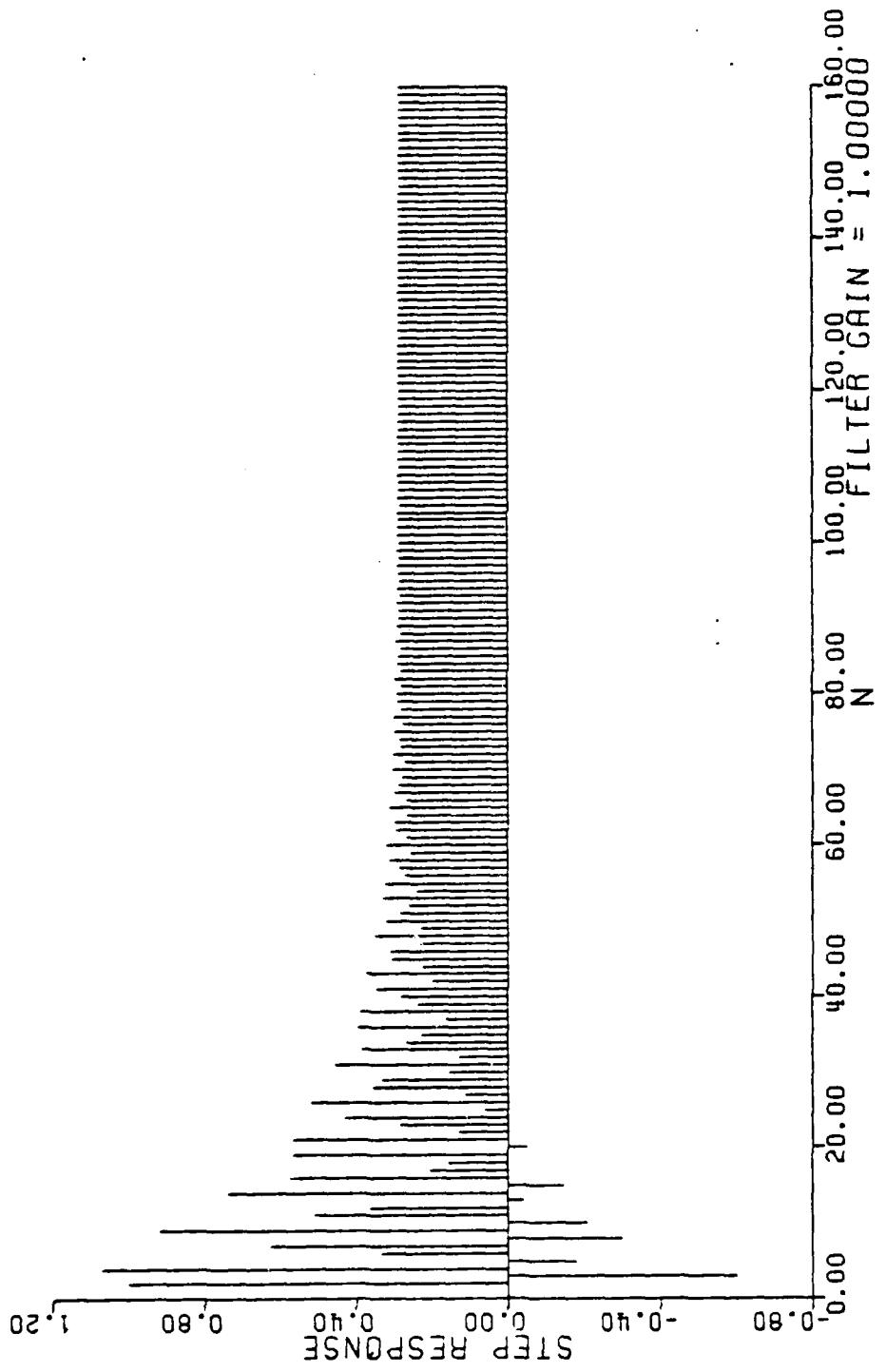


Figure 7.14c Unit Step Response For a Complex Pole Pair At (-0.8 +j0.5)

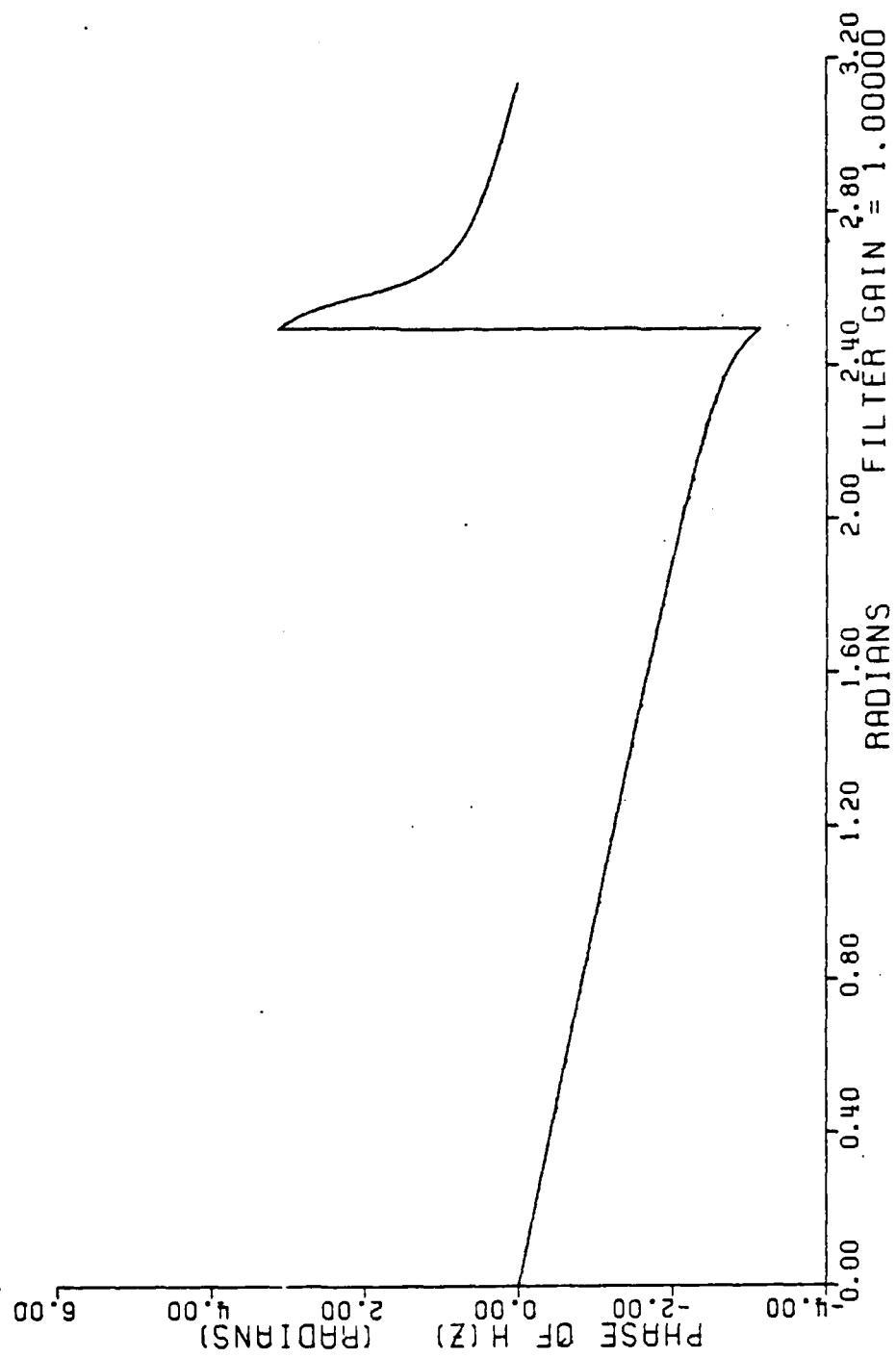


Figure 7-14d Phase Response For A Complex Pole Pair At  $(-0.8 + j0.5)$

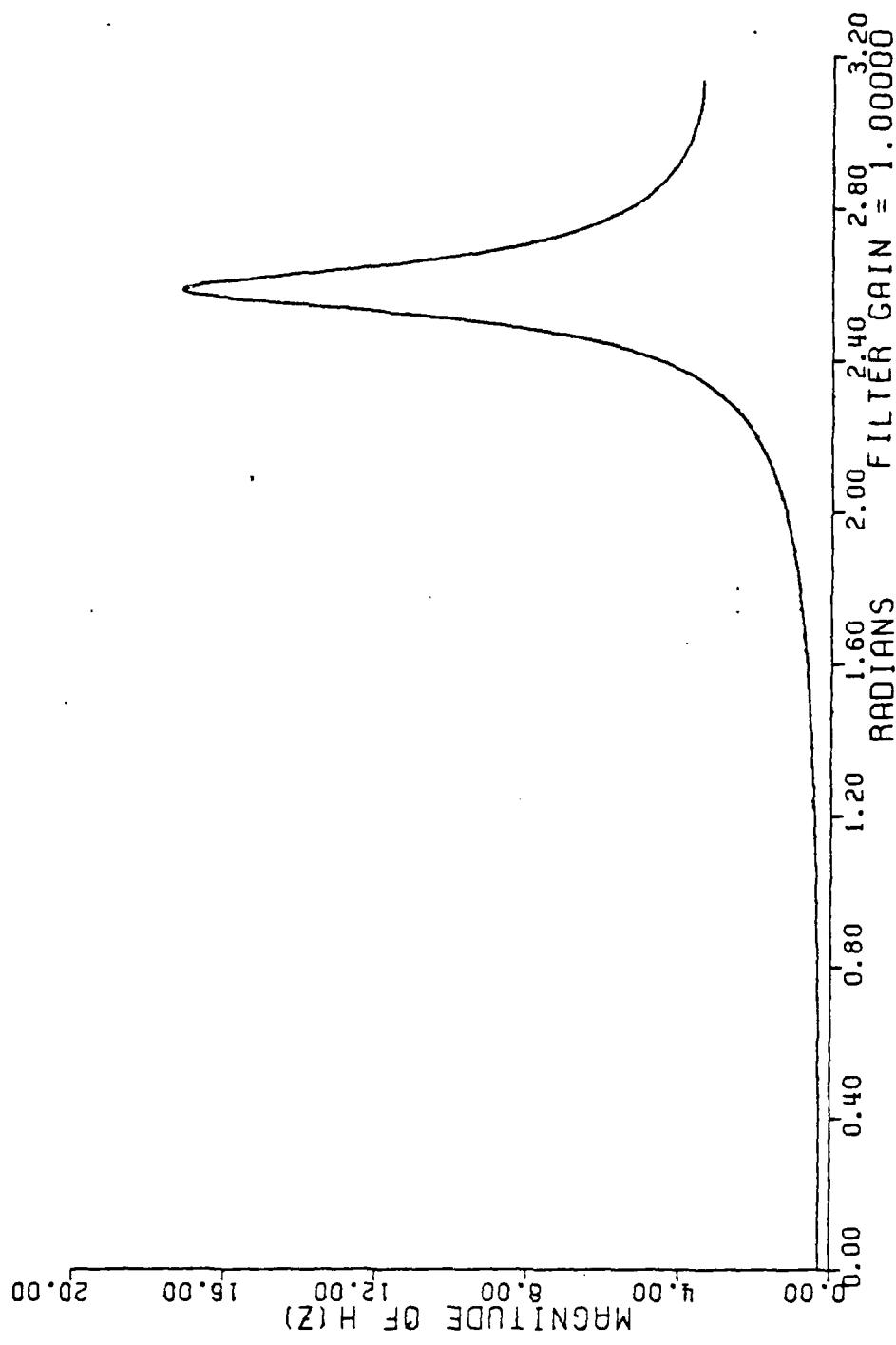


Figure 7-14e Magnitude Of  $H(z)$  For A Complex Pole Pair At  $(-0.8 \pm j0.5)$

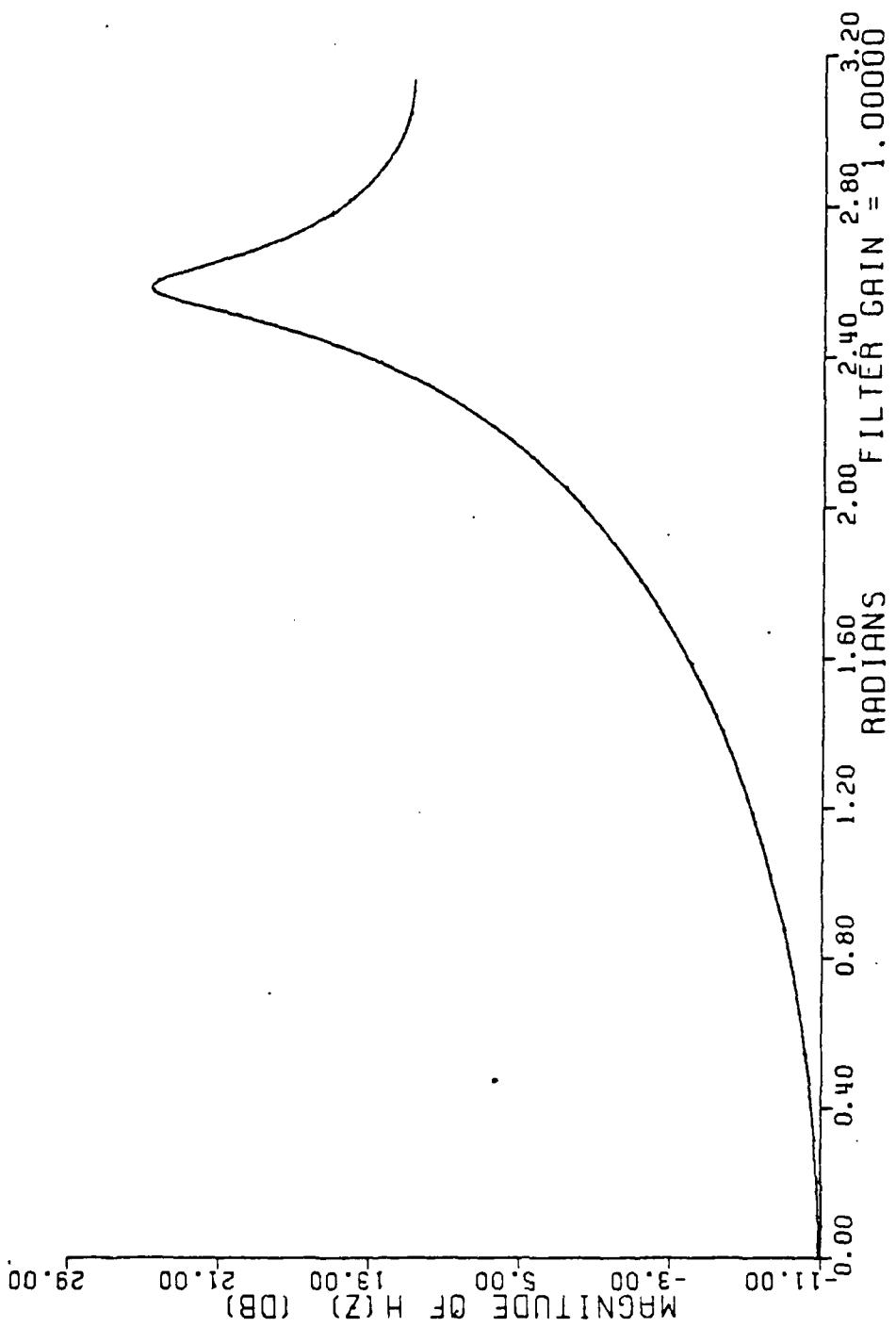


Figure 7-14f Magnitude Of  $H(z)$  In Decibels For A Complex Pole Pair At  $(-0.8 \pm j0.5)$

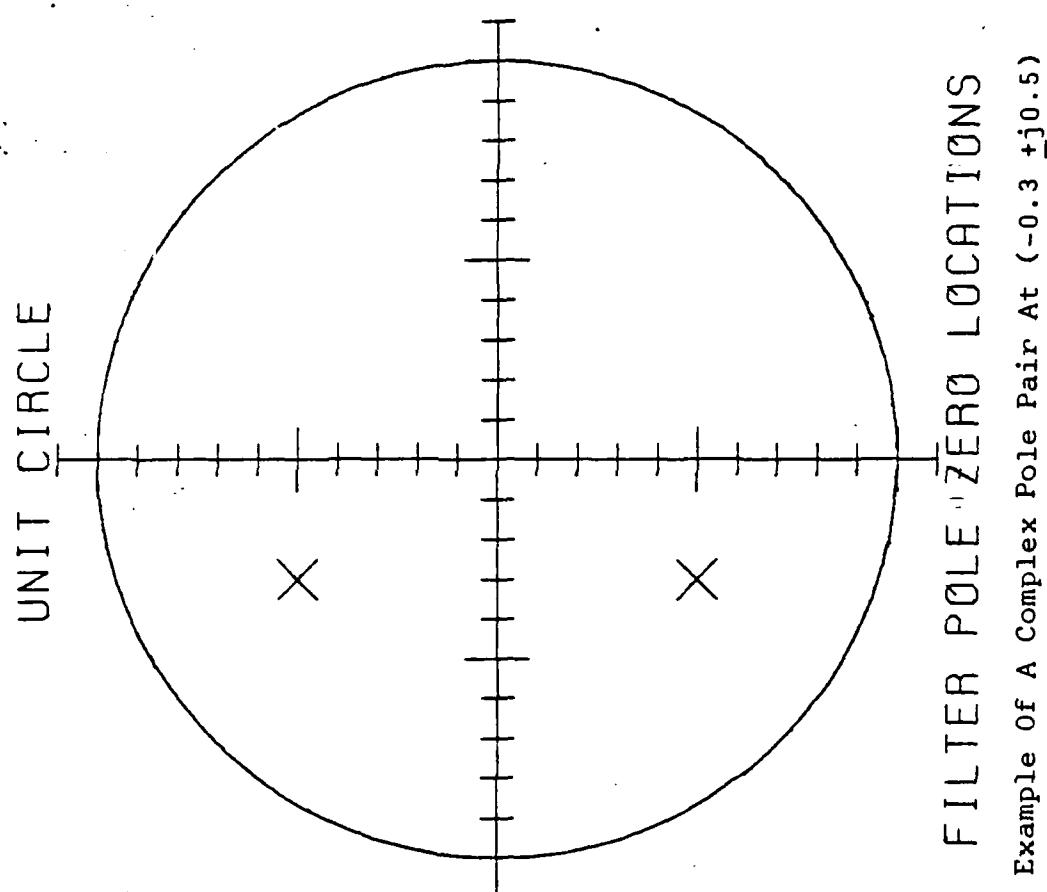


Figure 7-15a Example of A Complex Pole Pair At  $(-0.3 + j0.5)$

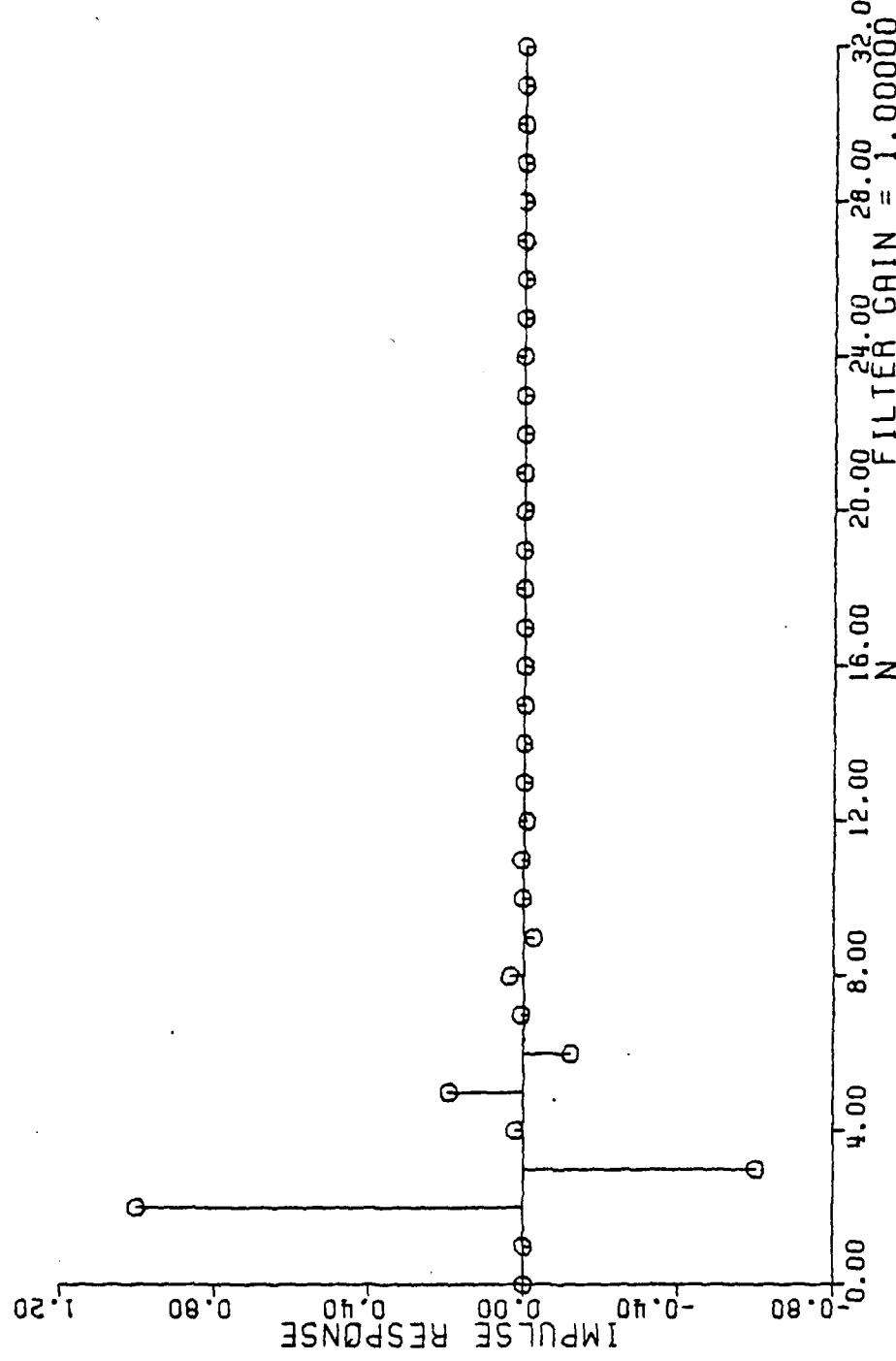


Figure 7-15b Unit Sample Response For A Complex Pole Pair At (-0.3 +j0.5)

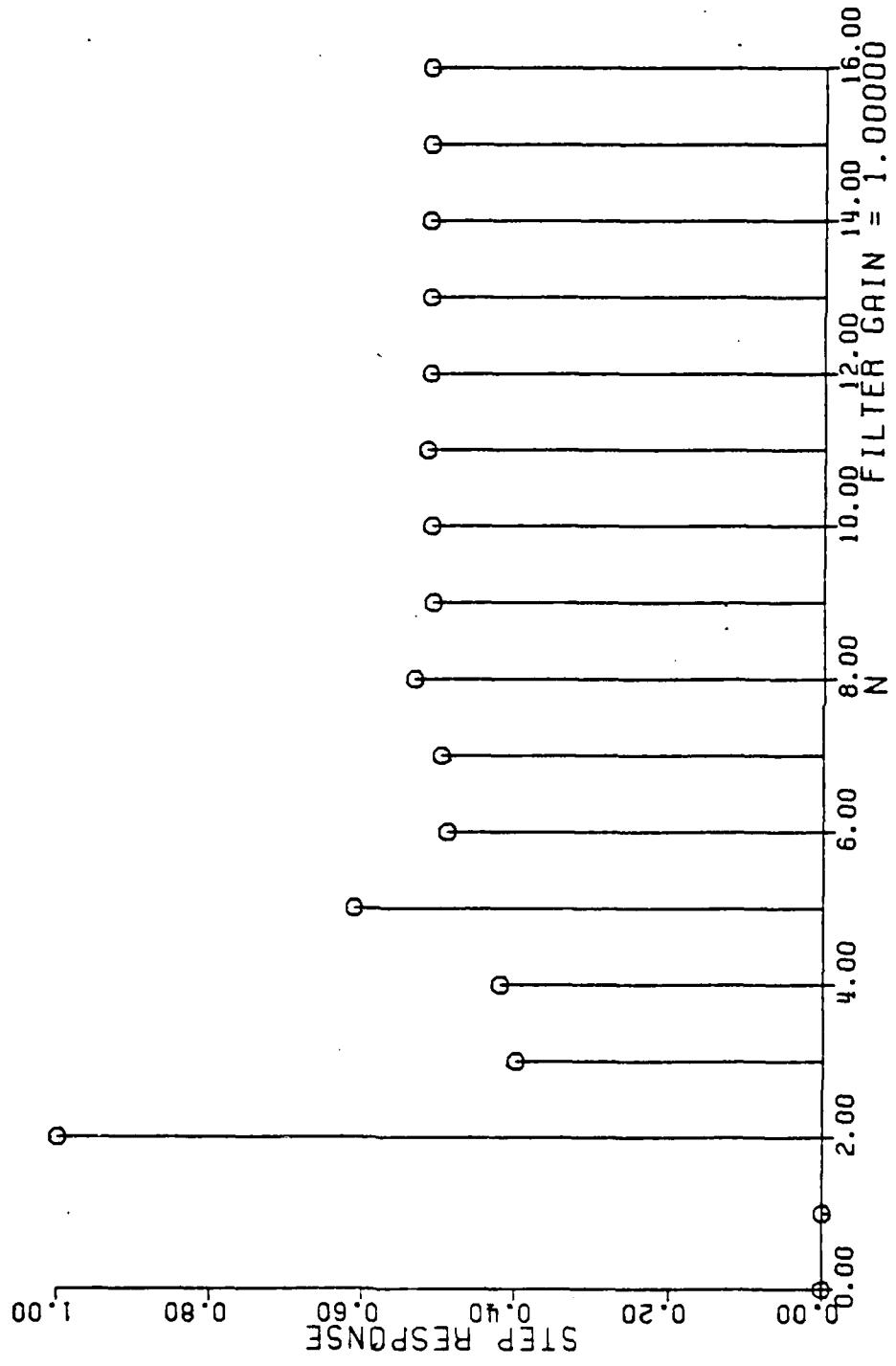


Figure 7-15c Unit Step Response For A Complex Pole Pair At  $(-0.3 \pm j0.5)$

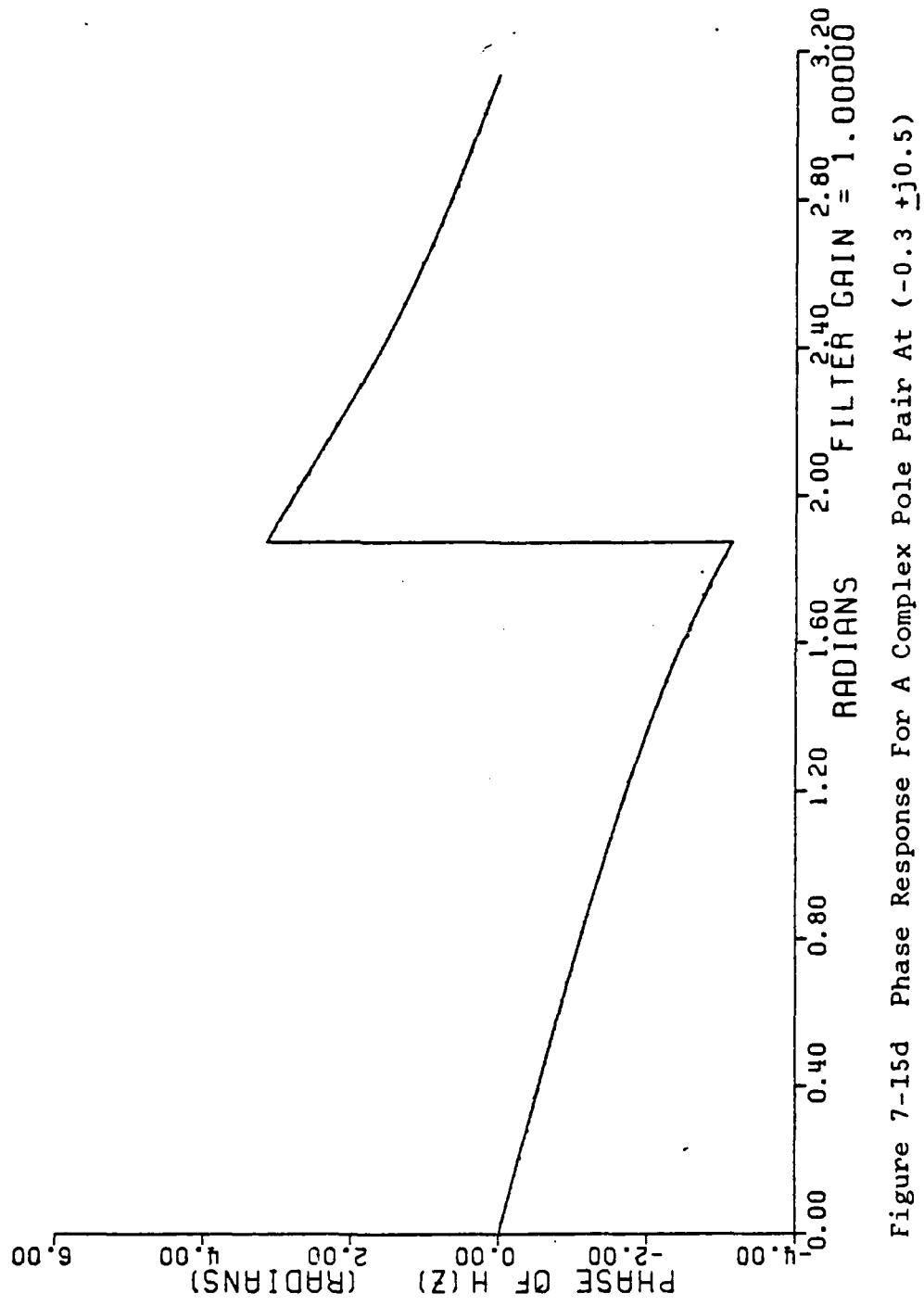


Figure 7-15d Phase Response For A Complex Pole Pair At (-0.3 ±j0.5)

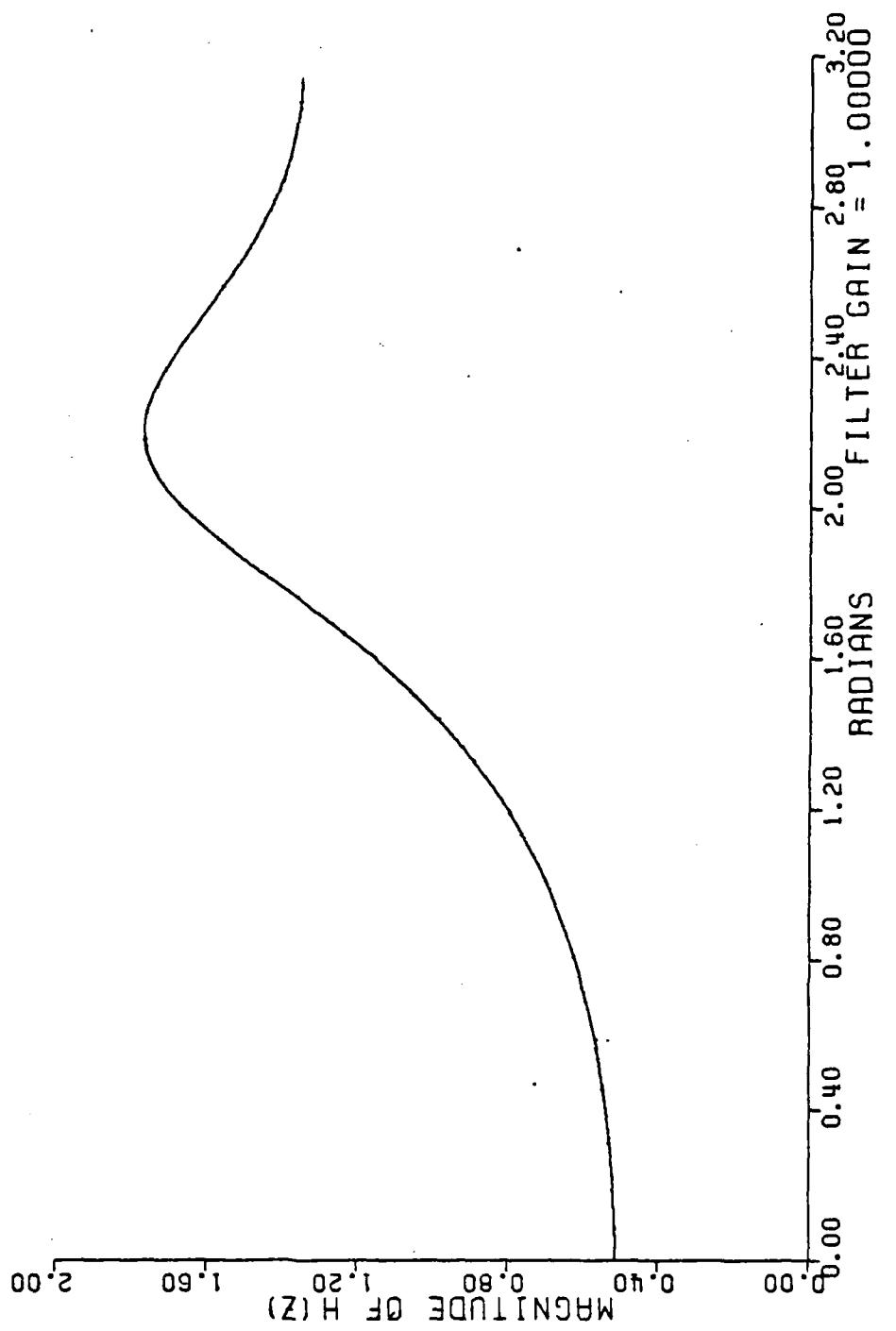


Figure 7-15e Magnitude Of  $H(z)$  For A Complex Pole Pair At  $(-0.3 \pm j0.5)$

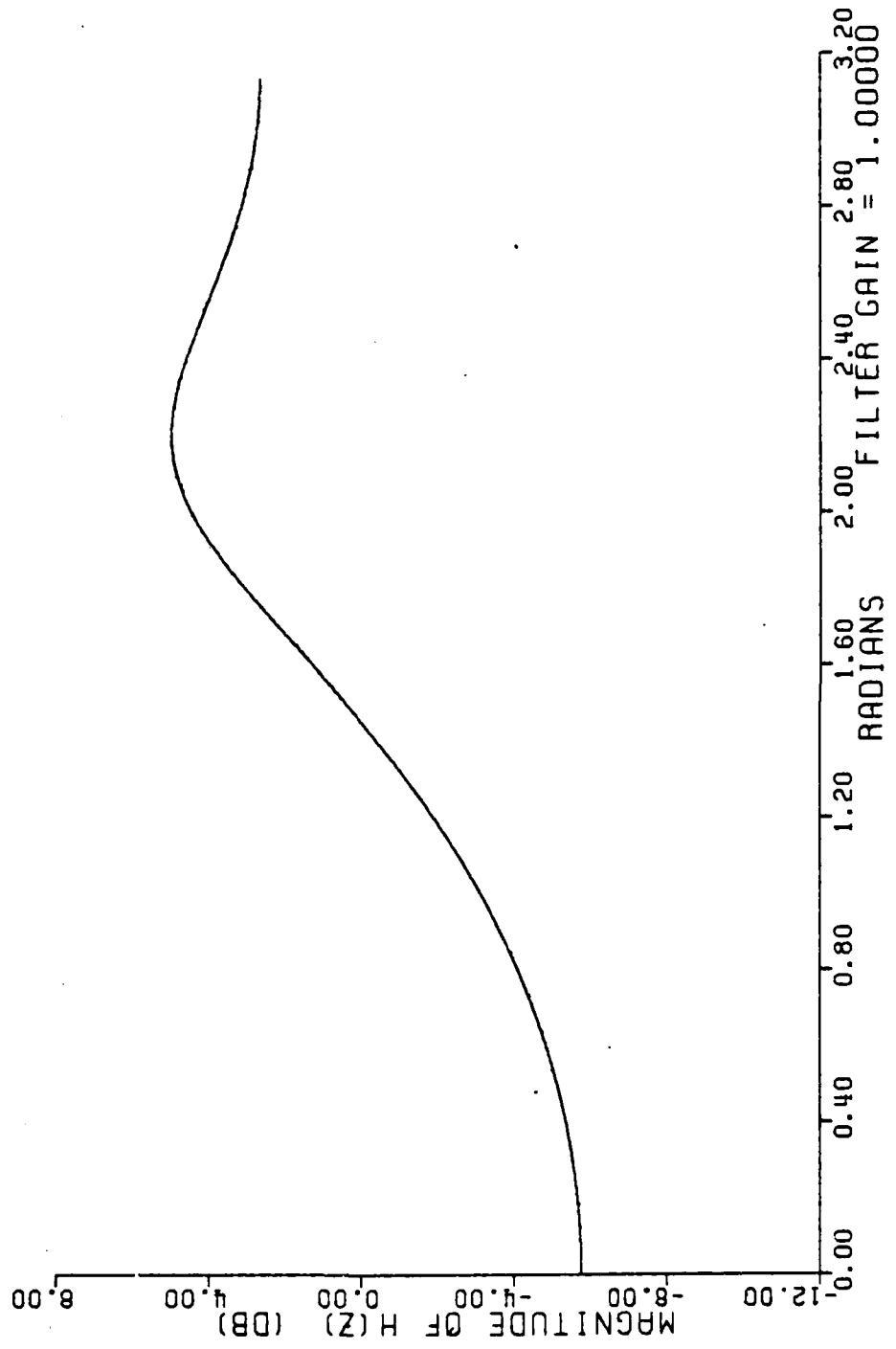


Figure 7-15f Magnitude Of (Hz) In Decibels For A Complex Pole Pair At (-0.3 ±j0.5)

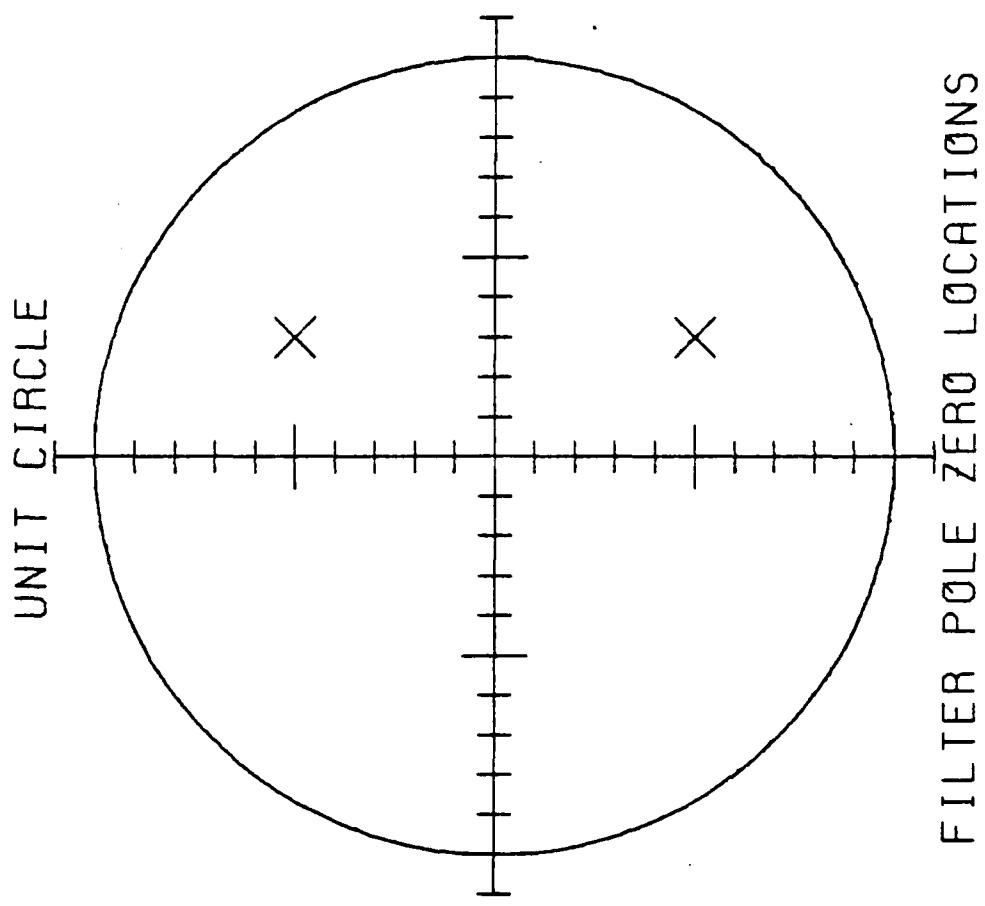


Figure 7-16a Example Of A Complex Pole Pair At  $(0.3 + j0.5)$

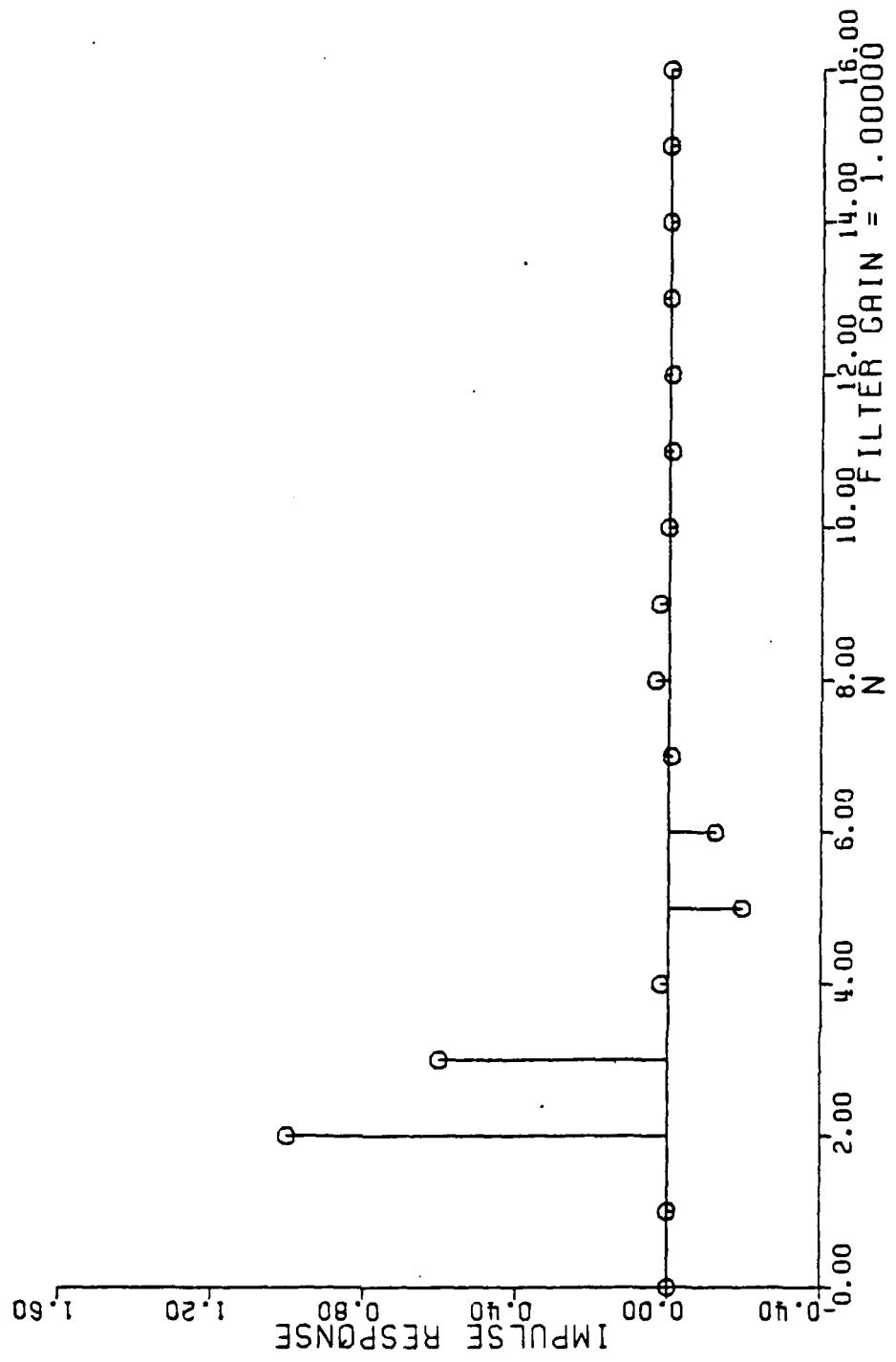


Figure 7-16b Unit Sample Response For A Complex Pole Pair At  $(0.3 + j0.5)$

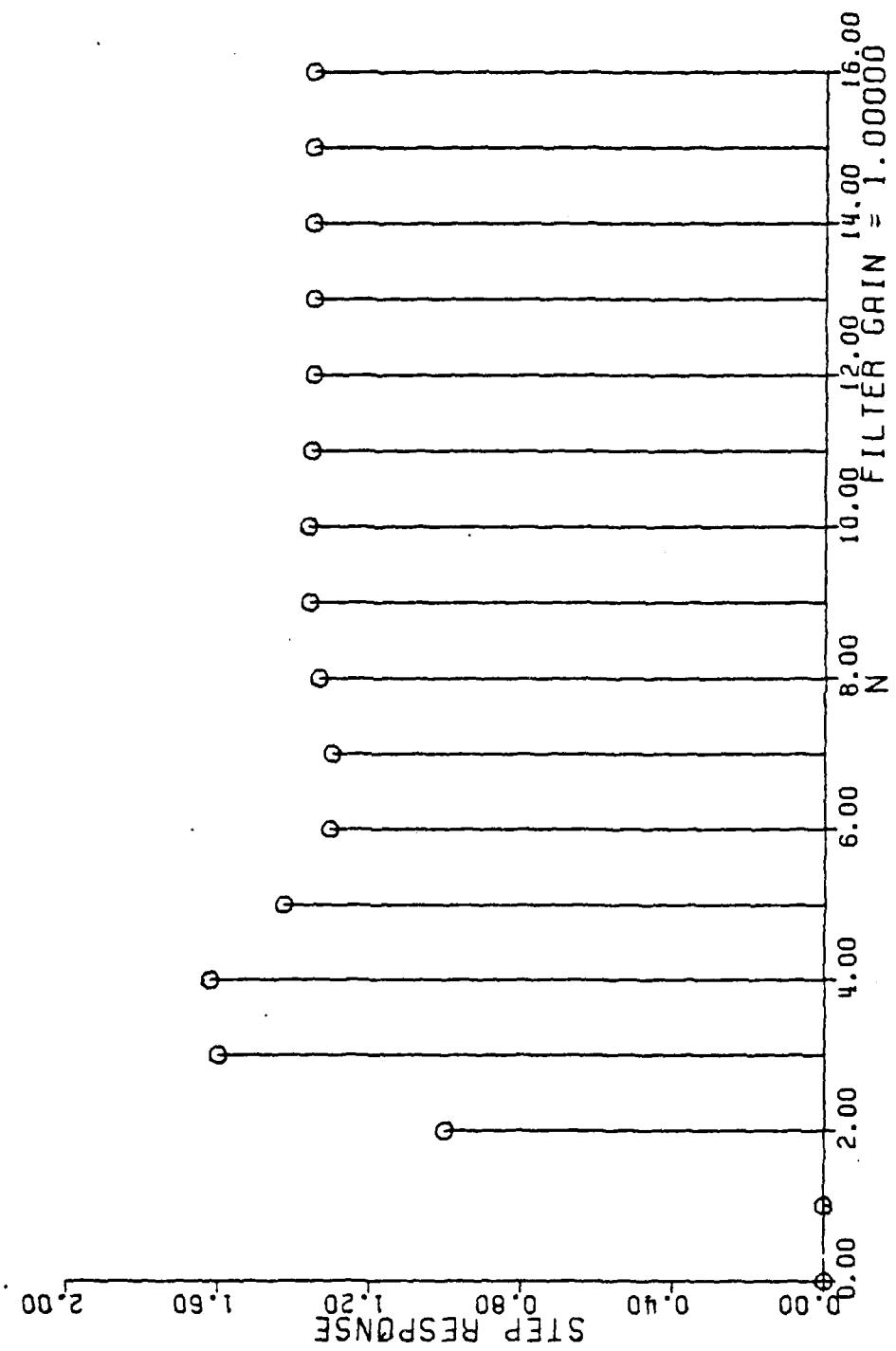


Figure 7-16c Unit Step Response For A Complex Pole Pair At  $(-0.3 \pm j0.5)$

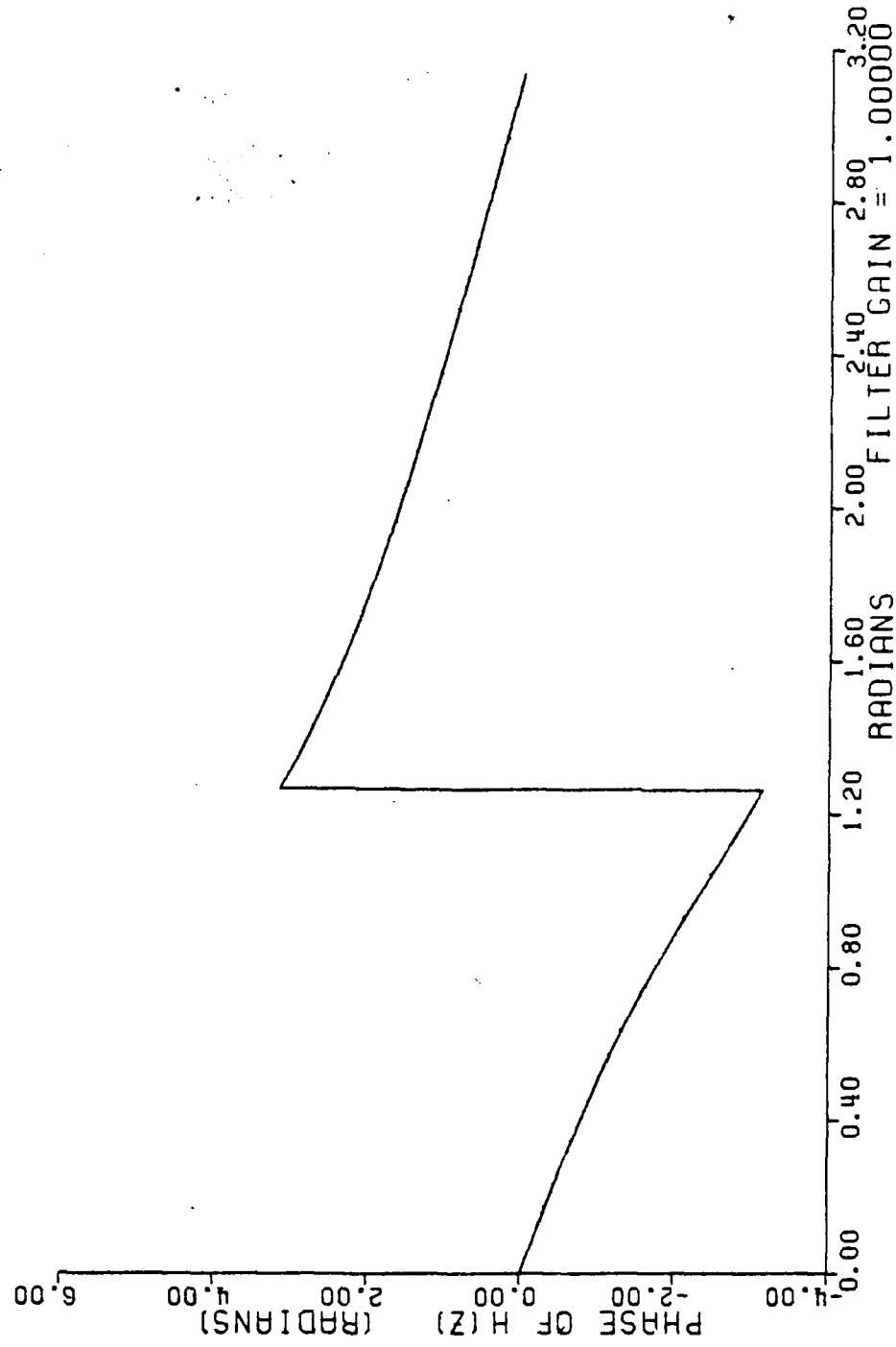


Figure 7-16d Phase Response For A Complex Pole Pair At  $(0.3 + j0.5)$

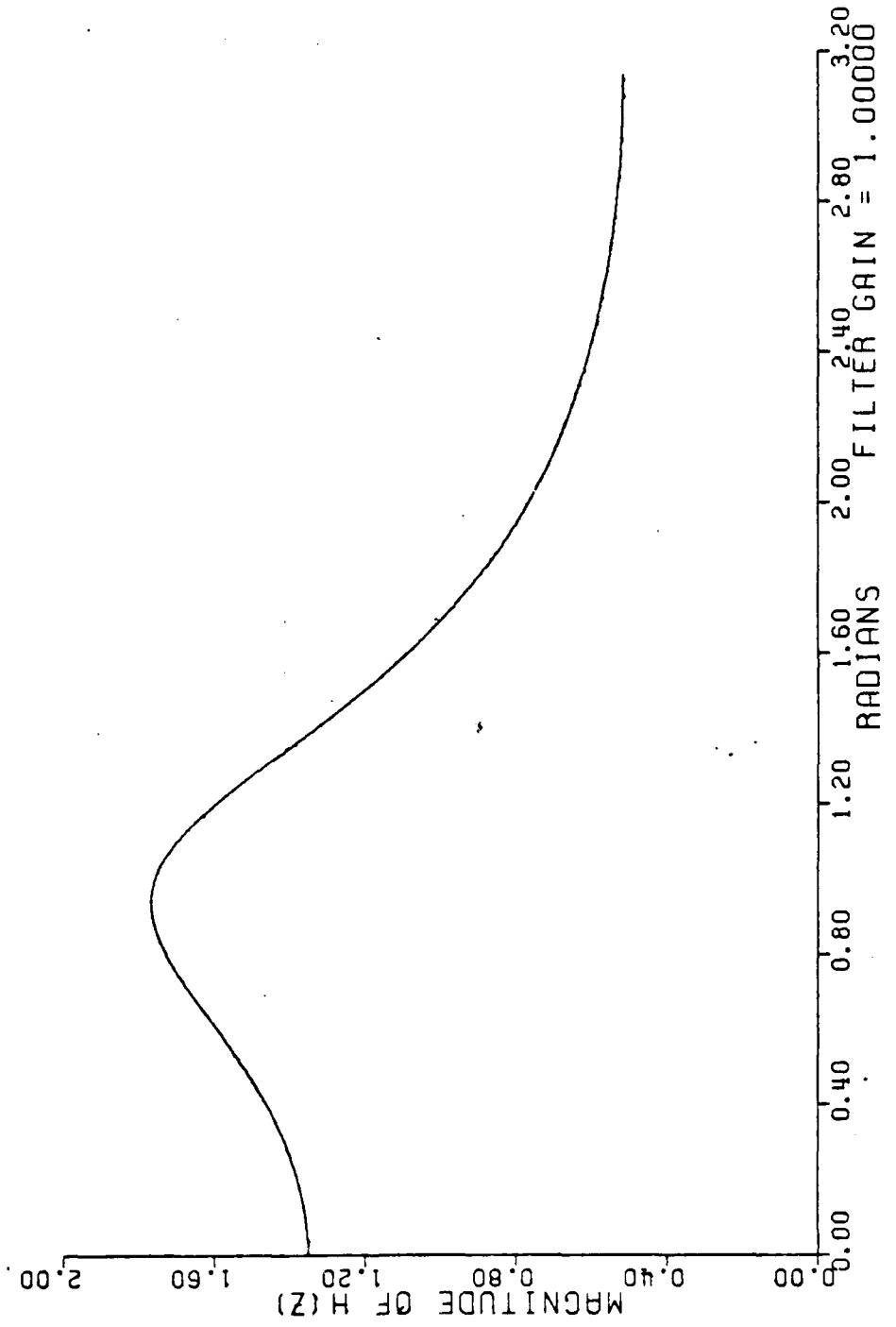


Figure 7-16e Magnitude Of  $H(z)$  For A Complex Pole Pair At  $(0.3 + j0.5)$

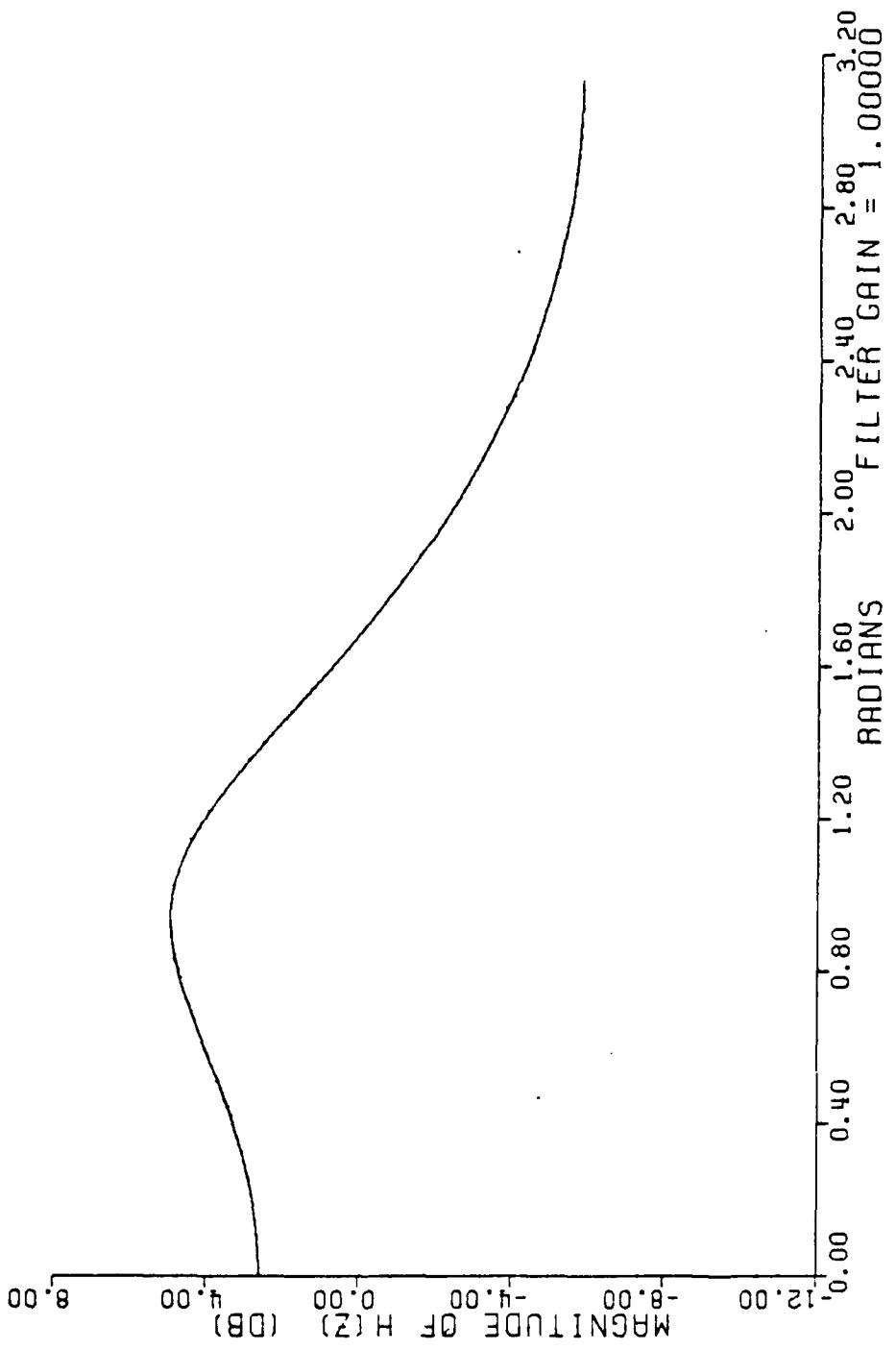


Figure 7-16f Magnitude Of  $H(z)$  In Decibels For A Complex Pole Pair At  $(0.3 + j0.5)$

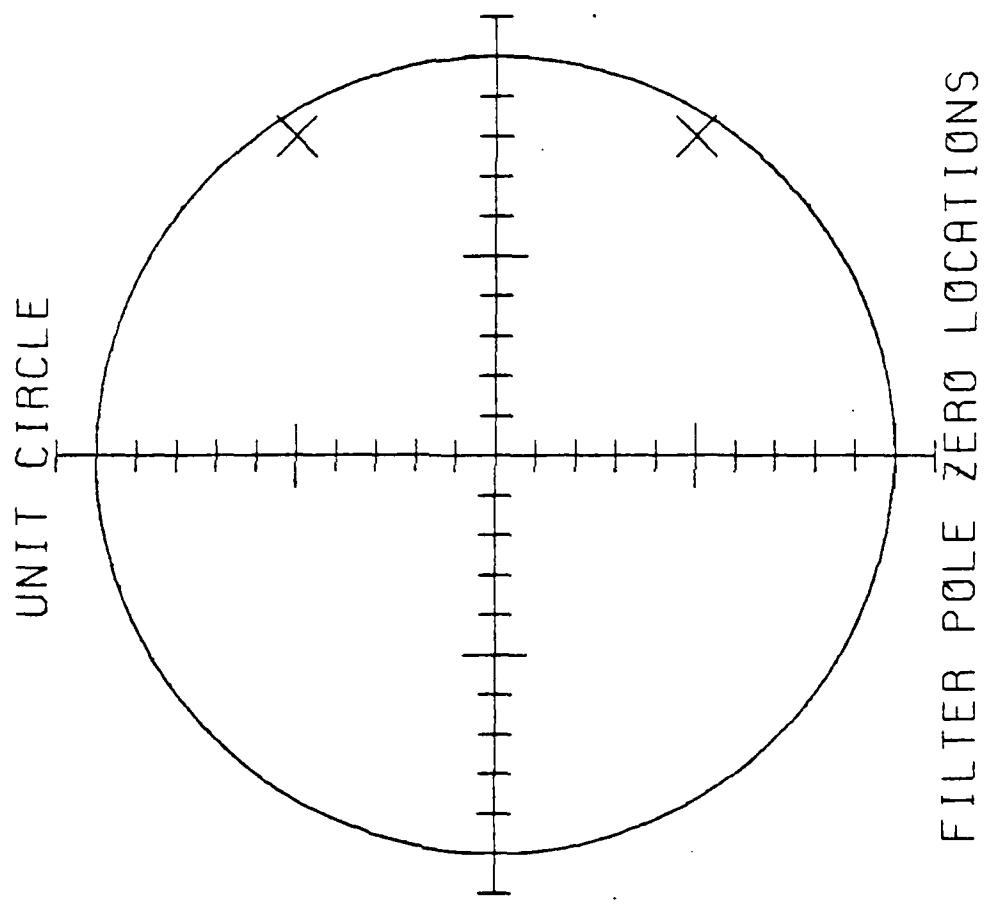


Figure 7-17a Example of A Complex Pole Pair At  $(0.8 \pm j0.5)$

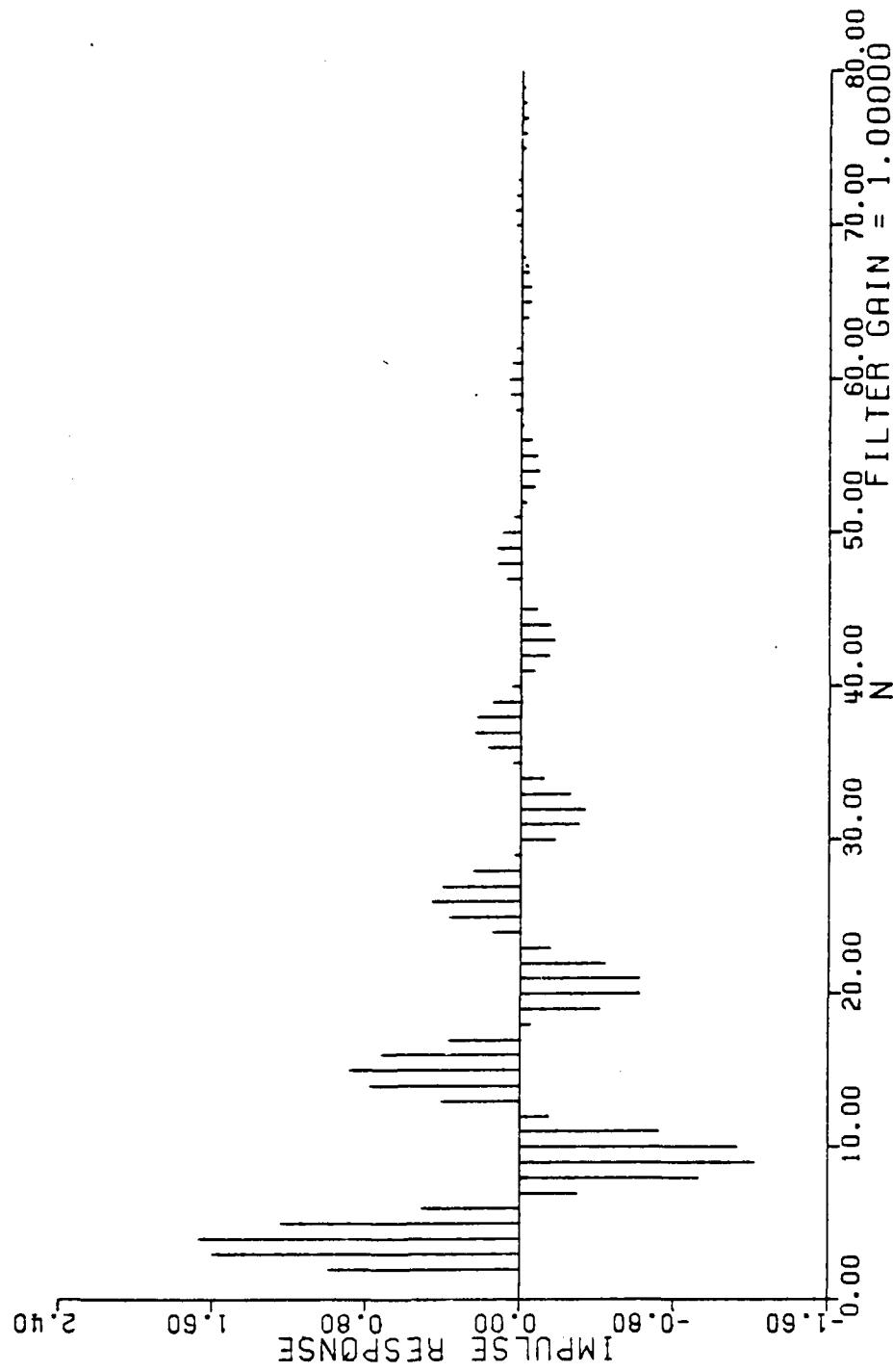


Figure 7-17b Unit Sample Response For A Complex Pole Pair At  $(0.8 \pm j0.5)$

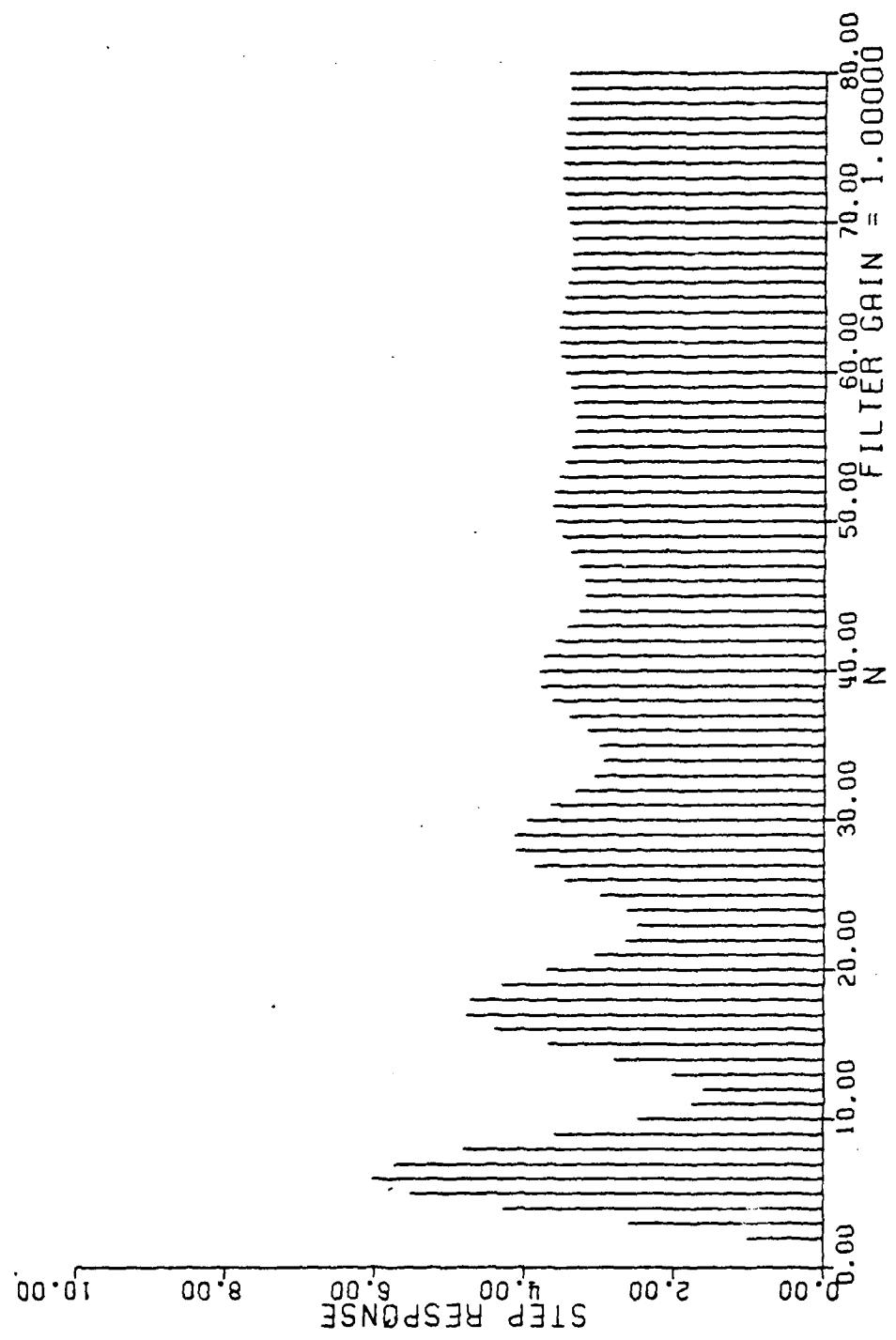


Figure 7-17c Unit Step Response For A Complex Pole Pair At  $(0.8 + j0.5)$

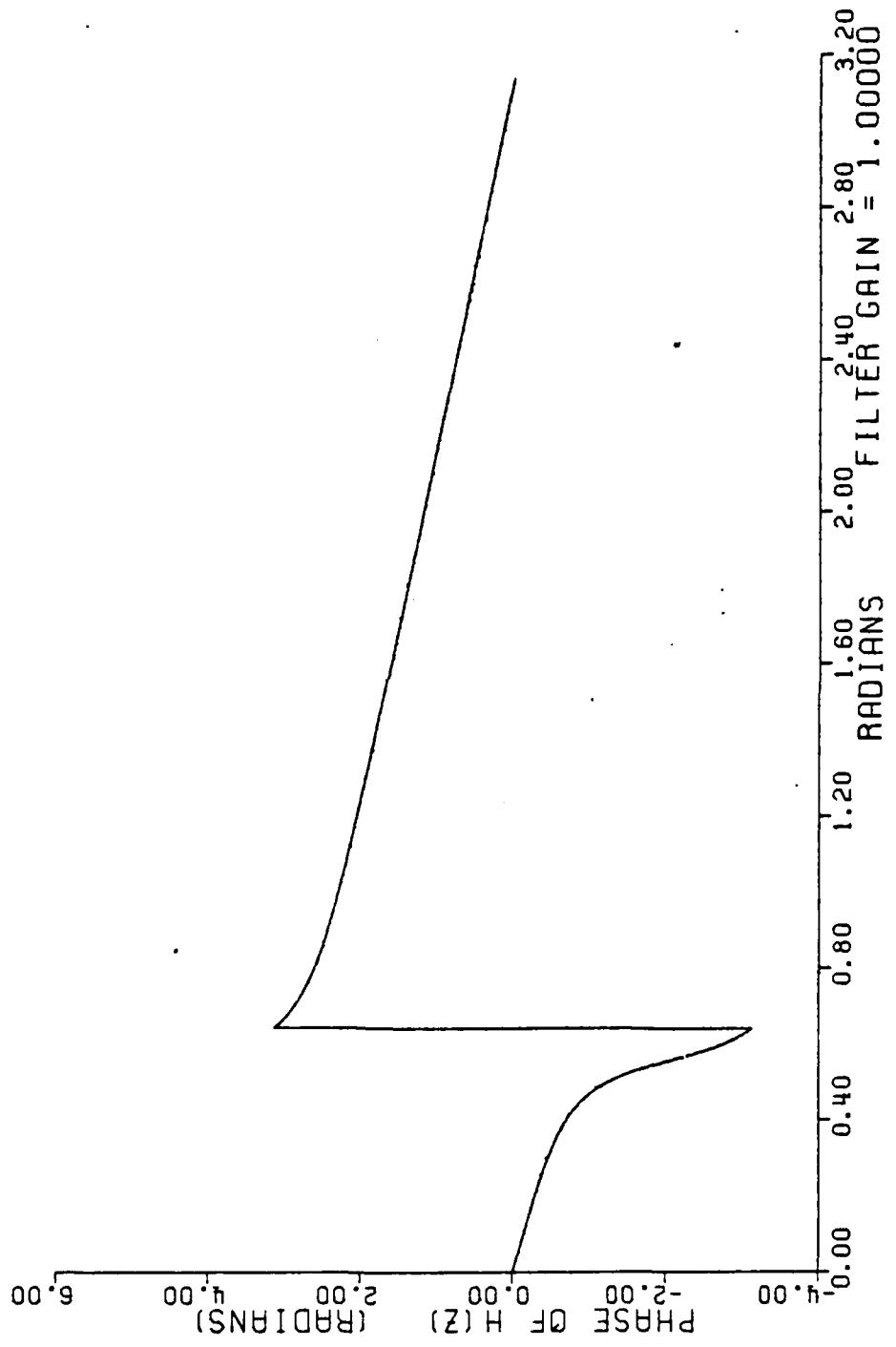


Figure 7-17d Phase Response For A Complex Pole Pair At  $(0.8 + j0.5)$

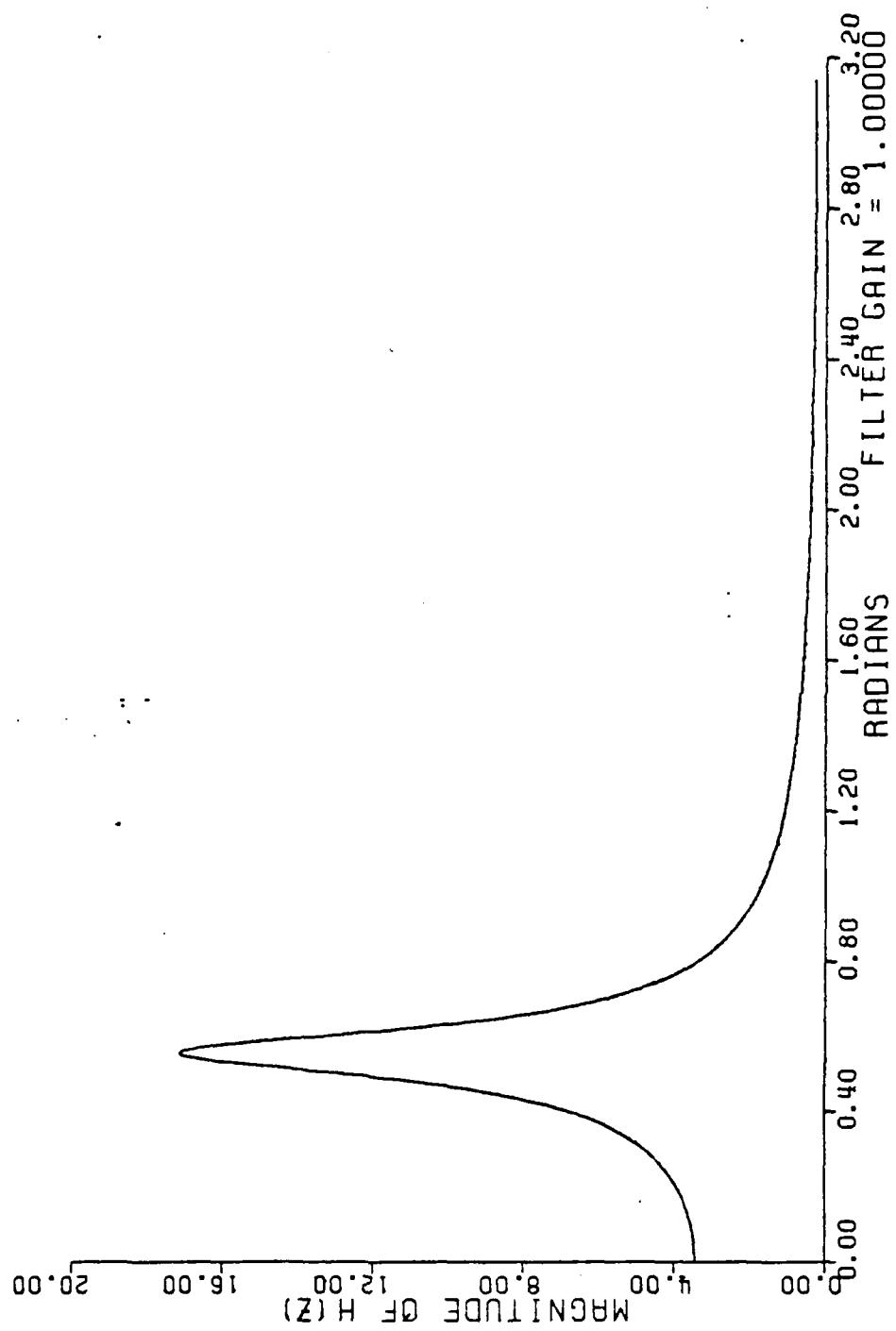


Figure 7-17e Magnitude Of  $H(z)$  For A Complex Pole Pair At  $(0.8 + j0.5)$

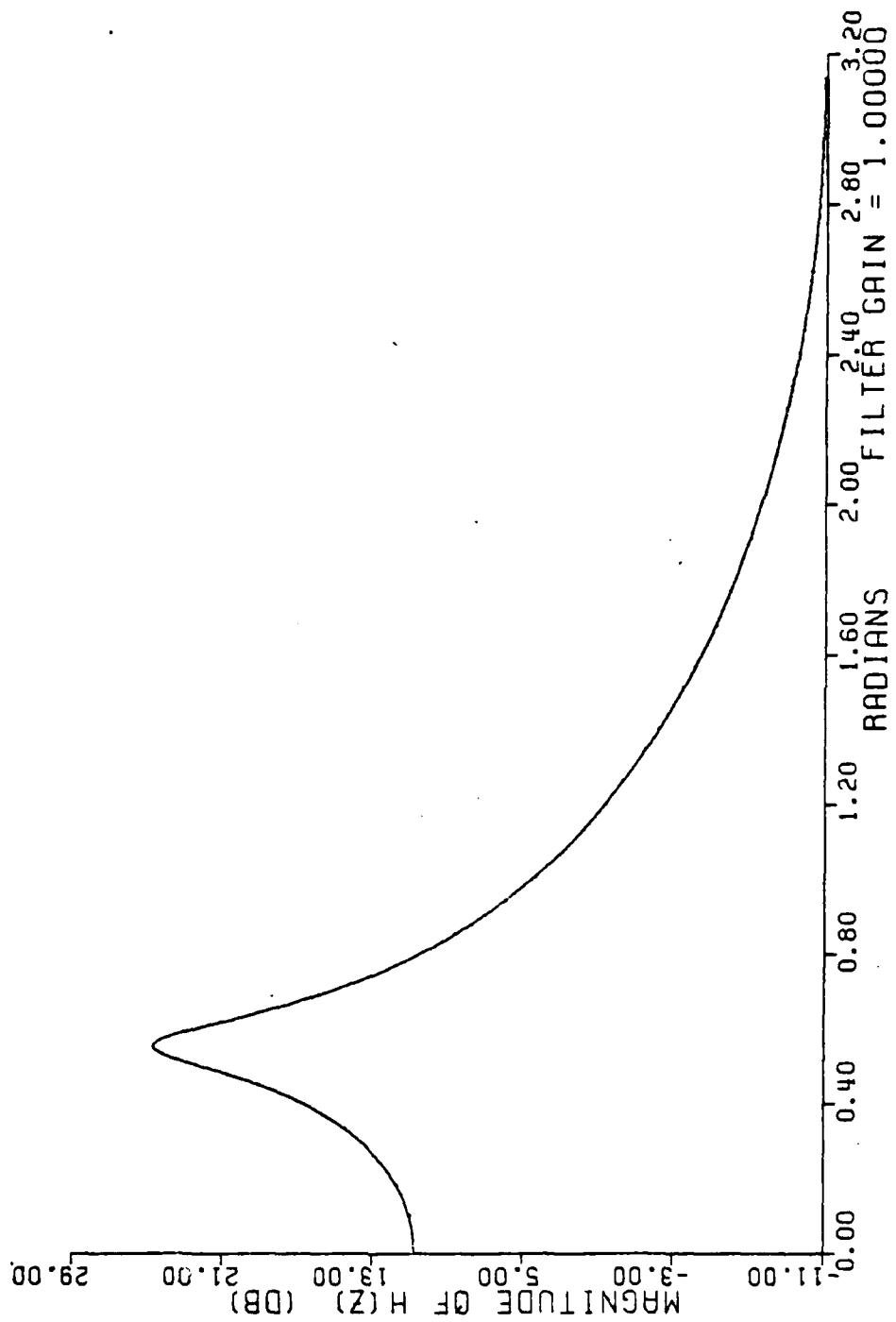


Figure 7-17f Magnitude Of  $H(z)$  In Decibels For A Complex Pole Pair At  $(0.8 + j0.5)$

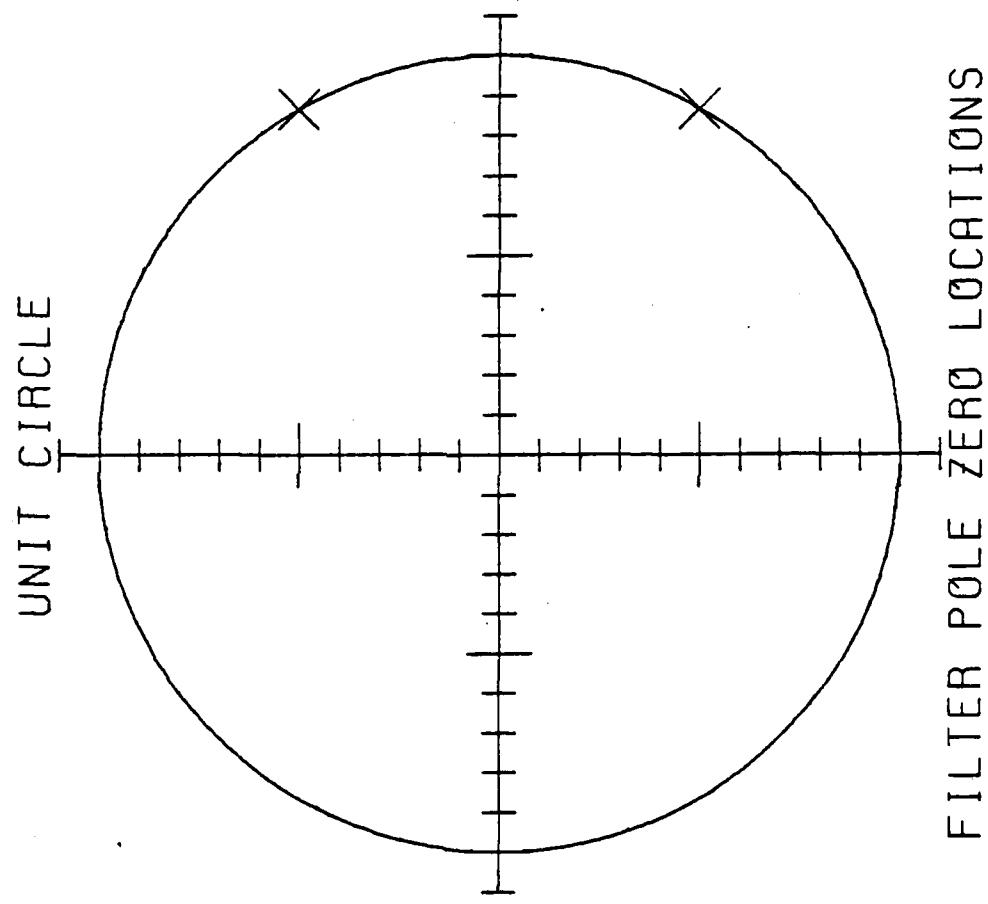


Figure 7.18a Example Of A Complex Pole Pair On The Unit Circle At  $(0.866025 + j0.5)$

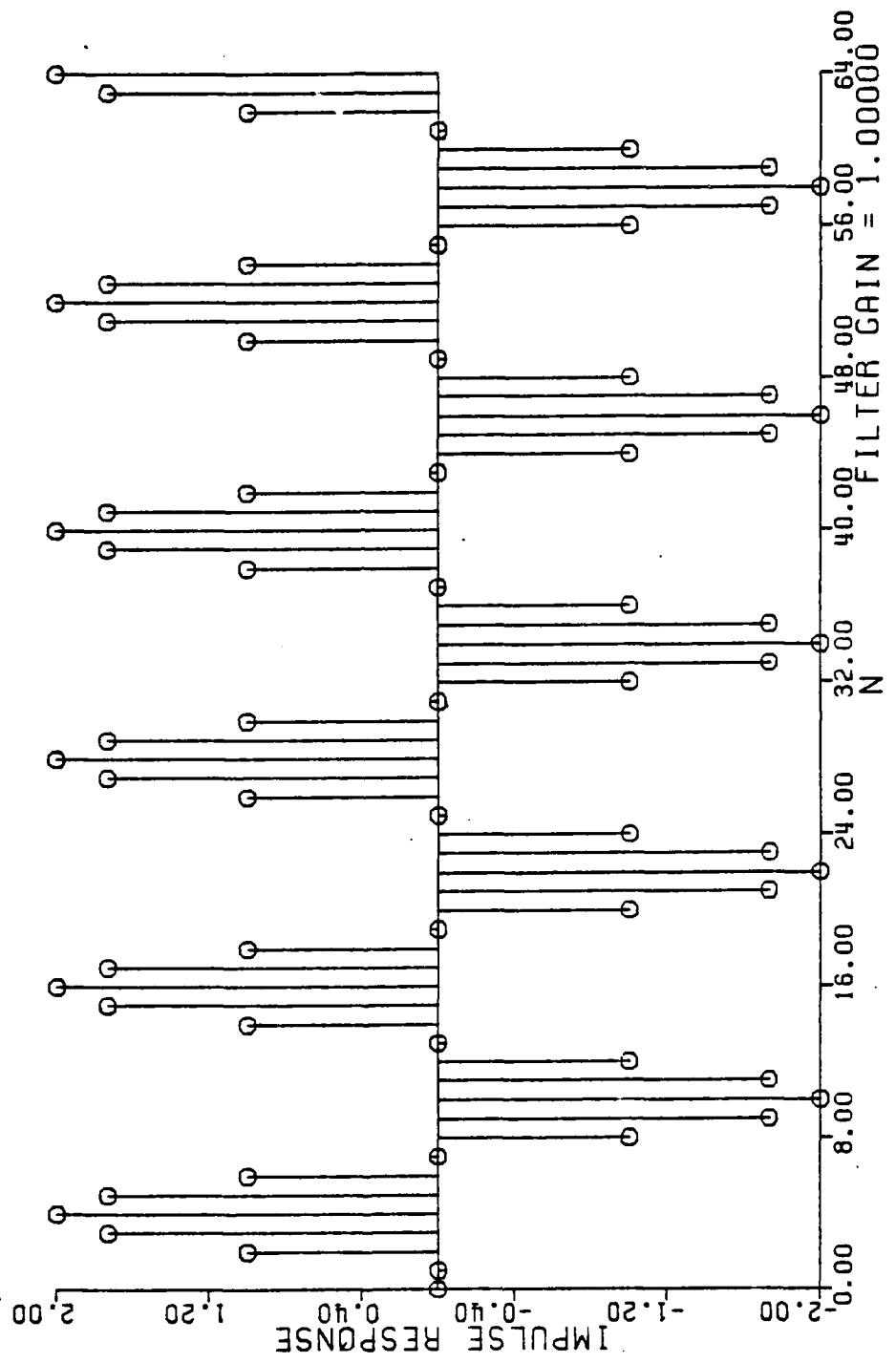


Figure 7-18b Unit Sample Response For A Complex Pole Pair At  $(0.866025 \pm j0.5)$

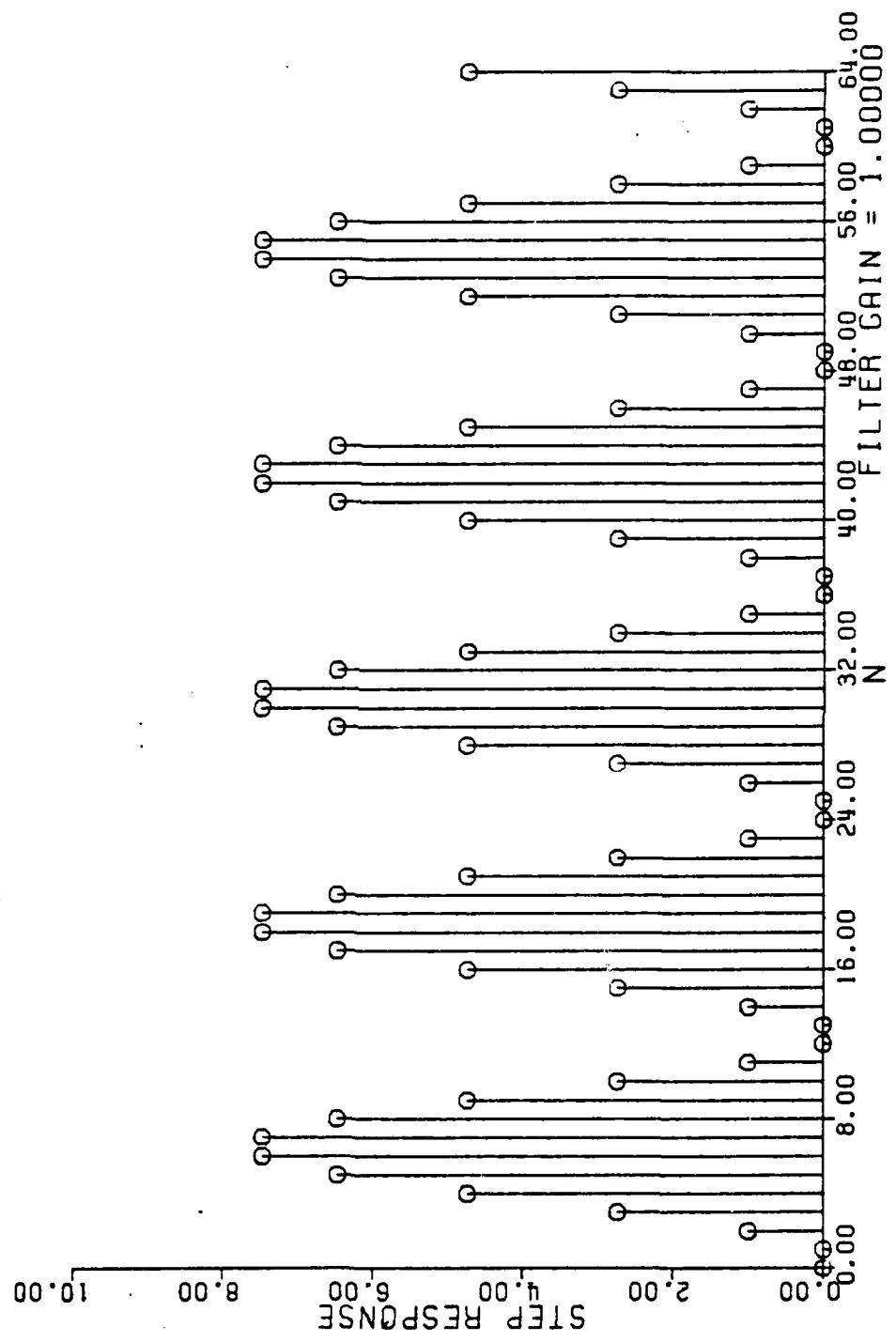


Figure 7-18c Unit Step Response For A Complex Pole Pair At  $(0.866025 \pm j0.5)$

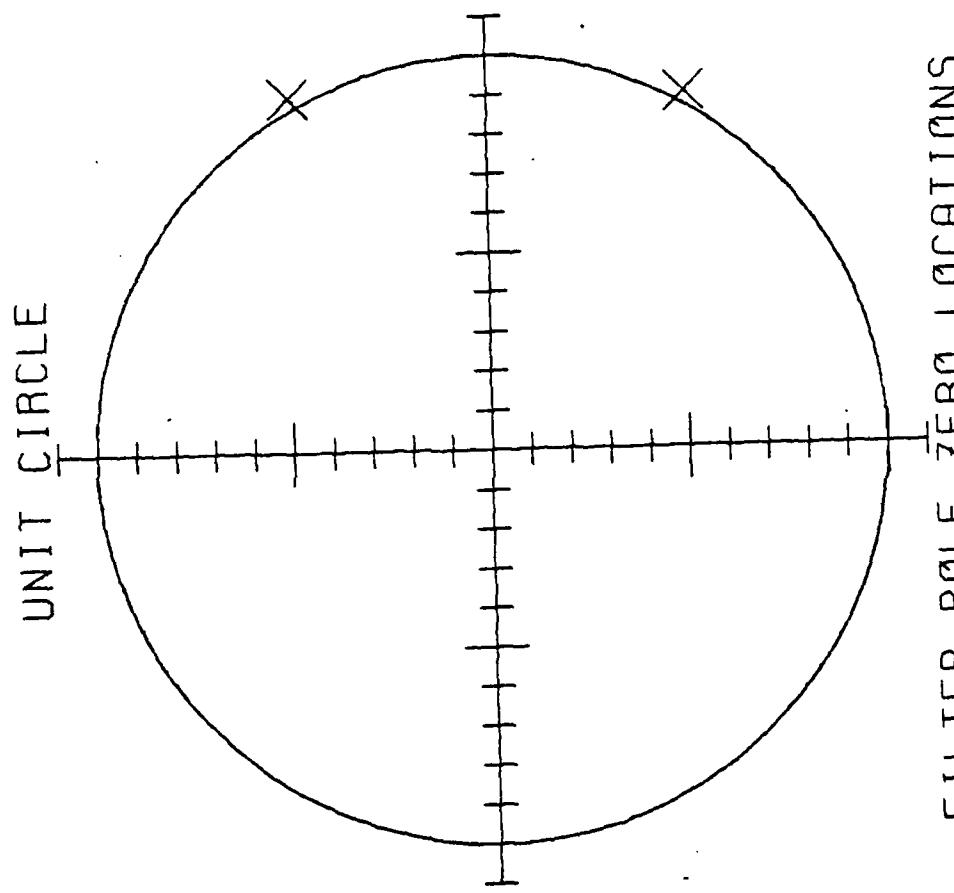


Figure 7-19a Example of A Complex Pole Pair Outside The Unit Circle At  $(0.9 + j0.5)$

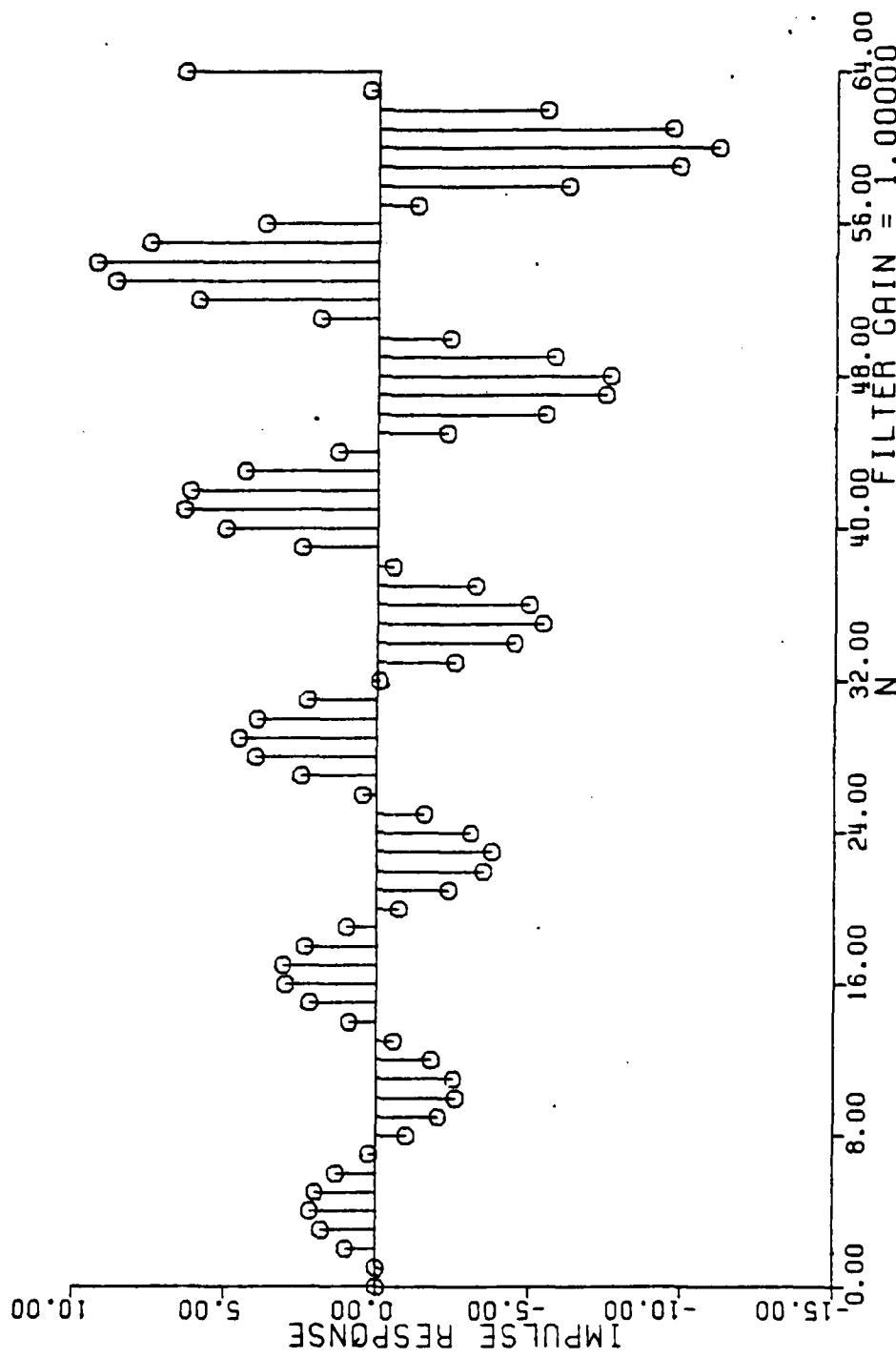


Figure 7-19b Unit Sample Response For A Complex Pole Pair At  $(0.9 + j0.5)$

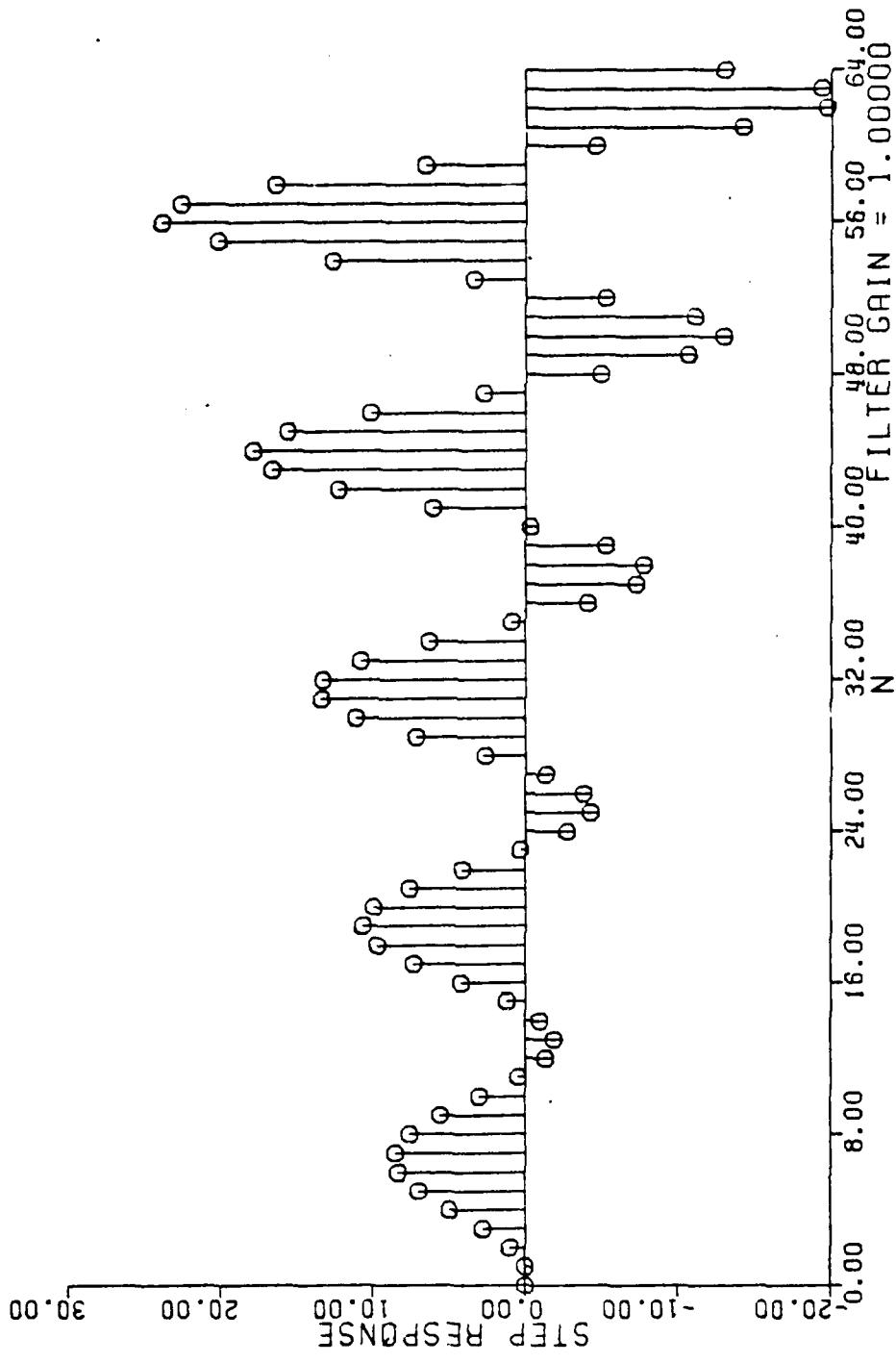


Figure 7-19c Unit Step Response For A Complex Pole Pair At  $(0.9 + j0.5)$

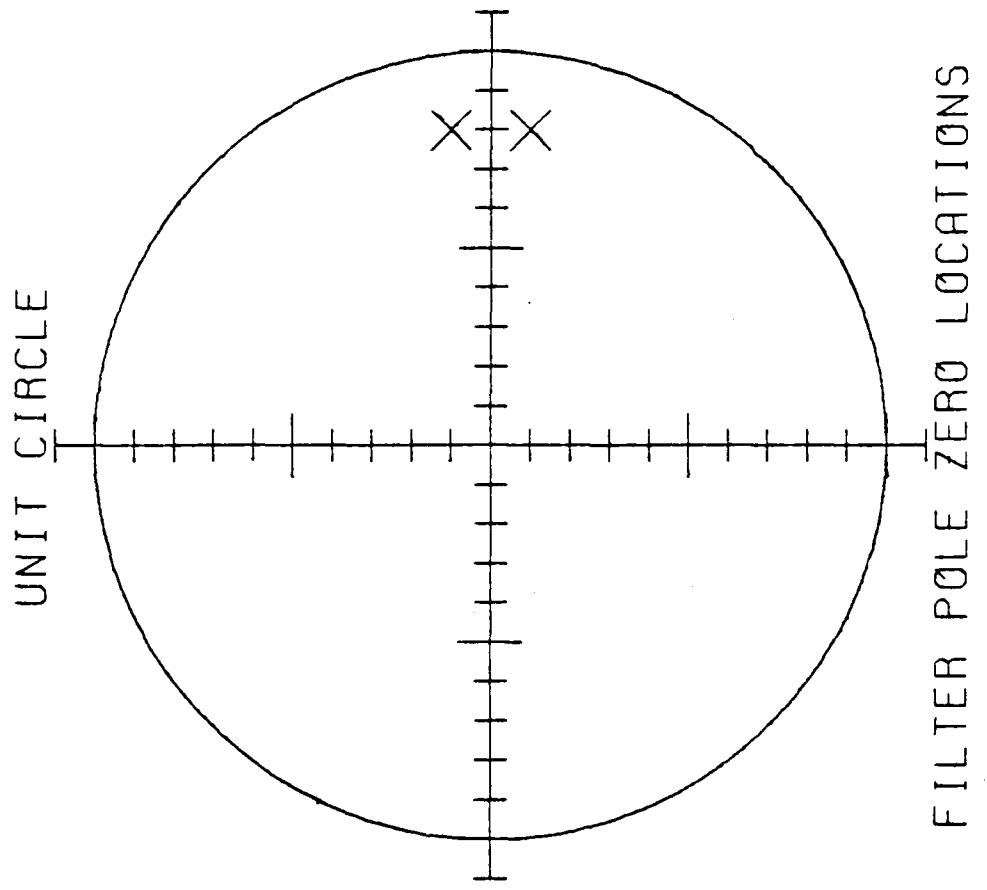


Figure 7-20a Example of A complex Pole pair At  $(0.8 \pm j0.1)$

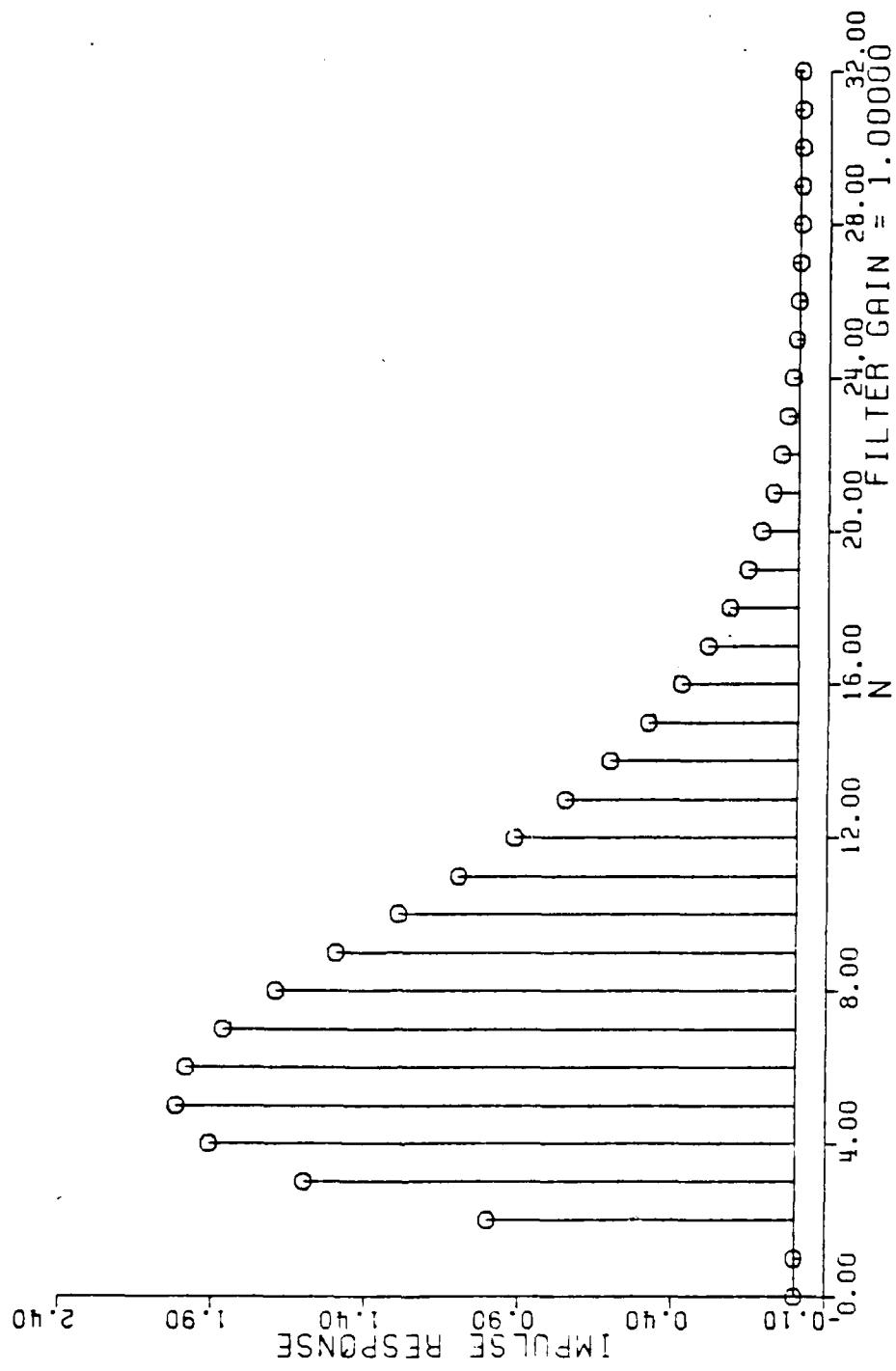


Figure 7-20b Unit Sample Response Of A Complex Pole Pair At  $(0.8 + j0.1)$

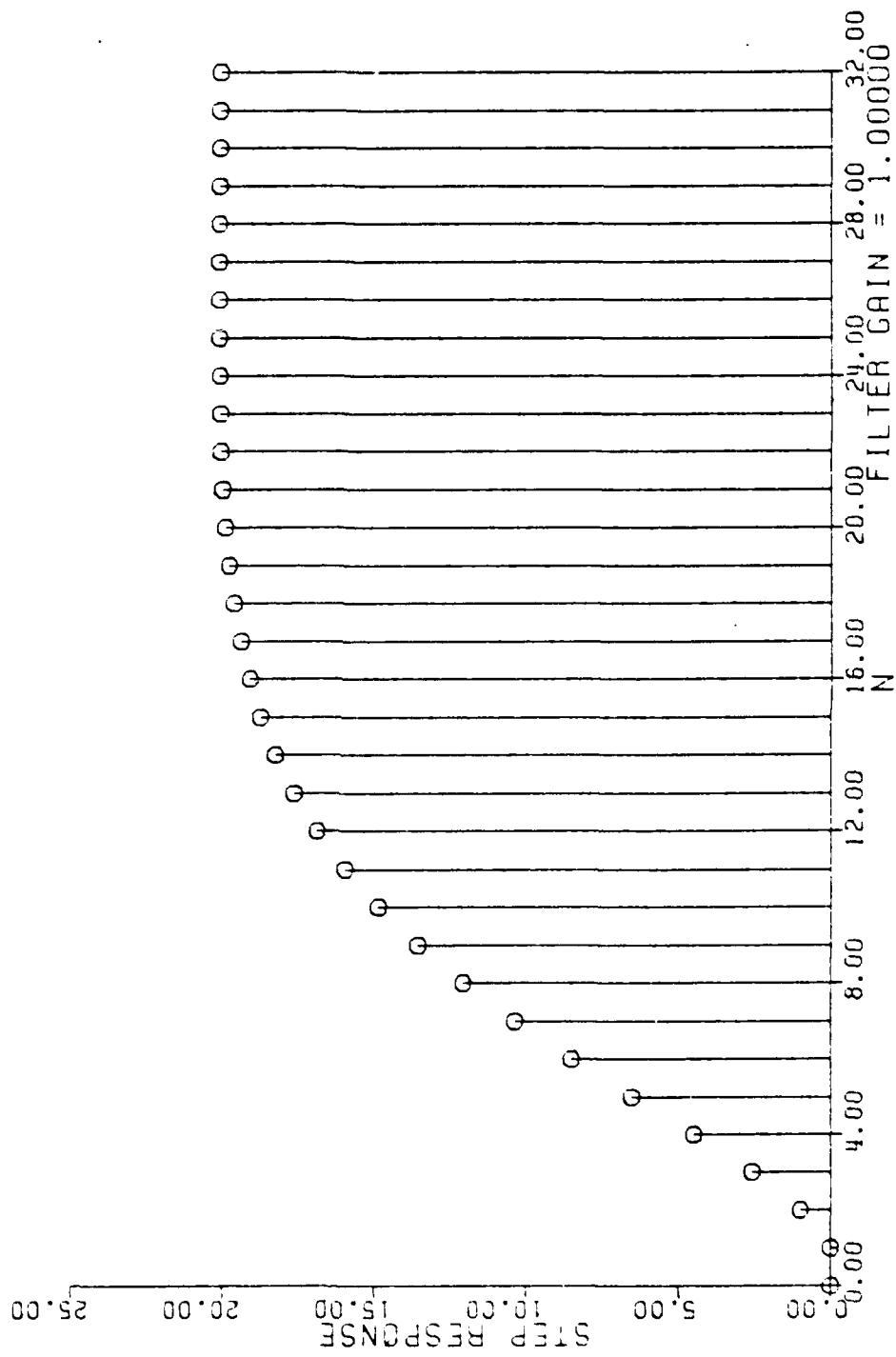


Figure 7-26c Unit Step Response For A Complex Pole Pair At  $(0.8 + j0.1)$

AD-A093 252

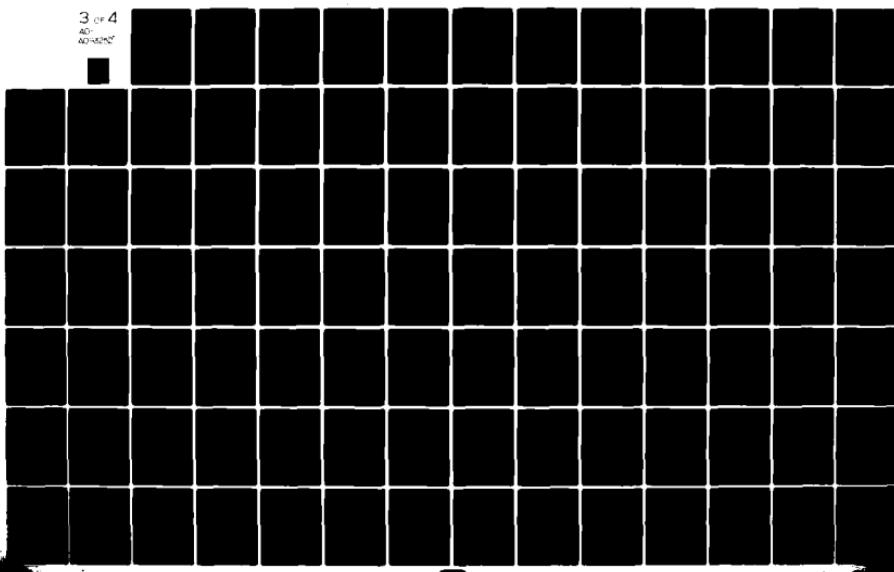
NAVAL POSTGRADUATE SCHOOL MONTEREY CA  
ADVANCED SIMULATION OF DIGITAL FILTERS. (U)  
SEP 80 G S DOYLE

F/6 9/3

UNCLASSIFIED

NL

3 OF 4  
AD-A093 252



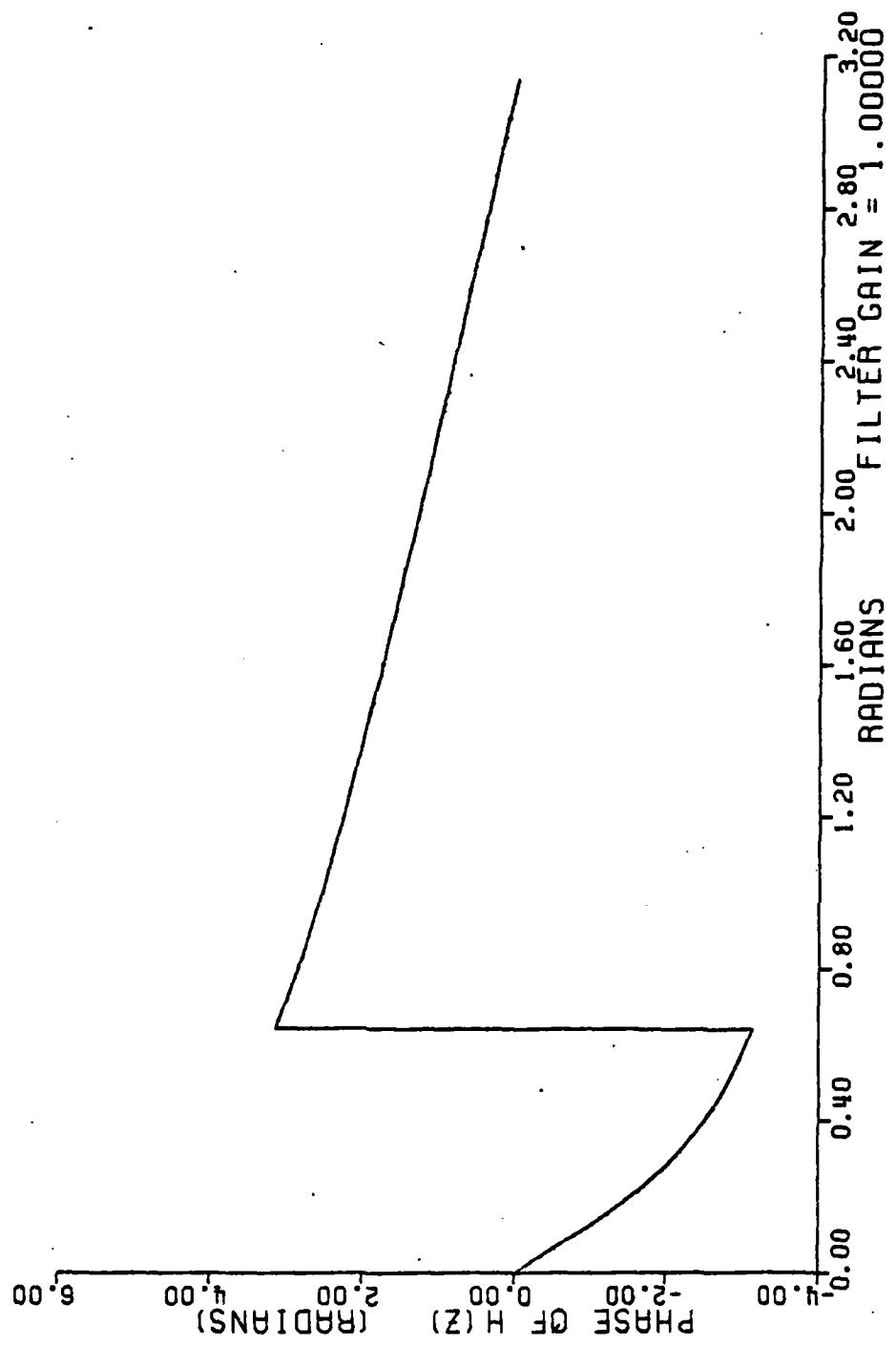


Figure 7-20d Phase Response For A Complex Pole Pair At  $(0.8 \pm j0.1)$

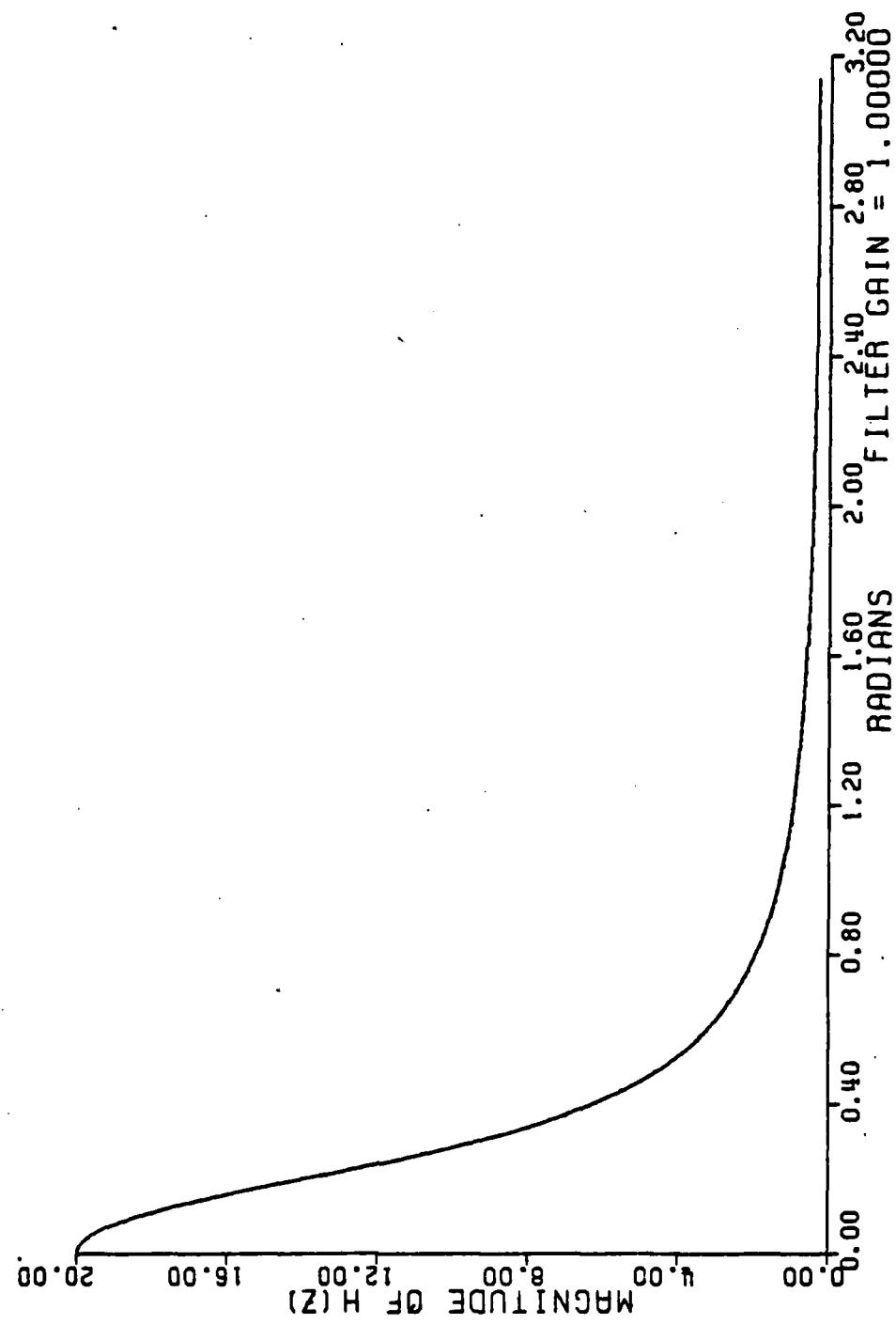


Figure 7-20e Magnitude Of  $H(z)$  For A Complex Pole Pair At  $(0.8 + j0.1)$

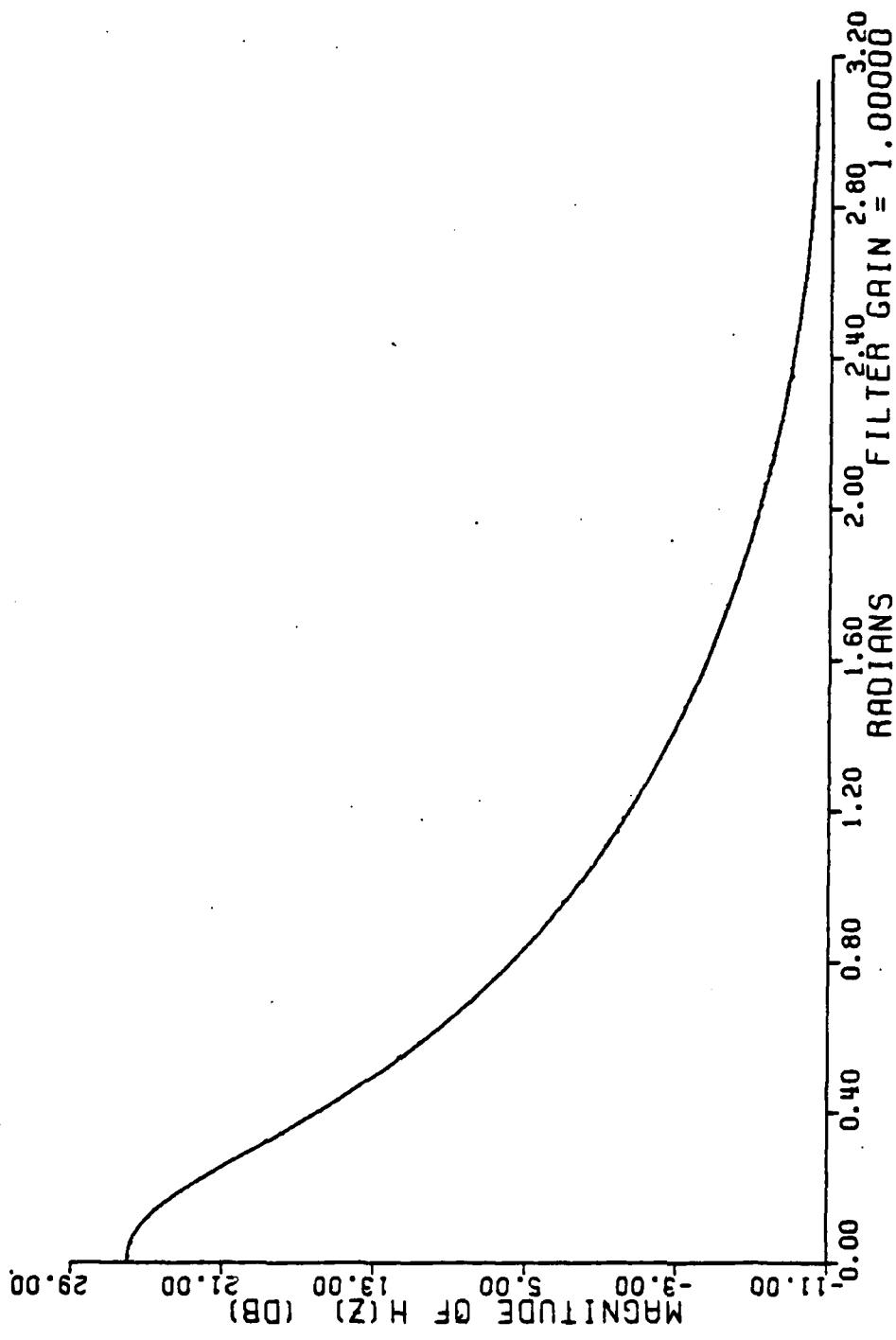
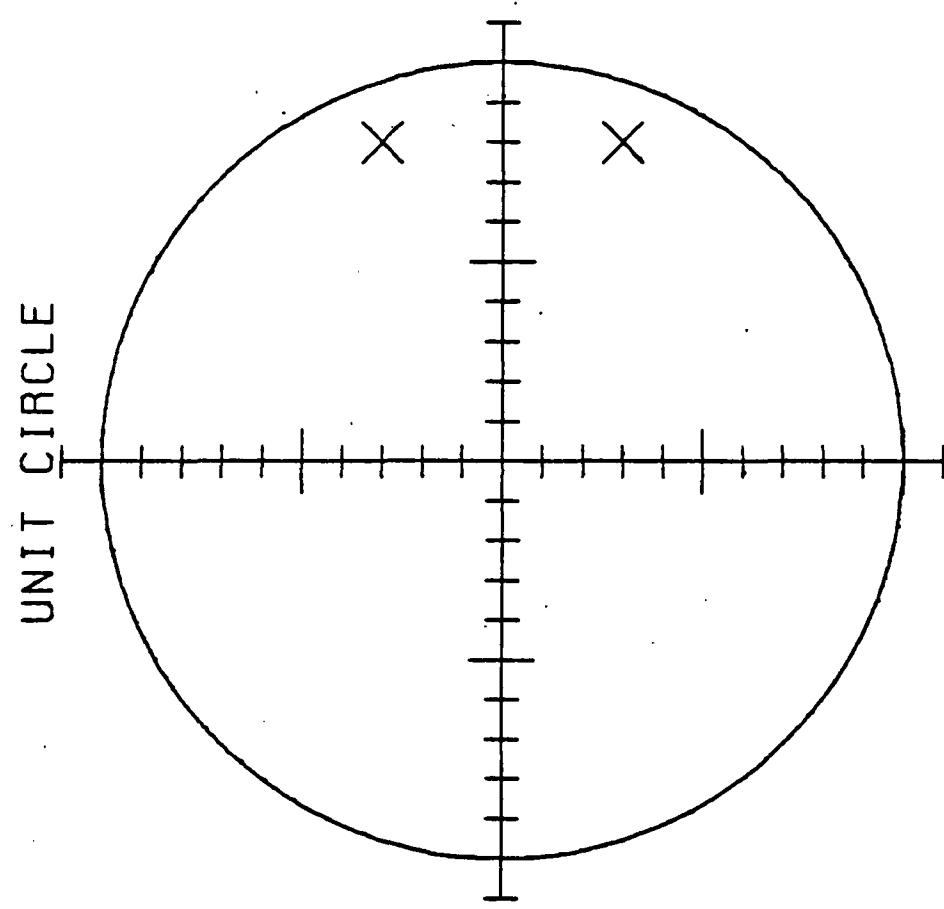


Figure 7-20f Magnitude Of  $H(z)$  In Decibels For A Complex Pole Pair At  $(0.8 \pm j0.1)$



FILTER POLE ZERO LOCATIONS  
Figure 7-21a Example Of A Complex Pole Pair At  $(0.8 + j0.3)$

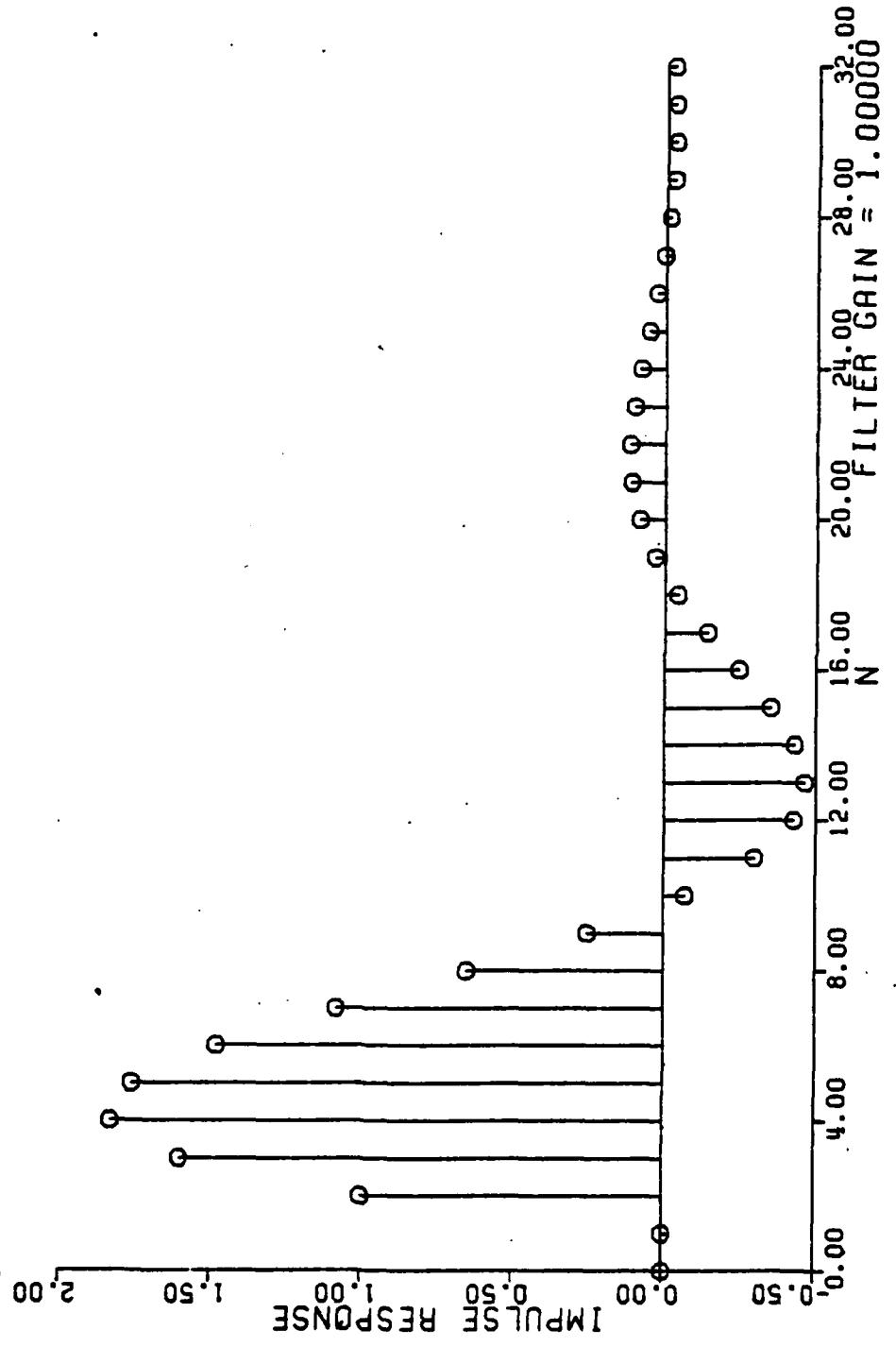


Figure 7-21b Unit Sample Response For A Complex Pole Pair At  $(0.8 + j0.3)$

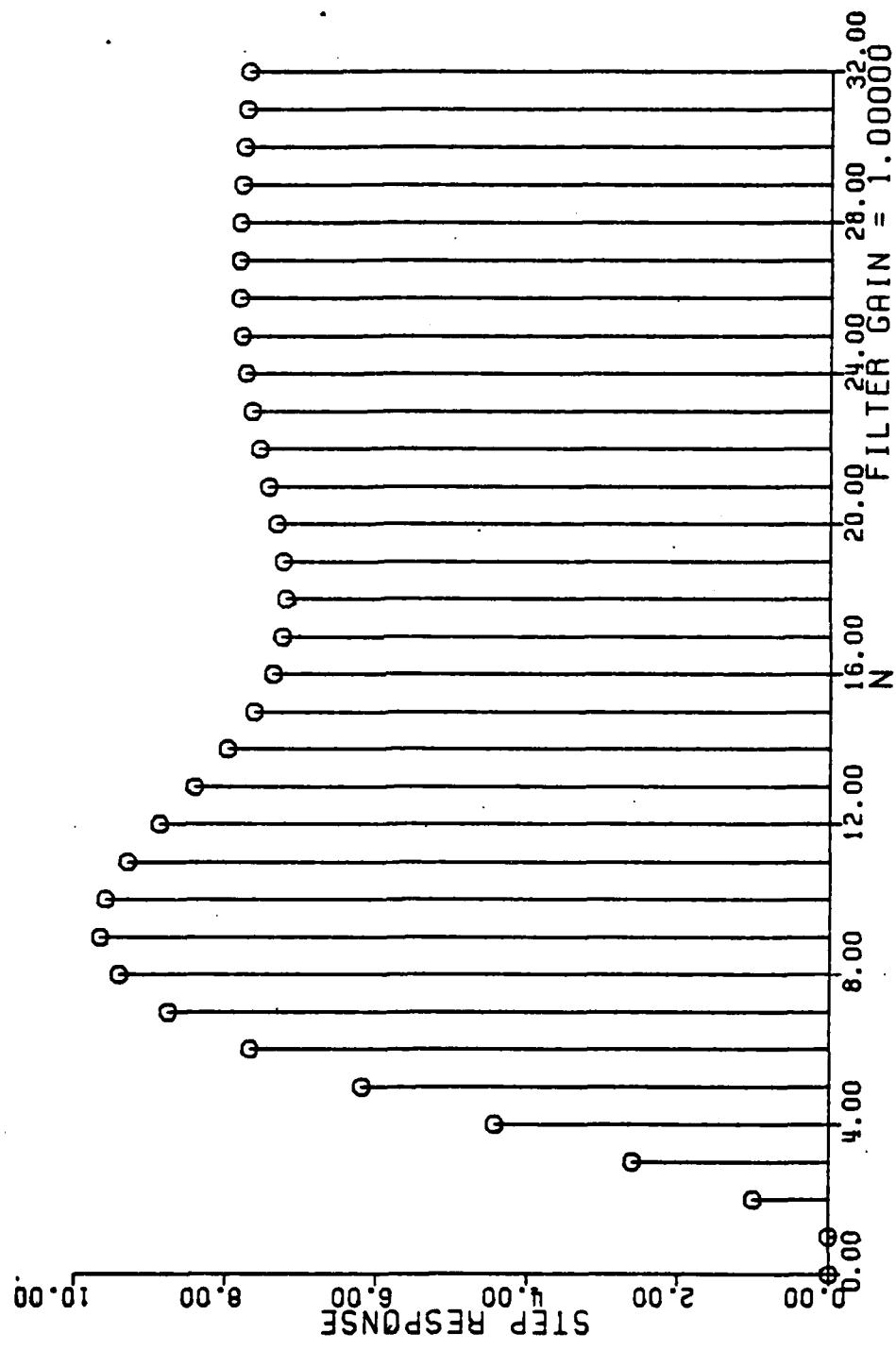


Figure 7-21c Unit Step Response For A Complex Pole Pair At  $(0.8 \pm j0.3)$

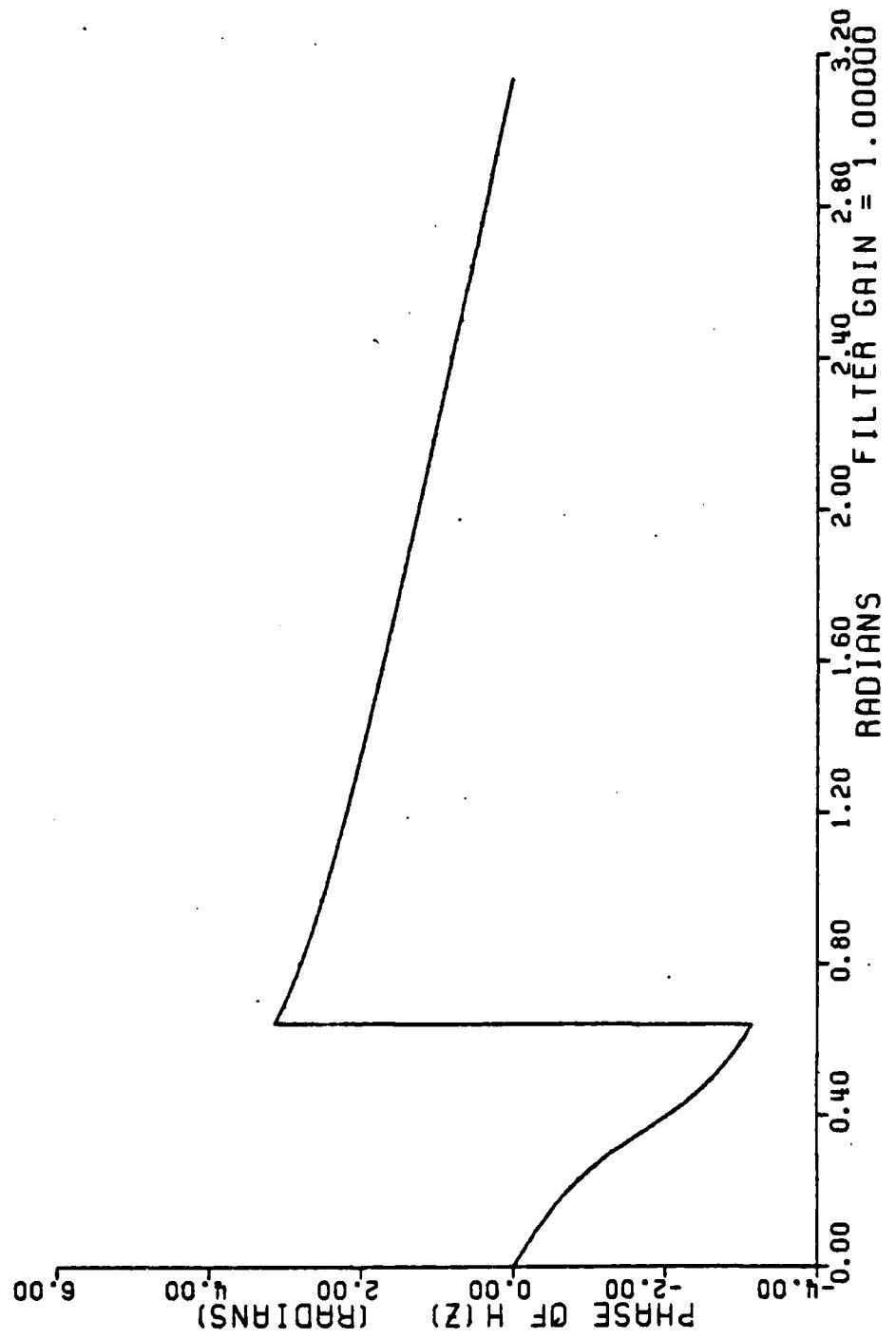


Figure 7-21d Phase Response For A Complex Pole Pair At  $(0.8 \pm j0.3)$

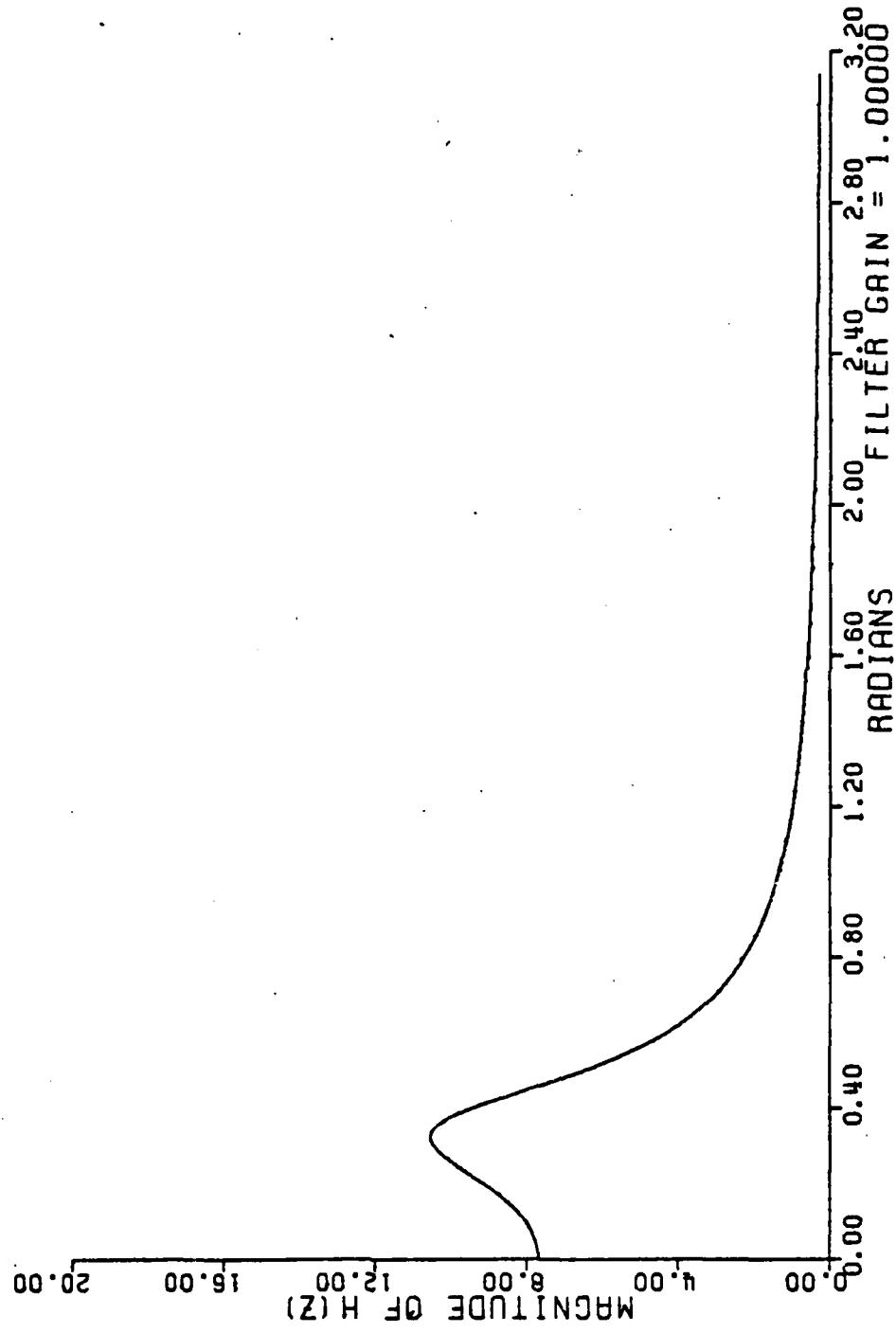


Figure 7-21e Magnitude Of  $H(z)$  For A Complex Pole Pair At  $(0.8 + j0.3)$

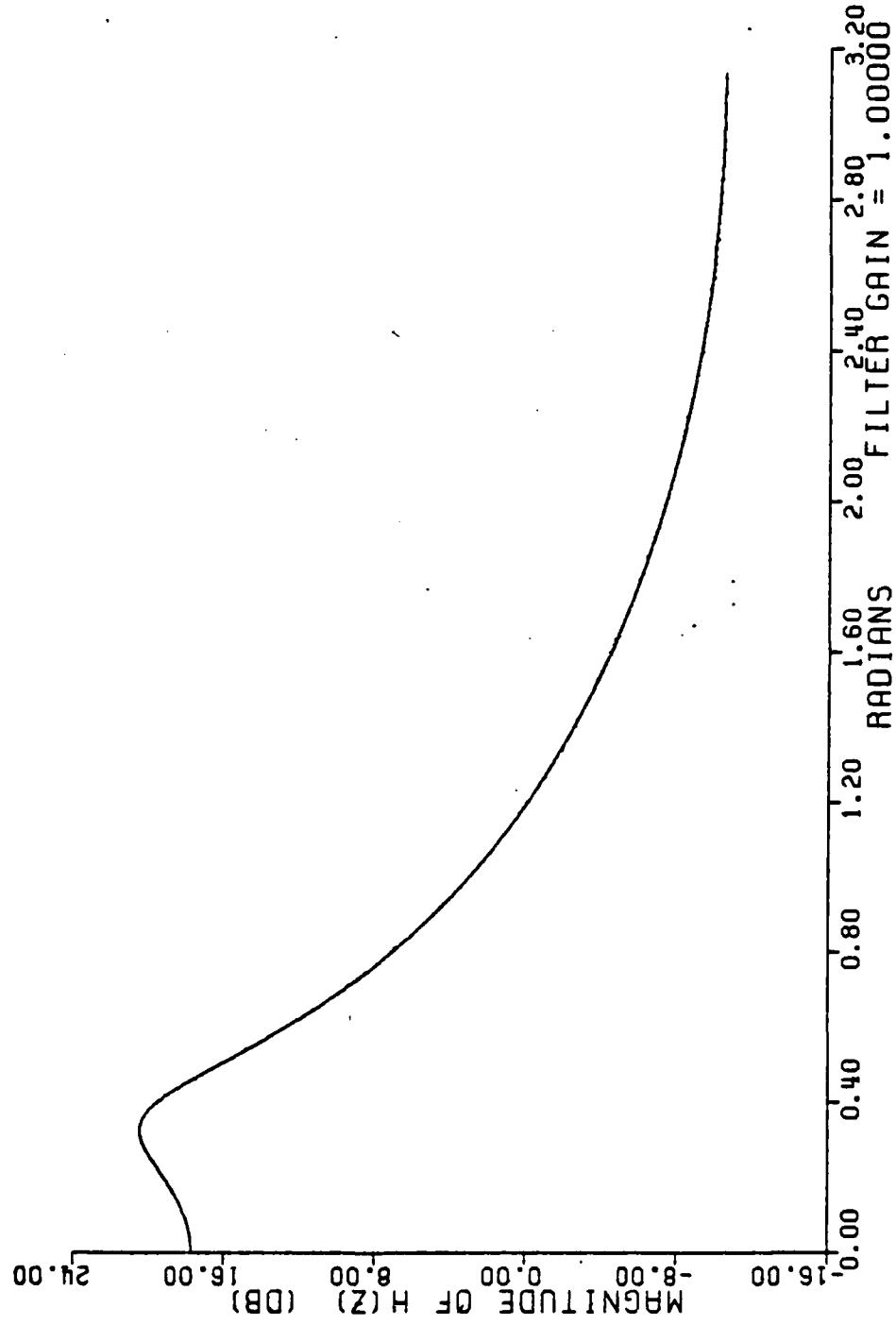


Figure 7-21f Magnitude Of  $H(z)$  In Decibels For a Complex Pole Pair At  $(0.8 + j0.3)$

## VIII. INTERPRETATION OF ASDF OUTPUT

When the user initially confronts the ASDF program it is expected that he will attempt to duplicate some of the examples presented earlier in this thesis or similar examples found in the literature. These types of applications of ASDF are straightforward and the results generated can be compared with published results. Interpretation of the output plots is seldom confusing.

As the user becomes more familiar with the use of the ASDF program and the positioning of the poles and zeros in the z-plane he will undoubtedly attempt to generate filters with sharper transition regions, and greater attenuation in the stop band(s). In general these filter improvements are accomplished by increasing the order of the system and positioning the poles closer to the unit circle. As the order of the system increases, and as the poles of the filter become closer to the unit circle, the filter becomes increasingly subject to the difficulties associated with the finite precision arithmetic used in the filter implementation.

A tacit assumption made very early in most digital signal processing courses (and often quickly forgotten) is that infinite precision arithmetic is available in performing the calculations. This assumption breaks down

when digital filters are realized in hardware or simulated! In general there are three sources of error which may affect the performance of digital filters. Due to the finite precision representation of the coefficients, the values of the implemented filter coefficients are only approximately equal to the desired values. Second, errors may be generated in the arithmetic operations. In general, the product of two n-bit numbers results in a 2n-bit result. An error occurs when this 2n-bit number is converted to n-bits for succeeding computations. The third type of error encountered is the analog to digital conversion required for processing analog signals with digital filters. Only the first two of these errors is of concern in the ASDF program.

While an in depth analysis of finite precision effects is beyond the scope of this work, let us consider the filter which has eight zeros located at the origin, and eight poles located at -0.9. Entering these locations into the z-plane using the ASDF program generates the filter responses in figures 6-1a, b, c. A superficial glance at these responses indicates that this filter is unstable. The filter must be stable, however, since all of the poles lie within the unit circle.

There are several phenomena involved in this example. The first is the dynamic range limitation of the system on which the filter is implemented. The IBM-360 is limited to computing with numbers between  $16^{64}$  and  $-16^{-63}$ . Once the

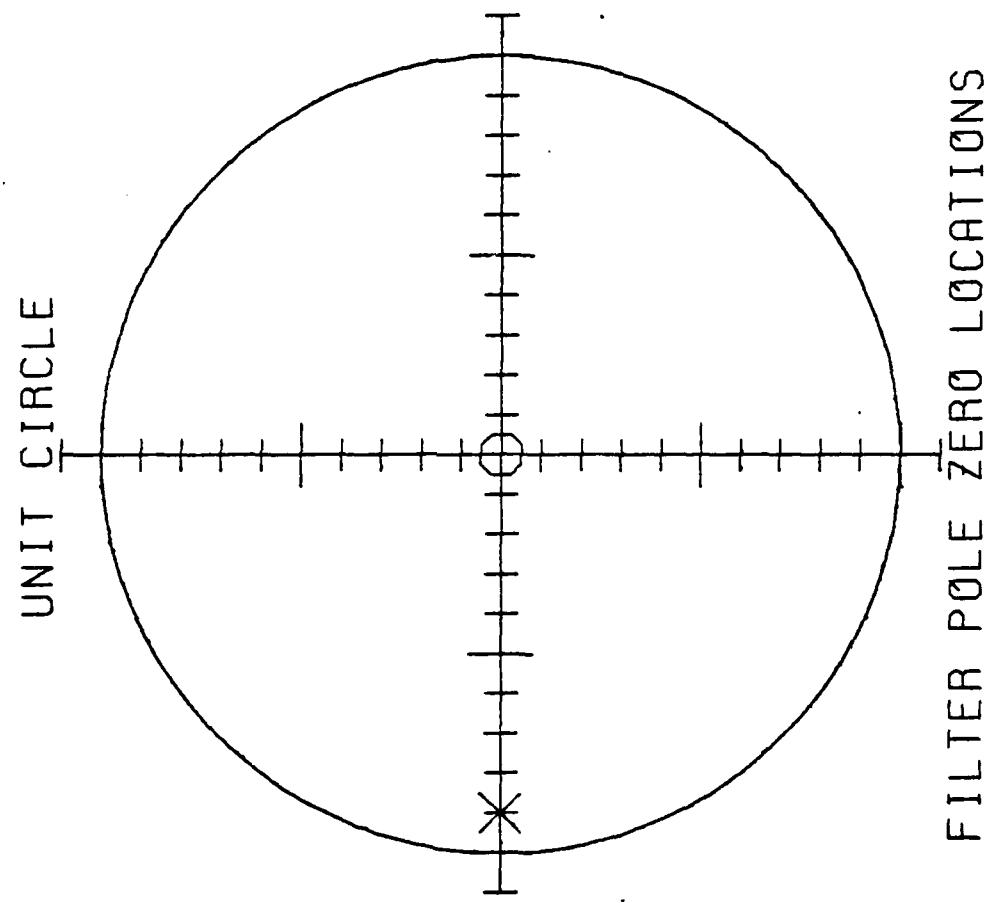


Figure 8-1a Example Filter With Eight Poles At  $-0.9$  And Eight Zeros At The Origin

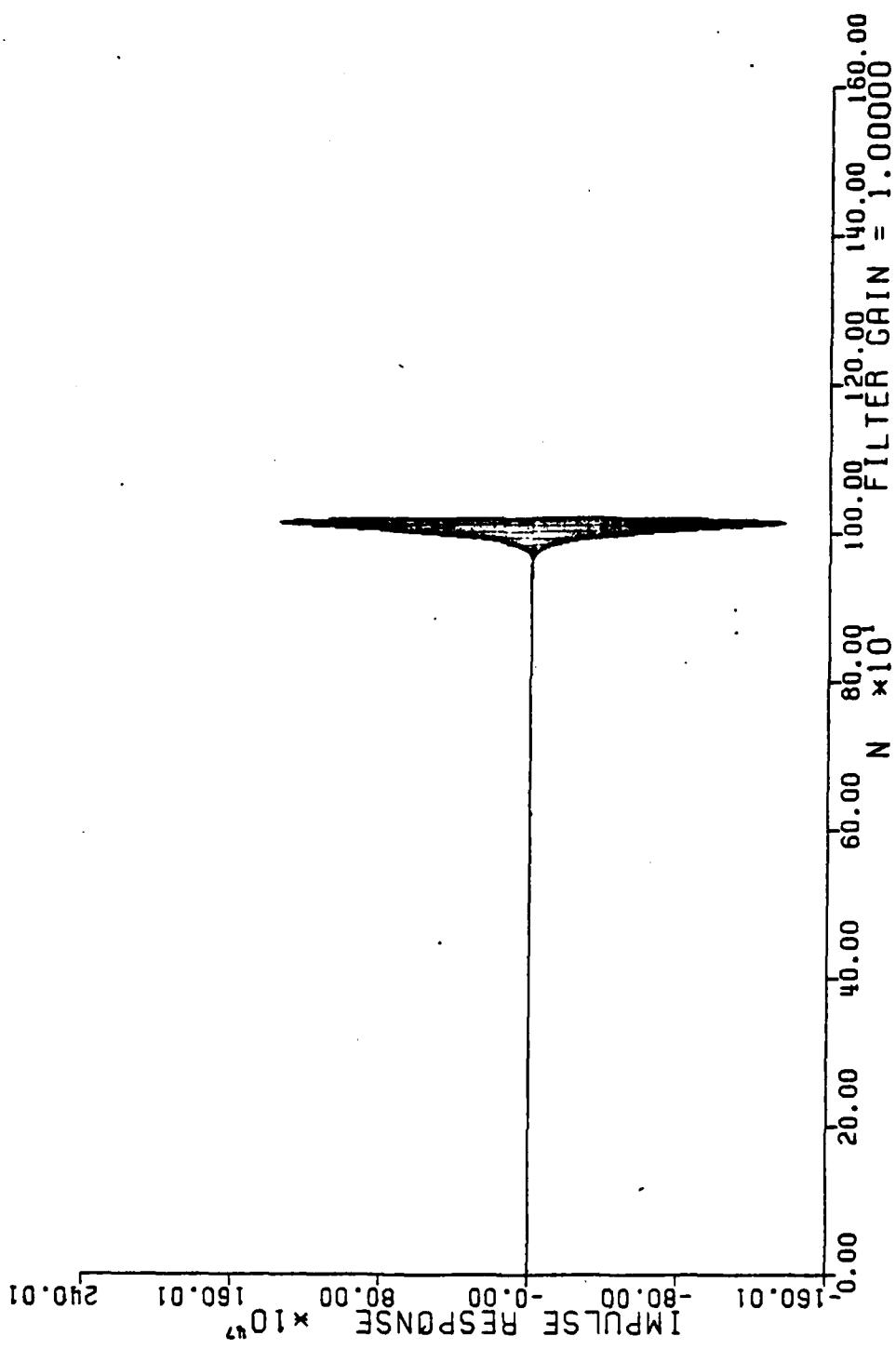


Figure 8-1b Unit Sample Response Of A Filter Exceeding System Dynamic Range Limitations

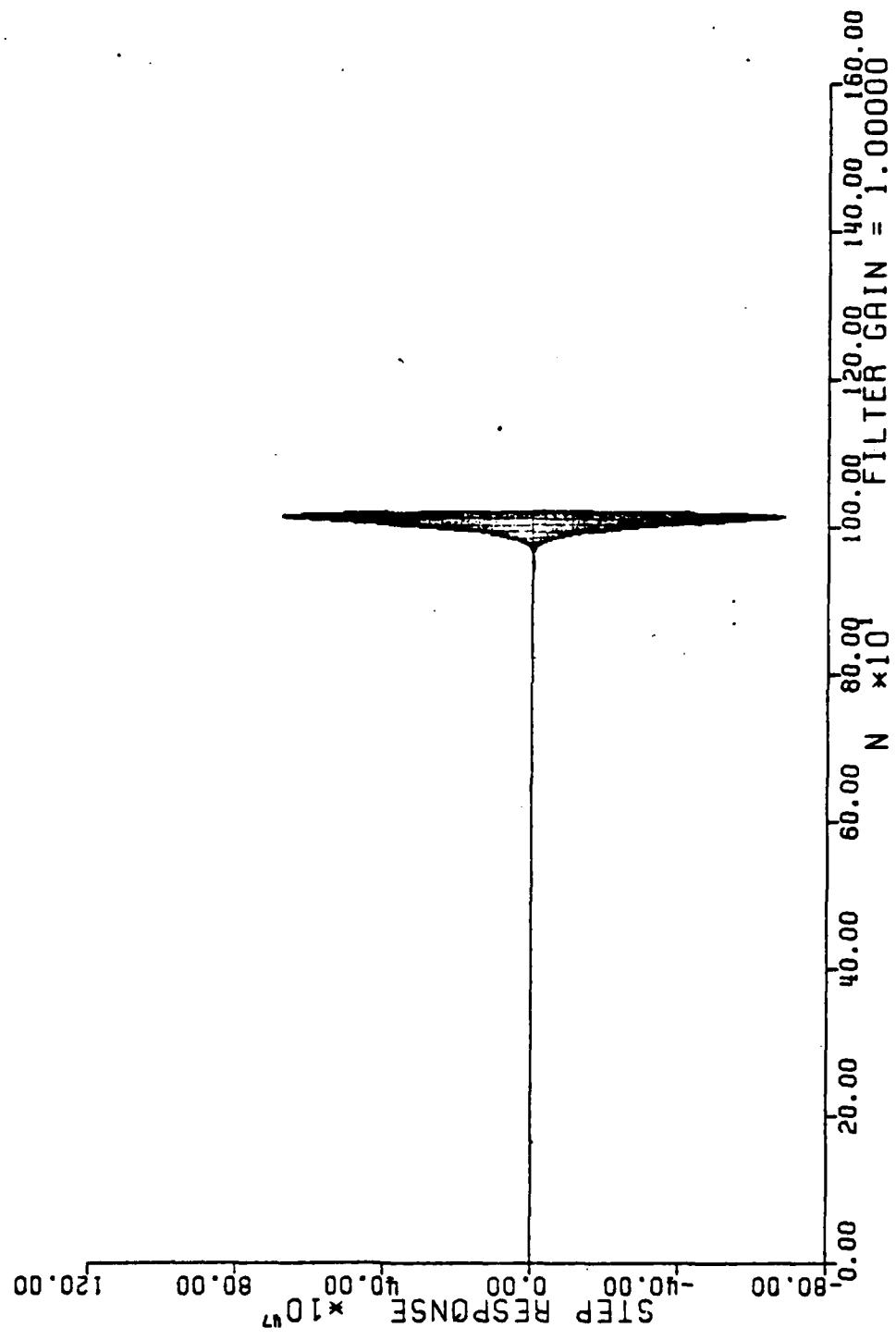


Figure 8-1c Step Response For A Filter Exceeding System Dynamic Range Limitations

larger of these limits is exceeded, the computations are terminated and it is not clear whether the designed filter is actually unstable or has merely exceeded the dynamic range limitations of the machine. The dedicated user may decide to modify the programs presented in the appendices to investigate the time responses of such systems. Clearly the form of the time responses will not be significantly altered if a modified unit sample response

$$1 \times 10^{-10}, 0, 0, 0, \dots$$

and a modified step response

$$1 \times 10^{-10}, 1 \times 10^{-10}, 1 \times 10^{-10}, \dots$$

is used.

If these modifications are performed, two other phenomena become apparent, each relating to the finite precision implementation of the digital filter. The first is that, in general, digital filters have deadbands, the second that the filter output may degenerate to a limit cycle. The original works by Blackman [Ref. 1] demonstrate that digital filters exhibit both of these effects. Extensive coverage of these phenomena is not appropriate here, however, a dead-band in a digital filter can be simplistically described as a span of filter input values for which the filter output does not change. The limit cycle effect is evident when a digital filter responds to a steady state input. For constant inputs, the filter output may run through a cycle of values. The propensity for

experiencing limit cycles is obvious in the calculation of the step response. A close look at the unit sample response shows that after a sufficiently large number of input values, this unit sample sequence becomes in reaching steady state, a constant.

When observing the output response of the example filter, there is still another possibility for explaining this output. This explanation revolves around the fact that the poles in the implemented filter are not at the locations expected. In fact, the poles may actually move outside the unit circle even though they were entered within. In general, there are only a finite number of pole locations possible with finite word length coefficient representations. The effect of this limitation is best explained using another example. Consider a filter with three zeros located at 0.5, and  $0.2 \pm j0.5$ , and four poles located at -0.999, -0.6, and  $-0.69 \pm j0.69$ . The infinite precision transfer function for this filter is expressed in equation 8.1.

$$\frac{z^3 - .9 z^2 + .49 z - .145}{z^4 + 2.979 z^3 + 3.75822 z^2 + 2.3497398 z + .57074868} \quad (8.1)$$

Now consider the finite precision case where each of the coefficients must be represented by a six bit number. The pole at -0.6 is expressed in binary (exclusive of sign) as

.10011001100. . . and is truncated to six bits as .100110. When all of the coefficients are so represented, the transfer function is expressed by equation 8.2. Clearly the poles and zeros of this second transfer function are not the

$$H(z) = \frac{z^3 - .890625 z^2 + .474275 z - .140625}{z^4 + 2.9375 z^3 + 3.75 z^2 + 2.3125 z + .5625} \quad (8.2)$$

same in equation 8.1. In general the differences will change all of the filter responses. In fact for this particular case the new poles of the system are at  $-0.70522 \pm j0.16677$ , and  $-0.76353 \pm j0.698616$ ; this filter is unstable!

The reason for the shift in pole locations is clearly portrayed by the filter whose characteristic equation is equation 8.3.

$$(z + .995)^8 = 0 \quad (8.3)$$

This filter has eight poles at  $-0.995$ . Note what happens to the filter when an error is introduced by truncating the infinite precision coefficient values to thirty-two bits. For simplicity restrict the discussion to the ramifications of an error generated in the value of the constant  $(.995)^8$ . This error can be as large as  $2 \times 10^{-10}$ . With this error explicitly included, the new characteristic equation will be:

$$(z + .995)^8 + 2 \times 10^{-10} = 0 \quad (8.4)$$

The roots of equation (8.4) are complex, and lie on a circle of radius 0.06 around the point  $-0.995 \pm j0.0$ . Figure 8-2 shows that three of these roots lie outside the unit circle. Thus with a finite precision implementation of the filter (even with 32 bits of precision), it is possible for the pole locations to move so far that the filter actually becomes unstable.

The results of this section as well as four types of ASDF outputs which have been observed, are summarized in figure 8-3. Trace A shows the unit sample response of a stable filter. Trace B shows the response of a filter which exceeds the dynamic range limitations of the implementation system. Trace B1 is for an unstable filter and B2 is for a stable filter caught in a limit cycle. These two traces can be observed or explored only by modifying the unit sample sequence. Trace C shows a stable filter which falls into a limit cycle below the dynamic range limit of the machine upon which the implementation has been performed. Note that the performance of a filter above the dynamic range limitation of the IBM 360 (or any other machine) cannot be observed, unless the ASDF program is modified.

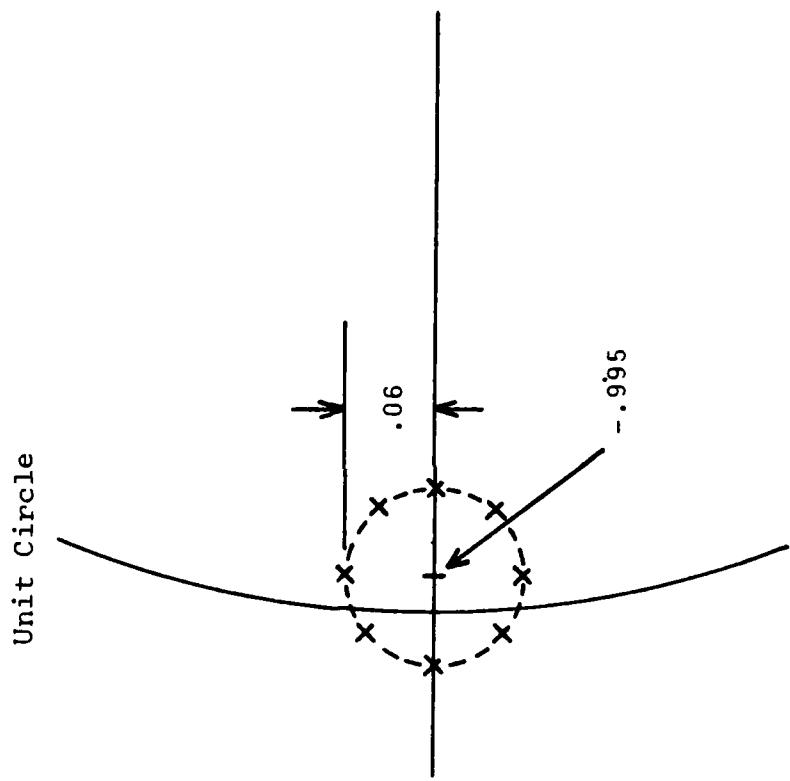


Figure 8-2 Three Of These Complex Poles Are Outside The Unit Circle

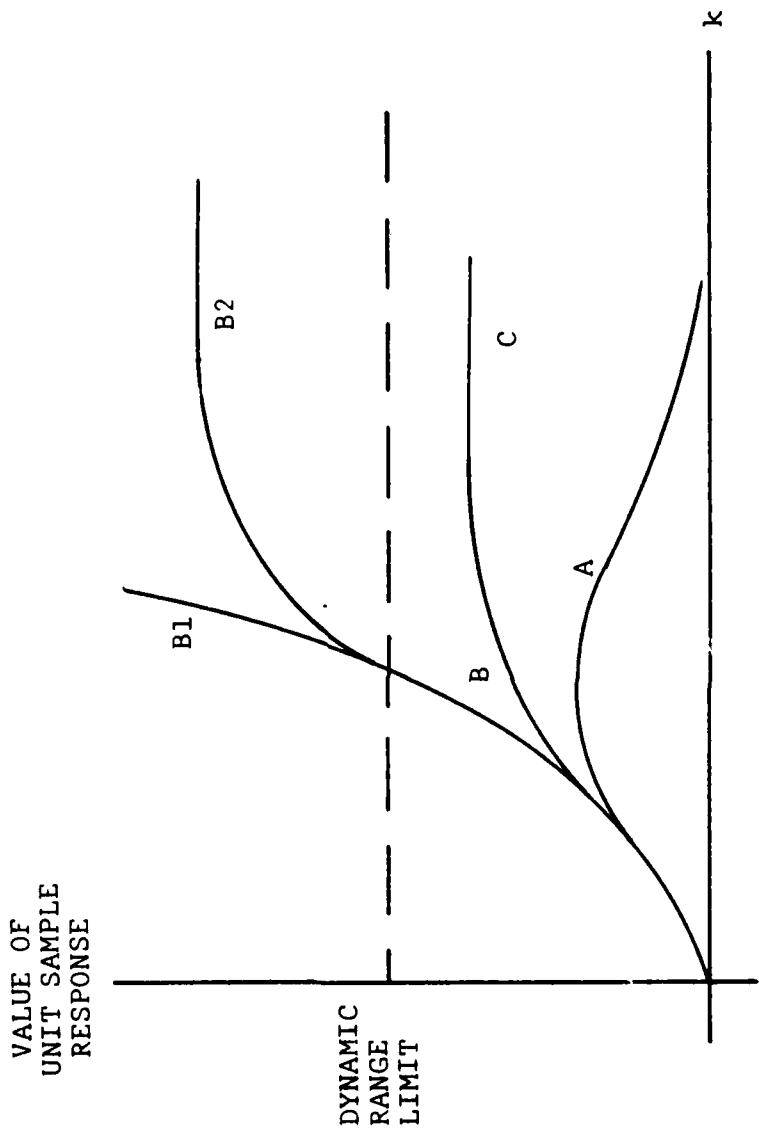


Figure 8-3 Summary Of Possible Observed Unit Sample Responses

## IX. SUMMARY AND CONCLUSIONS

The Advanced Simulation of Digital Filters has been implemented on the IBM 360, and is intended for the use by persons beginning their study of digital signal processing. The programs included within the package have been designed to make the user's interaction with the z-plane as simple as possible. While the programs themselves are available for study, all of the computations are invisible to the user, in an attempt to develop the user's intuition of the discrete domain without overwhelming him with arithmetic computations.

The ASDF package provides the user with an interactive method by which the filter pole and zero locations can be manipulated and the effects observed of such movement. ASDF can simulate filters of up to tenth order, and is punctuated with numerous comments and instructions which are to assist the user. The interface with the z-plane is available in a rapid interactive graphics mode, as well as in the slower polar and rectangular modes, each providing greater position location accuracy. The filter responses generated by ASDF are presented as a series of displays directly on the Tektronix 4012 terminal. Versatec plot capability has been integrated into the system to provide high quality copies of the system responses.

#### A. CONCLUSIONS

There are several points which are worth considering for persons intending to pursue this or other areas of interactive systems development with the graphics terminals. While comments may appear obvious they are stated to minimize the difficulties which can be encountered. First, a serious attempt should be made to define the entire data structure before beginning the programming stage of the work. All phases of the effort must be planned before commencing with the actual programming to insure that the data structure selected is sufficiently general, and sufficiently flexible to endure the additions and changes which inevitably occur when initial objectives are overlooked or changed. Second, it is imperative to master all of the software tools available and applicable to the project. There are features of the PLOT 10 software which exist and were not used in the ASDF program. This shortcoming is due to insufficient a priori knowledge. For example, the writing of text portions of the screen presentations should have been much simpler. Finally, it is important to research all of the attributes of the devices used for the final problem solution, and direct the solution to take advantage of all the system capabilities.

## B. AREAS FOR FUTURE WORK

There are several areas in which this program could be improved or extended. The possibility exists for transferring the ASDF programs to the Tektronix 4082 computing system. This move would avoid many of the shortcomings associated with the current IBM 360 system. The user would be relatively immune to system crashes, and the constraints placed upon him by concerning the IBM system's being operational and/or available. There are several disadvantages associated with this move. With the advent of the new computer system the majority of the current problems concerning system reliability, and constraints on available access hours should be eliminated. Furthermore, transferring these programs to the 4082 system will require significant rewriting to make execution possible on a system which has a much smaller virtual machine. Furthermore to fully benefit from the 4082 system, the interfacing routines should be rewritten to take advantage of the 4082 refresh capability. It seems that all of the effort involved for this change is not worth the expected improvements.

The ASDF program is now useful for analyzing digital filters. It seems likely that this capability could be expanded into a method for computer-aided design of digital filters. There are standard transformations which allow the filter designer to map analog filter requirements into the

appropriate digital requirements, and as well there are transformations which make possible the computation of digital filter transfer functions from known analog transfer functions. There are also a variety of optimization techniques referenced in the literature which could be implemented.

The other area of obvious expansion for the ASDF program is to include the capability for performing spectral analysis. It would be worthwhile (though perhaps not particularly involved) to include in the system the ability to calculate Discrete Fourier Transforms, and graphically display the results. Additionally, it would be possible to demonstrate the correspondence between performing convolution in the time domain directly and performing the convolution in the frequency domain by multiplying the DFT's. The relation between the circular and linear convolution could also be graphically portrayed.

As a final precautionary note, it is not possible to overestimate the length of time required to generate well documented, correct, useful programs on an interactive basis. Changes in system parameters, and the limitations in system software can make the process of simplifying the user's interactive responsibilities a very difficult process for anyone not thoroughly acquainted with all available resources. The myriad of possible incorrect user responses which must be anticipated make the problem extensive.

## APPENDIX A: PROBABLE SOLUTIONS FOR DIFFICULTIES

SYMPTOM: RESPONSE command returns an error message upon execution.

SOLUTION: Check the virtual machine size with the command "CP Q F" to insure a virtual machine size of 400K. If the user has only been allocated 256K, logoff and log back on as directed in chapter five. Load ASDF as described in chapter six.

SYMPTOM: User has inadvertently entered the control program, ie., CP.

SOLUTION: Type in "b" and "return." Normal program execution should resume.

SYMPTOM: The carat appears with the blinking cursor, but it is not located in the command array.

SOLUTION: Move the trace cursor into the command array, and type a "space." Normal operation should resume.

SYMPTOM: No terminal activity.

SOLUTION: First, check to see whether or not the system has crashed. If the system has crashed, logon as in chapter five, and load ASDF as in chapter six. If the system has not crashed, move the cursor to the center of the screen and

type "space" and "return." If normal operation has not resumed hit the "break" key. When the CP prompt appears, type "b." Normal operation should resume.

**SYMPTOM:** An error is detected in the execution of ASDF191 EXEC indicating that no temporary disk space is available.

**SOLUTION:** Check with the consultant or a systems programmer.

**SYMPTOM:** The user can not escape from a delete pole or delete zero command in the interactive graphics mode (IAG).

**SOLUTION:** Implicit in each request to delete from the z-plane is a request, validating the change to be made. In the delete IAG mode the trace cursor returns after illustrating the root to be deleted. Type "y" if the correct root was identified. Type "n" if the wrong root was identified, and attempt the procedure again.

**SYMPTOM:** The user did not enter the correct amount of data and the program terminated on a 217 error.

**SOLUTION:** Type "b" and "return." The program should restart with the ASDF signature. At this point reenter the command desired. If executing the POLZRO command it is advisable to execute the list (LST) command to check on the current filter status.

## APPENDIX B: IMPORTANT SUBROUTINES AND VARIABLES

The subroutines and variables described in this appendix are applicable to all programs within the ASDF package.

### A. SUBROUTINE NAMES

The subroutines within the ASDF package are divided into three major categories: 1) Plot-10 software, 2) Versatec software, and 3) routines generated explicitly for the ASDF programs.

#### 1. Plot-10 Software Subroutines

The Plot-10 subroutines are all adequately described in reference 10, and are listed below.

|        |        |        |
|--------|--------|--------|
| ERASE  | MOVABS | ANMODE |
| RECOVR | HOME   | LINEF  |
| NEWLIN | SVINDO | VVINDO |
| POLTRN | MOVEA  | DRAWSA |
| LINTRN | DRAWR  | DRWREL |
| MOVREL | VCURSR | BELL   |
| POINTA | SCURSR | INIT   |
| TABHOR | TABVER | SEELOC |
| FIN    | FINITT | DRAWA  |
|        |        | DRWABS |

## 2. Versatec Subroutines

The Versatec subroutines are listed below, and are explained in detail in reference 7.

|       |      |        |
|-------|------|--------|
| PLOTS | PLOT | WINDOW |
| SCALE | AXIS | SYMBOL |
| LINE  |      |        |

## 3. ASDF Subroutines

Each of the following subroutines have been generated for the ASDF programs.

CRRMM - Add and delete poles and zeros from the z-plane. The change "C" can be either "A" for add or "D" for delete. The roots "RR" can be "RZ" for real zero, "CZ" for complex zero, "RP" for real pole, or "CP" for complex pole. Mode "MMM" can be "IAG" for interactive graphics, "POL" for poles, or "RCT" for rectangular.

FLTR2 - Prints a listing of the pole and zero locations of the filter being considered.

ASUBK - Generates the  $a_k$  coefficients required to evaluate the transfer function.

BSUBR - Generates the  $b_r$  coefficients required to evaluate the transfer function.

ADJUST - Insures that the correct number of zeros located at the origin are included in the coefficients  $a_k$  and  $b_r$ .

RSPNSE - Computes the time responses of the filter.

FRQNCY - Computes the phase and magnitude of the transfer function for the prescribed filter.

PPPLT - Scales the ordinate data prior to plotting the responses.

PLTIMP - Plots the unit sample response.

PLTSTP - Plots the unit step response.

PLTTRF - Plots the phase of the transfer function as well as the magnitude in linear and decibel format.

UNTCR - Plots the unit circle with the appropriate poles and zeros.

START - Initializes all arrays and required variables.

FINISH - Checks to insure that the constructed filter is causal, and generates a file to save the pole and zero locations.

ANGLE - Draws the angle sign for polar commands.

ERROR - Controls program flow and error messages for user generated errors.

LST - Prints a listing of the current pole zero location.

PLTTBL - Plots the poles and zeros on the unit circle.

CHCKSZ - Insures that roots are available to be deleted and that the maximum system order will not be exceeded.

UPDATE - Makes changes in the POLZRO array to correspond to user changes in the z-plane.

LOCATE - Searches the POLZRO table for the root closest to that which the user wishes to delete.

STRRTS - Puts poles and zeros into the POLZRO array.

PLOTRT - Plots a single pole or zero on the unit circle.

## B. IMPORTANT VARIABLES

The variables described below pertain to all of the subroutines and programs within the ASDF package.

IROOTS(1) - Keeps track of the number of poles and zeros in the system under consideration. IROOTS(1) is the number of real zeros. IROOTS(2) is the number of complex zero pairs. IROOTS(3) is the number of real poles. IROOTS(4) is the number of complex pole pairs.

POLZRO(I,J) - The locations of the zeros are stored for values of I from one to ten. The pole locations are stored for values of I from 11 through 20. The real part of the rectangular representation of a root location is stored with J equal to one. The imaginary part of the rectangular representation for a root location is stored with J equal to two. The magnitude and angle of the root's polar representation are stored for J values of three and four, respectively. POLZRO(1,5) holds the root type.

IERROR - Keeps track of the generation of an error. Once the error has been identified the value is set to one. When the error has been explained to the user the value is reset to zero.

A(I) and B(I) - Store the values of the  $a_k$  and  $b_r$  coefficients.

AA(I) and BB(I) - Store the double precision values of the  $a_k$  and  $b_r$  coefficients.

YI(I) - Stores the values of the unit sample response to be plotted.

YS(I) - Stores the values of the unit step response to be plotted.

YP(I) - Stores the values of the phase of the transfer function to be plotted.

YM(I) - Stores the magnitudes of the transfer function to be plotted.

YMDB(I) - Stores the transfer function magnitudes in decibels to be plotted.

EN(I) - Stores the time values against which the dependent variables are plotted.

IYIPTS - Holds the number of unit sample points to be plotted.

IYSPTS - Holds the number of unit step response points to be plotted.

NNEN - Is the order of the denominator plus one.

NNUM - Is the order of the numerator plus one.

NORDER - Is the order of the system under consideration.  
This can be either of the numerator or denominator.

LAST - Holds the number of points to be plotted.

FLTRGN - Is the value that the user assigns to the filter gain.

ZEROS(I) - Holds the complex coefficients which will be made real to generate the  $b_r$  coefficients.

POLES(1) - Holds the complex coefficients which will be made real to generate the  $a_k$  coefficients.

The remainder of the variables are either obvious, or used merely for control of the program flow, i.e. do loop indicies, etc.

#### **APPENDIX C. STRUCTURE FOR ASDF TEXT FILE**

The file ASDF TEXT is a composite file made up of all of the required programs and EXEC files for running the ASDF program package. These files have been consolidated to minimize the time required for transfer from DISK02 to DSX001. The structure of the composite file is listed below:

BREAK001

EXEC file ASDF192

BREAK002

TEXT file for POLZRO command

BREAK003

TEXT file for RESPONSE command

BREAK004

Information printed out by the INTRO command

BREAK005

VTEC1 JCL - used for EXEC HRD\$CPY

BREAK006

VTEC2 JCL - used for EXEC HRD\$CPY

BREAK007

Labels for RESPONSE plots

BREAK008

EXEC file to execute the EXEC PUNCH command

BREAK009

Initial file FT01F001 with no poles or zeros  
BREAK010  
TEXT file for generating JOB cards  
BREAK011  
TEXT file for the INTRO command  
BREAK012  
Information printed by OPTIONS command  
BREAK013  
Information printed on the title page  
BREAK014  
EXEC file to execute HRD\$CPY command  
BREAK015  
TEXT file for the OPTIONS command  
BREAK016  
TEXT file for the software page clear  
BREAK017

#### APPENDIX D. JCL FOR EXEC HRD\$CPY COMMAND

The Job Control Language required for the execution of the EXEC HRD\$CPY command is provided to give insight into the file manipulation utilized by the ASDF package. Should the permanent locations of any of the portions of the ASDF package change this section of JCL must be changed also.

##### JCL for VTEC1

```
//GO EXEC PGM=THEPLT,REGION=180K
//STEPLIB DD UNIT=3330,VOL=SER=DISK03,DISP=SHR,DSN=S1502.ASDF
//FT05F001 DD DDNAME=SYSIN
//FT06F001 DD SYSOUT=A
//FT15F001 DD DDNAME=PLOTPARM
//PLOTLOG DD SYSOUT=A
//VECTR2 DD DSN=&VECTR2,DISP=(,PASS),SPACE=(CYL,(5,5)),UNIT=SYSDA
//VECTR1 DD DSN=&VECTR1,DISP=(,PASS),SPACE=(TRK,(1,1)),UNIT=SYSDA
//GO.SYSIN DD *
```

##### JCL for VTEC2

```
//PLOT EXEC PGM=IEVMAPP,COND=(4,LT)
//FT15F001 DD DDNAME=PLOTPARM
//STEPLIB DD DSN=SYS1.VTECPLOT,DISP=SHR
//PLOTLOG DD SYSOUT=A
//VECTR1 DD DISP=(OLD,DELETE),DSN=&VECTR1
//VECTR2 DD DISP=(OLD,DELETE),DSN=&VECTR2
//SYSVECTR DD SYSOUT=(A,,5555)
//VECTTAPE DD DUMMY
//
```

APPENDIX E: SOURCE DECK FOR ASDF191 EXEC

```
ASDF1001  
ASDF1002  
ASDF1003  
ASDF1004  
ASDF1005  
ASDF1006  
ASDF1007  
ASDF1008  
ASDF1009  
ASDF100A  
ASDF100B  
ASDF100C  
ASDF100D  
ASDF100E  
ASDF100F  
ASDF100G  
ASDF100H  
ASDF100I  
ASDF100J  
ASDF100K  
ASDF100L  
ASDF100M  
ASDF100N  
ASDF100O  
ASDF100P  
ASDF100Q  
ASDF100R  
ASDF100S  
ASDF100T  
ASDF100U  
ASDF100V  
ASDF100W  
ASDF100X  
ASDF100Y  
ASDF100Z  
ASDF1020  
ASDF1021  
ASDF1022  
ASDF1023  
ASDF1024  
ASDF1025  
ASDF1026  
ASDF1027  
ASDF1028  
ASDF1029  
ASDF1030  
ASDF1031  
ASDF1032  
ASDF1033  
ASDF1034  
ASDF1035  
ASDF1036  
ASDF1037  
ASDF1038  
ASDF1039  
ASDF1040  
ASDF1041  
ASDF1042  
ASDF1043  
ASDF1044  
ASDF1045  
ASDF1046  
ASDF1047  
ASDF1048  
  
*****  
COMMENT* SOURCE DECK FOR ASDF COMMAND: EXEC ASDF191 *  
COMMENT* *****  
COMMENT* GENERATE A STACK TO EDIT THE ASDF192 FILE  
COMMENT* OFF OF THE BEGINNING OF THE ASDF TEXT FILE  
COMMENT WHICH IS STORED ON DISK02  
COMMENT  
COMMENT BEGINSTACK  
COMMENT F0718. ASDF#  
ND  
F BREAK002  
D 50000  
# FILE ASDF192  
ENDSTACK  
COMMENT RESERVE AND FORMAT THE TEMPORARY DISK SPACE  
COMMENT DEFINE T2314 192 10  
FORMAT ALL {NOTYPE}  
COMMENT GIVE THE PROGRAMS ACCESS TO ALL REQUIRED LIBRARIES  
GLOBAL TEKLIB SYSLIB  
SET LINLEN 72  
COMMENT MODIFY THE TOCP EXEC ON THE SYSTEM DISK  
COMMENT SO THAT IT WILL ACCEPT THE STACK OF  
COMMENT EDIT COMMANDS AND GET A SDF TEXT FROM DISK  
LOADMOD OSDISK {CLEAR  
LUPST 138E4 18111811  
LUPST 1392C 4 780CF34  
START * ASDF TEXT T1 237  
COMMENT GENERATE THE CORRECT FILETYPE FOR ASDF  
ALTER ASDF TEXT T1 ASDF EXEC T1  
COMMENT PERFORM THE EDITING OF THE ASDF TEXT FILE  
EXECUT ASDF EXEC T1 ASDF TEXT T1  
COMMENT PREPARE TO MOVE THE USER TO THE
```

E COMMENT TEMPORARY DISK - INFORM THE USER OF  
E COMMENT THE APPROPRIATE COMMANDS TO ISSUE OF  
E COMMENT RELEASE 192 T

EPRINT EPRINT EPRINT EPRINT EPRINT EPRINT

ISSUE THE COMMAND: LOGIN 192 P

ISSUE THE COMMAND: EXEC ASDF192

ASDF1049  
ASDF1050  
ASDF1051  
ASDF1052  
ASDF1053  
ASDF1054  
ASDF1055  
ASDF1056  
ASDF1057  
ASDF1058  
ASDF1059  
ASDF1060  
ASDF1061  
ASDF1062  
ASDF1063



```

FILE
FILE
#END#ND #ENDSTACK
ECOMMENT SPLIT EACH SUCCESSIVE FILE OFF OF THE
ECOMMENT COMPOSITE ASDF TEXT FILE; THEN CHANGE
ECOMMENT THE FILE TYPE TO P1.
ECOMMENT ASDF TEXT PULZRO TEXT BREAK002 BREAK003
SPLIT ASDF TEXT P5 PULZRO TEXT BREAK003 BREAK004
ALTER ASDF TEXT RESPONSE P5 PULSE TEXT P1
SPLIT ASDF TEXT INTR0 F704FOOL BREAK004 BREAK005
ALTER ASDF TEXT FT04FOOL P5 INTR0 F704FOOL P1
SPLIT ASDF TEXT VTEC1 JCL BREAK005 BREAK006
ALTER VTEC1 JCL VTEC1 JCL P1
SPLIT ASDF TEXT VTEC2 JCL BREAK006 BREAK007
ALTER VTEC2 JCL VTEC2 JCL P1
SPLIT ASDF TEXT FILE FT02FOOL BREAK007 BREAK008
ALTER FT02FOOL P5 FILE FT02FOOL P1
SPLIT ASDF TEXT PUNCH EXEC P5 PUNCH EXEC P1
ALTER PUNCH EXEC P5 PUNCH EXEC P1
SPLIT ASDF TEXT FILE FT01FOOL BREAK009 BREAK010
ALTER FT01FOOL P5 FILE FT01FOOL P1
SPLIT ASDF TEXT FILE FT01FOOL P5 FILE FT01FOOL P1
ALTER FT01FOOL P5 FILE FT01FOOL P1
SPLIT ASDF TEXT FILE FT01FOOL P5 FILE FT01FOOL P1
ALTER FT01FOOL P5 FILE FT01FOOL P1
SPLIT ASDF TEXT FILE FT01FOOL P5 FILE FT01FOOL P1
ALTER FT01FOOL P5 FILE FT01FOOL P1
SPLIT ASDF TEXT OPTIONS FT03FOOL BREAK012 BREAK013
ALTER JOBS$CRD TEXT INTR0 TEXT BREAK011 BREAK012
SPLIT ASDF TEXT INTR0 TEXT P5 INTR0 TEXT P1
ALTER ASDF TEXT INTR0 TEXT OPTIONS FT03FOOL BREAK012 BREAK013
SPLIT ASDF TEXT OPTIONS FT03FOOL P5 FILE FT03FOOL P1
ALTER ASDF TEXT COVER FT04FOOL BREAK013 BREAK014
ALTER COVER FT04FOOL P5 COVER FT04FOOL P1
SPLIT ASDF TEXT HRD$CPY EXEC CPY EXEC CPY EXEC P1
ALTER HRD$CPY EXEC P5 HRO$CPY EXEC P5 HRO$CPY EXEC P1
ALTER ASDF TEXT OPTIONS TEXT P5 OPTIONS TEXT P1
SPLIT ASDF TEXT CLEAR TEXT BREAK015 BREAK016
ALTER CLEAR TEXT P5 CLEAR TEXT P1
SPLIT ASDF TEXT P5 CLEAR TEXT P1
ECOMMENT EDIT EACH OF THE FILES JUST CONSTRUCTED
ECOMMENT TO ELIMINATE THE LOGICAL SEPARATORS.
ECOMMENT THESE SEPARATORS ARE
ECOMMENT ALL OF THE FORM BREAKXX.

```

```

COMMENT
EDIT POL2RO TEXT P1
EDIT RESPONSE TEXT P1
EDIT INTRO FT04F001 P1
EDIT VTEC1 JCL P1
EDIT VTEC2 JCL P1
EDIT FILE F T02F001 P1
EDIT PUNCH EXEC P1
EDIT FILE F T01F001 P1
EDIT FILE F T02F001 P1
EDIT JOB$CRD TEXT P1
EDIT INTRO TEXT P1
EDIT FILE F T03F001 P1
EDIT COVER FT04F001 P1
EDIT HRT$CPY EXEC P1
EDIT OPTION $ TEXT P1
EDIT CLEAR TEXT P1
COMMENT LOAD EACH OF THE CREATED FILES
COMMENT AND GENERATE A CORE IMAGE
COMMENT SO THAT SUBSEQUENT LOADING AND
COMMENT LINKING IS NOT REQUIRED.
LOAD POL2RO
GENMOD POL2RO (NOMAP P2)
LOAD RESPONSE (NOMAP P2)
LOAD INTRO
GENMOD INTRO
LOAD JOB$CRD
GENMOD JOB$CRD
LOAD OPTIONS
GENMOD OPTIONS (NOMAP P2)
LOAD CLEAR
GENMOD CLEAR (NOMAP P2)
&TYPE OUT OFF
ALTER COVER FT04F001 P1 FILE FT04F001 P1
INTRO
ALTER FILE FT04F001 P1 COVER FT04F001 P1
ALTER INTRO FT04F001 P1 FILE FT04F001 P1
OPTIONS
CLEAR
COMMENT THESE NEXT STATEMENTS FORM AN
COMMENT INFINITE LOOP WHICH PROCESSES
COMMENT SUCCESSIVE ASDF AND CP/CMS COMMANDS.
COMMENT -LOOP &PRINT *ASDF-READY
&READ
&ERROR EG010 -LOOP2

```

CLEAR  
E<sub>G</sub>O<sub>T</sub>O -L<sub>O</sub>O<sub>P</sub>  
-L<sub>O</sub>O<sub>P</sub>2 E<sub>P</sub>R<sub>I</sub>N<sub>T</sub> INPUT COMMAND ERROR  
E<sub>G</sub>O<sub>T</sub>O -L<sub>O</sub>O<sub>P</sub>

A SDF 2145  
A SDF 2146  
A SDF 2147  
A SDF 2148

APPENDIX G: SOURCE DECK FOR ASDF COMMAND: POLZRO

```

***** SOURCE DECK FOR ASDF COMMAND: POLZRO ****
C* THIS IS THE MAIN PROGRAM FROM WHICH ALL SUBROUTINES
C* WILL BE CALLED
C* COMMON IROOTS(4),POLZRO(20,5),IERROR,IOLD
C* CALL START
C* CALL UNTCIR
C* IF(IROOTS(1)+2*IROOTS(2)*LE.IROOTS(3)+2*IROOTS(4))STOP
C* CALL ERASE
C* CALL MOVABS(126,425)
C* CALL ANMODE
C* WRITE(6,100)
C* 100 X*ACTION*
C* CALL RECOVR
C* CALL MOVABS(301,381)
C* CALL ANMODE
C* WRITE(6,102)
C* 102 FORMAT('HIT A SPACE AND RETURN TO CONTINUE')
C* CALL RECOVR
C* CALL MOVABS(525,337)
C* CALL ANMODE
C* READ(5,101) IN
C* 101 FORMAT(1A1)
C* CALL RECOVR
C* IOLD=1
C* GO TO 10
C* END

SUBROUTINE LETTER
C* THIS SUBROUTINE GENERATES THE ALPHANUMERIC INFORMATION FOR
C* THE UNIT CIRCLE SUBROUTINE (32)
C* DIMENSION ICMD(13)
C* DATA ICMD/3HACZ,3HACZ,3HARZ,3HARP,
C*      1          3HDHZ,3HDHZ,3HDRZ,3HDRP,
C*      2          3HLST,3HEEM,3HEDY,3HEXC/
C* MOVE THE CURSOR TO THE SCREEN TOP LEFT CORNER (1)
C* CALL HOME
ASDF3001
ASDF3002
ASDF3003
ASDF3004
ASDF3005
ASDF3006
ASDF3007
ASDF3008
ASDF3009
ASDF3010
ASDF3011
ASDF3012
ASDF3013
ASDF3014
ASDF3015
ASDF3016
ASDF3017
ASDF3018
ASDF3019
ASDF3020
ASDF3021
ASDF3022
ASDF3023
ASDF3024
ASDF3025
ASDF3026
ASDF3027
ASDF3028
ASDF3029
ASDF3030
ASDF3031
ASDF3032
ASDF3033
ASDF3034
ASDF3035
ASDF3036
ASDF3037
ASDF3038
ASDF3039
ASDF3040
ASDF3041
ASDF3042
ASDF3043
ASDF3044
ASDF3045
ASDF3046
ASDF3047
ASDF3048

```

```

C* GENERATE A BLANK LINE (1)
C* CALL LINEF
C* ANMODE IS REQUIRED FOR FORTRAN I/O IN GRAPHIC MODE (1)
C* CALL ANMODE
C* PRINT THE TITLES (2)
C*      WRITE(6,100)
C*      100 FORMAT(6X,20HUNIT CIRCLE COMMANDS)
C* GET THE TERMINAL BACK TO THE GRAPHIC MODE (1)
C*      CALL RECOVR
C*      CALL NEWLIN
C*      CALL LINEF
C*      CALL ANMODE
C*      WRITE(6,101)
C*      101 FORMAT(9X,18HINTER-
C*                  KEYBOARD)
C*      CALL RECOVR
C*      CALL NEWLIN
C*      CALL ANMODE
C*      WRITE(6,102)
C*      102 FORMAT(3X,25HCMD$ ACTIVE RECT POLAR)
C*      CALL RECOVR
C*      CALL NEWLIN
C*      CALL LINEF
C*      CALL NEWLIN
C*      CALL ANMODE
C*      WRITE(6,103)
C*      103 FORMAT(4X,A3)
C*      RETURN
C*      END
C*      PRINT THE COMMANDS (6)
C*      DO 40 N=1,10
C*      CALL ANMODE
C*      WRITE(6,103) ICMD(M)
C*      CALL RECOVR
C*      CALL LINEF
C*      40 FORMAT(4X,A3)
C*      RETURN
C*      END
C*      SUBROUTINE PLOTUC
C* THIS SUBROUTINE DRAWS THE UNIT CIRCLE WITH THE AXES

```

```

C* CONFINE THE UNIT CIRCLE TO A 600 X 600 RASTER UNIT SQUARE
C* POSITION THE SCREEN WINDOW
C* XMIN = (1023-600) = 423
C* YMIN = 0
C* CALL SWINDO (393,630,0,630)
C* GENERATE THE UNIT CIRCLE (4)
C* CALL VWINDO (0.,1.,0.,360.)
C* CALL POLTRN (0.,360.,0.)
C* CALL MOVEA (1.,0.)
C* CALL DRAWA (1.,360.)
C* RETURN TO RECTANGULAR COORDINATES
C* VIRTUAL WINDOW: -1.1 LE X,Y LE +1.1 (2)
C* CALL LINTRN
C* CALL VWINDO (-1..1,2..2,-1..1,2..2)
C* GENERATE THE X-AXIS (2)
C* CALL MOVEA (1.,0.)
C* CALL DRAWA (-2.,0.)
C* GENERATE THE Y-AXIS (2)
C* CALL MOVEA (0.,1.)
C* CALL DRAWA (0.,-2.)
C* GENERATE THE X-AXIS TICK MARKS {5}
C* B IS THE TICK MARK LENGTH IN USER UNITS
C* DO 10 I=1,19
B=.05
IF(I.EQ.5.OR.I.EQ.15)B=.1
10 CALL MOVEA (-1.+FLDAT(I)*.1,-B/2.)
CALL DRAWA (0.,B)
C* GENERATE THE Y-AXIS TICK MARKS {5}
C* B IS THE TICK MARK LENGTH IN USER UNITS
C* DO 20 I=1,19
B=.05
IF(I.EQ.5.OR.I.EQ.15)B=.1
20 CALL MOVEA (-B/2.*1.-FLDAT(I)*.1)
CALL DRAWA (B,0.)
ASDF3097
ASDF3098
ASDF3099
ASDF3100
ASDF3101
ASDF3102
ASDF3103
ASDF3104
ASDF3105
ASDF3106
ASDF3107
ASDF3108
ASDF3109
ASDF3110
ASDF3111
ASDF3112
ASDF3113
ASDF3114
ASDF3115
ASDF3116
ASDF3117
ASDF3118
ASDF3119
ASDF3120
ASDF3121
ASDF3122
ASDF3123
ASDF3124
ASDF3125
ASDF3126
ASDF3127
ASDF3128
ASDF3129
ASDF3130
ASDF3131
ASDF3132
ASDF3133
ASDF3134
ASDF3135
ASDF3136
ASDF3137
ASDF3138
ASDF3139
ASDF3140
ASDF3141
ASDF3142
ASDF3143
ASDF3144
ASDF3145

```

```

      RETURN
      END

      SUBROUTINE BOXUC
C*   THE PURPOSE OF THIS SUBROUTINE IS TO GENERATE THE "CHOICE"
C*   BOXES FOR THE UNIT CIRCLE SUBROUTINE
C*
C*   DIMENSION IBCORD (3,3)
C*
C*   DATA DESCRIBING THE LOWER LEFT CORNER (LLC) OF
C*   EACH BOX AND THE NUMBER OF BOXES IN EACH COLUMN
C*   IBCORD (J,1) IBCORD (J,2) IBCORD (J,3)
C*   LLCX    LLCY    NO. BOXES
C*
C*   DATA IBCORD/140,238,336,439,483,10,8,8/
C*
C*   GENERATE THE "CHOICE" BOXES (10)
C*
      DO 10 J=1,3
C*   MOVE TO THE LOWER LEFT CORNER OF THE BOX (1)
C*   CALL MOVABS (IBCORD(J,1),IBCORD(J,2))
C*   "IBCORD(J,3)" CONTROLS THE NUMBER OF BLOCKS TO BE DRAWN (10)
C*   K=IBCORD(J,3)
      DO 20 I=1,K
C*   DRAW THE ACTUAL BOX (4)
C*
C*   CALL DRWREL (0,16)
C*   CALL DRWREL (14,0)
C*   CALL DRWREL (0,-16)
C*   CALL DRWREL (-14,0)
C*
C*   PROCEED TO THE NEXT HIGHER BOX IN THE COLUMN (1)
C*   20   CALL MOVREL (0,22)
      10   CONTINUE
      RETURN
      END

      SUBROUTINE ACZIAG
COMMON TROOTS(4),POLZRO(20,5), TERROR
CALL CHCKSZ(2,2)
IF(TERROR.NE.0)RETURN

```

```

CALL VCURSR {ICCHAR,X,Y}
CALL STRRTS {2,1,X,Y}
RETURN
END

SUBROUTINE ACPIAG
COMMON IXXXX(4) PXXXX(20,5), IERROR
CALL CHCKSZ (2,4)
IF(IERROR.NE.0)RETURN
CALL VCURSR (ICCHAR, X,Y)

C* INSURE THAT THE POLES ARE WITHIN THE UNIT CIRCLE
C*
C* IF(SQRT(X**2+Y**2)>1)IERROR=9
C* IF(IERROR.NE.0)RETURN
CALL STRRTS (4,1,X,Y)
RETURN
END

SUBROUTINE ARZIAG
COMMON IXXXX(4) PXXXX(20,5), IERROR
CALL CHCKSZ (1,1)
IF(IERROR.NE.0)RETURN
CALL VCURSR (ICCHAR, X,Y)
Y = 0
CALL STRRTS (1,1,X,Y)
RETURN
END

SUBROUTINE ARPIAG
COMMON IXXXX(4) PXXXX(20,5), IERROR
CALL CHCKSZ (1,3)
IF(IERROR.NE.0)RETURN
CALL VCURSR (ICCHAR, X,Y)

C* INSURE THAT THE POLE IS WITHIN THE UNIT CIRCLE
C*
C* Y=0
C* IF(SQRT(X**2+Y**2)>1)IERROR=9
C* IF(IERROR.NE.0)RETURN
CALL STRRTS (3,1,X,Y)
RETURN
END

SUBROUTINE DCZIAG
COMMON IXXXX(4) POLZO(20,5), IERROR
CALL CHCKSZ (-1,2)
IF(IERROR.NE.0)RETURN

```

```

10 CALL VCURSR({ICHAR,X,Y,LINEPZ})
C* INDICATE THE COMPLEX ZERO NEAREST THE USER'S CURSOR
C* WITH A BRIGHT DOT FIVE TIMES {4}
C*
      XX=POLZRO(1,LINEPZ,1)
      YY=POLZRO(1,LINEPZ,2)
      IF(POLZRO(1,LINEPZ,3).LE.1.0) GO TO 15
      ANGLE=ATAN2(YY,XX)
      XX=1.05*COS(ANGLE)
      YY=1.05*SIN(ANGLE)
      DO 20 NREPS=1,5
      CALL BELL
      IF(Y.LE.0.) CALL POINTA(XX,-YY)
      IF(Y.GT.0.) CALL POINTA(XX,YY)
      CALL SCURSR({ICHAR,IX,IY})
      IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
      CALL UPDATE(2,LINEPZ)
      CALL NUC
      RETURN
END

SUBROUTINE DCPIAG
COMMON IXXX,XX(4),POLZRO(20,5),IERROR
CALL CHCKSZ(-1,4)
IF(IERROR.NE.0)RETURN
10 CALL VCURSR({ICHAR,X,Y,LINEPZ})
CALL LOCATE(4,X,Y,LINEPZ)
C* INDICATE THE COMPLEX POLE NEAREST DOT {4}
C* FIVE TIMES WITH A BRIGHT DOT
C*
      DO 20 NREPS=1,5
      CALL BELL
      IF(Y.LE.0.) CALL POINTA(POLZRO(1,LINEPZ,1),-POLZRO(1,LINEPZ,2))
      IF(Y.GT.0.) CALL POINTA(POLZRO(1,LINEPZ,1),POLZRO(1,LINEPZ,2))
      CALL SCURSR({ICHAR,IX,IY})
      IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
      CALL UPDATE(4,LINEPZ)
      CALL NUC
      RETURN
END

SUBROUTINE DRZIAG
COMMON IXXX,XX(4),POLZRO(20,5),IERROR
CALL CHCKSZ(-1,1)
IF(IERROR.NE.0)RETURN

```

```

10 CALL VCURSR(ICHAR,X,Y)
CALL LOCATE(1,X,0.,LINEPZ)
DO 20 NREPS=1,5
CALL BELL
CALL POINTA(POLZR((LINEPZ,1),0.))
CALL SCURSR(ICHAR,IX,IY)
IF(ICHAR.NE.121)AND(ICHAR.NE.89)GO TO 10
CALL UPDATE(1,LINEPZ)
CALL NUC
RETURN
END

SUBROUTINE DRPIAG
COMMON IXXXX(4)
CALL CHCKSZ(-1,3)
IF(TERROR.NE.0)RETURN
CALL VCURSR(ICHAR,X,Y)
CALL LOCATE(3,X,0.,LINEPZ)
DO 20 NREPS=1,5
CALL BELL
CALL POINTA(POLZR((LINEPZ,1),0.))
CALL SCURSR(ICHAR,IX,IY)
IF(ICHAR.NE.121)AND(ICHAR.NE.89)GO TO 10
CALL UPDATE(3,LINEPZ)
CALL NUC
RETURN
END

SUBROUTINE UNTCIR
C* THIS SUBROUTINE CONTROLS THE IMPLEMENTATION OF
C* COMMANDS ASSOCIATED WITH THE UNIT CIRCLE
C*
DATA ISE/2H E/
DATA IX/2H X/
DIMENSION IBCORD(4,3),IHTBL(10),IVTBL(10)
COMMON IXXXX(4),PXXXXX(20,5),TERROR,OLD
C* SET THE TAB TABLE SIZE TO TEN
C* CALL TTBLSZ(10)
C* LOCATE THE HORIZONTAL AND VERTICAL TABS (2)
C* DATA IHTBL/128,226,324,505,527,549,571,593,615,637/
C* DATA IVTBL/439,461,483,505,527,549,571,593,615,637/
C* INITIATE THE GRAPHICS ROUTINES (1)

```

```

C*      IF(IOLD.EQ.0)CALL INIT
C*      IF WORKING ON AN OLD FILTER - CONTINUE WITH IT
C*      IF(IOLD.EQ.1)CALL NUC
C*      IF(IOLD.EQ.1)GO TO 30
C*      IF(IOLD.EQ.0)CALL OLFILTER
C*      IF(IOLD.EQ.0)CALL ERASE
C*      IF(IOLD.EQ.1)CALL NUC
C*      IF(IOLD.EQ.1)GO TO 30
C*      GENERATE THE ALPHANUMERIC I/O FOR THE COMMAND TABLE
C*      OF THE UNIT CIRCLE SUBROUTINE (1)
C*      CALL LETTER
C*      GENERATE THE "CHOICE" BOXES (1)
C*      CALL BOXUC
C*      GENERATE THE UNIT CIRCLE (1)
C*      CALL PLOTUC
C*      ALLOW THE USER TO SELECT THE DESIRED COMMAND (1)
C*      30   CALL BELL
C*            CALL SCURSR (IIS,IIX,IIY)
C*      ADJUST CURSOR FOR INACCURACY ON USER'S PART (1)
C*      CALL MOVABS (IIX-63,IIY+3)
C*      PUT THE ALPHANUMERIC CURSOR IN THE NEAREST BOX (2)
C*      CALL TABHOR (IHTBL)
C*            CALL TABVER (IVTBL)
C*      RECORD THE LOCATION OF THE CURSOR AFTER
C*      THE TAB COMMAND HAS BEEN EXECUTED (1)
C*      CALL SEELOC (IA,IB)
C*      HIGHLIGHT THE CHOSEN BLOCK / COMMAND WITH THE FLASHING CURSOR (4)
C*      CALL ANMODE
C*      READ (5,104) IZ

```

```

104 FORMAT(A2)
CALL RECOVER

C* IF HE HAS RESPONDED WITH "SPACE" AND "X"
C* AND AN "E" THEN DO NOT EXECUTE THIS COMMAND
C* RETURN HIM TO THE CURSOR {1}
C* IFE1Z.EQ.1SE130 TO 30

C* ROUTE THE PROGRAM CONTROL TO THE APPROPRIATE CURSOR LOCATION (34)
C* SUBROUTINE BASED ON THE TABBED CURSOR LOCATION (34)

40 IF(I1A.EQ.128.AND.IB.EQ.637) CALL ACZIAG
IF(I1A.EQ.128.AND.IB.EQ.615) CALL ACPIAG
IF(I1A.EQ.128.AND.IB.EQ.593) CALL ARZIAG
IF(I1A.EQ.128.AND.IB.EQ.571) CALL ARPPIAG
IF(I1A.EQ.128.AND.IB.EQ.549) CALL DCZIAG
IF(I1A.EQ.128.AND.IB.EQ.527) CALL DCPPIAG
IF(I1A.EQ.128.AND.IB.EQ.505) CALL DRZIAG
IF(I1A.EQ.128.AND.IB.EQ.483) CALL DRCIAG
IF(I1A.EQ.128.AND.IB.EQ.461) CALL LNUCIAG
IF(I1A.EQ.128.AND.IB.EQ.439) CALL LACZRCT
IF(I1A.EQ.128.AND.IB.EQ.417) CALL ACZRCT
IF(I1A.EQ.128.AND.IB.EQ.395) CALL ARZRCT
IF(I1A.EQ.128.AND.IB.EQ.373) CALL DCZRCT
IF(I1A.EQ.128.AND.IB.EQ.351) CALL DCPRCT
IF(I1A.EQ.128.AND.IB.EQ.329) CALL DRZRCT
IF(I1A.EQ.128.AND.IB.EQ.307) CALL ACZPLR
IF(I1A.EQ.128.AND.IB.EQ.285) CALL ACPPLR
IF(I1A.EQ.128.AND.IB.EQ.263) CALL ARZPLR
IF(I1A.EQ.128.AND.IB.EQ.241) CALL DCZPLR
IF(I1A.EQ.128.AND.IB.EQ.219) CALL DCPPLR
IF(I1A.EQ.128.AND.IB.EQ.197) CALL DRZPLR
IF(I1A.EQ.128.AND.IB.EQ.175) CALL ACZPLR
IF(I1A.EQ.128.AND.IB.EQ.153) CALL ACPPLR
IF(I1A.EQ.128.AND.IB.EQ.131) CALL ARZPLR
IF(I1A.EQ.128.AND.IB.EQ.109) CALL DCZPLR
IF(I1A.EQ.128.AND.IB.EQ.87) CALL DCPPLR
IF(I1A.EQ.128.AND.IB.EQ.65) CALL DRZPLR
IF(I1A.EQ.128.AND.IB.EQ.43) CALL ACZPLR
IF(I1A.EQ.128.AND.IB.EQ.21) CALL ACPPLR
IF(I1A.EQ.128.AND.IB.EQ.9) CALL ARZPLR
IF(I1A.EQ.128.AND.IB.EQ.7) CALL DCZPLR
IF(I1A.EQ.128.AND.IB.EQ.5) CALL DCPPLR
IF(I1A.EQ.128.AND.IB.EQ.3) CALL DRZPLR
IF(I1A.EQ.128.AND.IB.EQ.1) CALL ACZPLR
IF(I1A.EQ.128.AND.IB.EQ.0) CALL ACPPLR
IF(I1A.EQ.128.AND.IB.NE.0) CALL ARZPLR
IF(I1A.EQ.128.AND.IB.NE.0) CALL DCZPLR
IF(I1A.EQ.128.AND.IB.NE.0) CALL DCPPLR
IF(I1A.EQ.128.AND.IB.NE.0) CALL DRZPLR
GO TO 30

SUBROUTINE OLFILTER
END

```

```

COMMON IROOTS(4), POLZRO(20,5), IERROR, IOLD, FLTRGN
CALL MOVABS(126,374)
CALL ANMODE
WRITE(6,100)
FORMAT(6,100)
YOU HAVE AN OLD FILTER THAT YOU WISH TO MODIFY?•
CALL RECOVR
CALL MOVABS(399,330)
CALL ANMODE
WRITE(6,101)
FORMAT(1 TYPE Y OR N)
CALL RECOVR
CALL SCURSR(IN,IX,IV)
IF(IN.NE.121.AND.IN.NE.89)RETURN
DO 10 I=1,20
READ(1,104)(POLZRO(I,J),J=1,5)
10 4 FORMAT(1X,5F12.8)
READ(1,105)(IROOTS(I),I=1,4)
10 5 FORMAT(1X,4I2)
READ(1,106)FLTRGN
10 6 FORMAT(1X,F16.8)
IOLD=1
RETURN
END

SUBROUTINE FINISH
COMMON IROOTS(4), POLZRO(20,5), IERROR, IOLD, FLTRGN
CALL ERASE
CALL ANMODE
REWIND 1
DO 10 I=1,20
WRITE(1,100)(POLZRO(I,J), J=1,5)
10 10 FORMAT(1X,5F12.8)
CONTINUE
10 11 WRITE(1,101)(IROOTS(I),I=1,4)
10 12 FORMAT(1X,4I2)
IF(IOLD.EQ.0)FLTRGN=1.
CALL RECOVR
CALL MOVABS(217,528)
CALL ANMODE
WRITE(6,102)FLTRGN
FORMAT(6,102)
THE FILTER GAIN IS CURRENTLY: •,F12.8
CALL RECOVR
CALL MOVABS(252,484)
CALL ANMODE
WRITE(6,103)
FORMAT(6,103)
YOU WISH TO CHANGE THE FILTER GAIN?•
CALL RECOVR
CALL MOVABS(427,440)

```

```

CALL ANMODE
WRITE(6,104)
FORMAT(1,I10)
104 CALL RECOVER
CALL SCURSR(NEWGN,IX,IY)
CALL ANMODE
IF(INEGN.NE.121.AND.NEGN.NE.89)GO TO 30
CALL RECOVER
CALL MOVABS(182,396)
CALL ANMODE
WRITE(6,106)
FORMAT(1,I10)
106 CALL RECOVER
CALL MOVABS(357,374)
CALL ANMODE
WRITE(6,109)
FORMAT(1,I10)
109 CALL RECOVER
CALL MOVABS(421,330)
CALL ANMODE
READ(5,107) FLTRGN
FORMAT(1I12.8)
107 CALL RECOVER
CALL MOVABS(259,286)
CALL ANMODE
WRITE(6,108) FLTRGN
FORMAT(1X,F16.8)
108 FORMAT(1X,F16.8)
30 CALL ANMODE
WRITE(11,110) FLTRGN
CALL FIN
RETURN
40 END

SUBROUTINE NUC
CALL ERASE
CALL LETTER
CALL BOXUC
CALL PLOTUC
CALL PLTTBL
RETURN
END

SUBROUTINE ACIRCT
COMMON IXXXX(4) PQLZRO(20,5), TERROR
DIMENSION LTRACZ(64)
DATA LTRACZ/4H0A,4H0D,A,4H COM,4HPLEX,4HZER,4HO TO,4H THE
X ,4H ,4HD1SP,4HLAY,4H ENT,4HER T,4HHE R,4HEAL,4HAND
ASDF3481
ASDF3482
ASDF3483
ASDF3484
ASDF3485
ASDF3486
ASDF3487
ASDF3488
ASDF3489
ASDF3480
ASDF3491
ASDF3492
ASDF3493
ASDF3494
ASDF3495
ASDF3496
ASDF3497
ASDF3498
ASDF3499
ASDF3500
ASDF3501
ASDF3502
ASDF3503
ASDF3504
ASDF3505
ASDF3506
ASDF3507
ASDF3508
ASDF3509
ASDF3510
ASDF3511
ASDF3512
ASDF3513
ASDF3514
ASDF3515
ASDF3516
ASDF3517
ASDF3518
ASDF3519
ASDF3520
ASDF3521
ASDF3522
ASDF3523
ASDF3524
ASDF3525
ASDF3526
ASDF3527
ASDF3528

```

```

        *4H '4HIMAG,4HINAR,4HY PA,4HRTS '4HWITH,4HIN T,4HHE B
        *4HOXES '4HPROV,4HIODE,4H EA,4HCH N,4HUMBE,4HR RE,4HQURI
        *4HES A,4HDEC I,4HMA L,4H REA,4HL PA,4HRT M,4HINUS,4H SIG
        *4HNS '4HMUST,4H BE,4H INC L,4HUED,4H WIT,4HHIN,4HTHE
        *4HBOX '4HNOTE,4H AL,4HLC O,4HMPLE,4HNE,4HROES,4H MUS
        *4HTBX E{64},4HIN T,4HEN U,4HNTS,4H OF,4HORIG,
        DATA LTRACZ{64}/4HIN /
CALL LTRACZ{2,2}
IF(IERROR.NE.0)RETURN
      CALL CHCKS{2,2}
      CALL MOVAB{0,528}
DO 30 I=1,57,8
      CALL ANMODE
      WRITE(6,100) (LTRACZ(I+J-1), J=1,8)
      CALL RECOVR
      CALL NEWLN
      FORMAT(21X,8A4)
      CALL NEWLN
      CALL ANMODE
      WRITE(6,101)
      FORMAT(27X,4HREAL,9X,9H IMAGINARY)
      CALL RECOVR
      CALL NEWLN
      CALL ANMODE
      WRITE(6,102)
      FORMAT(34X,5H+/- JJ)
      CALL RECOVR
      CALL MOVABS(320,302)
      CALL DRWREL(0,122)
      CALL DRWREL(0,-122)
      CALL DRWREL(-138,0)
      CALL DRWREL(212,0)
      CALL DRWREL(0,122)
      CALL DRWREL(140,0)
      CALL DRWREL(0,-22)
      CALL DRWREL(-140,0)
      CALL CARTN(0,3)
      CALL ANMODE
      WRITE(6,103)
      FORMAT(22X,>" )
      READ(5,104) X,Y
      FORMAT(F10.7,5X,F10.7)
      CALL RECOVR
      CALL SQRT(X**2+Y**2)*GE .10. )I ERROR=10
      IF(IERROR.NE.0)RETURN
      CALL NEWLN
ASDF3529
ASDF3530
ASDF3531
ASDF3532
ASDF3533
ASDF3534
ASDF3535
ASDF3536
ASDF3537
ASDF3538
ASDF3539
ASDF3540
ASDF3541
ASDF3542
ASDF3543
ASDF3544
ASDF3545
ASDF3546
ASDF3547
ASDF3548
ASDF3549
ASDF3550
ASDF3551
ASDF3552
ASDF3553
ASDF3554
ASDF3555
ASDF3556
ASDF3557
ASDF3558
ASDF3559
ASDF3560
ASDF3561
ASDF3562
ASDF3563
ASDF3564
ASDF3565
ASDF3566
ASDF3567
ASDF3568
ASDF3569
ASDF3570
ASDF3571
ASDF3572
ASDF3573
ASDF3574
ASDF3575
ASDF3576

```

```

CALL NEWLIN
CALL ANMODE
Z=ABS(Y)
WRATE(6,105) X,Z
FORMAT(9X,29HTHE NEW COMPLEX ZERO WILL BE ,F10.7,6H +/- J,F10.7)
105 CALL RECOVER
CALL NEWLIN
CALL ANMODE
WRITE(6,106)
FORMAT(21X,32HIF CORRECT TYPE *Y*, IF NOT *N*.)
106 CALL RECOVER
CALL SCURSR(ICHAR,IX,IY)
IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
CALL NUC
CALL STRRTS(2,1,X,Y)
RETURN
END

SUBROUTINE ACPRCT POLZR(20,5), ERROR
COMMON IX,XX(14) POLZR(64)
DIMENSION LTRACP(64)
DATA LTRACP/4HTO A,4HDD A,4H COM,4HPLEX,4H POL,4HE WI,4HTHIN
X   *4H THE,4HUNIT,4HCIR,4HCLTE,4HENT,4HERT,4HHE R,4HEAL
X   *4H AND,4HIMAG,4HINAR,4H PA,4HRT,4HHE T,4HHE B
X   *4HOES,4HPROV,4HIDED,4H EA,4HRT,4HHE RE,4HQUIR
X   *4HES A,4HDEC1,4HMAI,4H REA,4HL PA,4HRTM,4HINUS,4H SIG
X   *4HNS,4HMUST,4H BE,4HINCCL,4HUDED,4HWIT,4HHIN,4HTHE
X   *4HBOX,4HNODE,4H AL,4HL CO,4HMPLE,4HX PO,4HLES,4HMUST
X   *4H BE,4HLOCA,4HTE,4HINSI,4HDE T,4HHE U,4HNIT,4HCIRC/
X   DATA LTRACP(64)/4HLE
CALL CHCKSZ(2,4)
IF(ERROR.NE.0)RETURN
CALL ERASE
CALL MOVAB(0,528)
DO 30 I=1,5,7,8
CALL ANMODE
WRITE(6,100) I,TRACP(I+J-1), J=1,8
30 CALL RECOVER
CALL NEWLIN
FORMAT(21X,8A4)
300 CALL NEWLIN
CALL ANMODE
WRITE(6,101)
FORMAT(62X,4HREAL,9X,9HIMAGINARY)
101 CALL RECOVER
CALL NEWLIN
CALL ANMODE
WRITE(6,102)

```

```

102 FORMAT (34X, 5H+/- J)
      CALL RECOVR
      CALL MOVABS(320,302)
      CALL DRWREL(0,22)
      CALL DRWREL(138,0)
      CALL DRWREL(0,-22)
      CALL DRWREL(-138,0)
      CALL DRWREL(212,0)
      CALL DRWREL(0,22)
      CALL DRWREL(140,0)
      CALL DRWREL(0,-22)
      CALL DRWREL(-140,0)
      CALL MOVREL(0,3)
      CALL CARTNE
      CALL ANMODE
      WRITE (6,103)
      FORMAT (22X,>')
      READ (5,104) X,Y
      FORMAT (F10.7,5X,F10.7)
      CALL RECOVR
      CALL SQRT(X**2+Y**2)
      GT .1.0) IERROR=10
      IF (IERROR.NE.0) RETURN
      CALL NEWLIN
      CALL NEWLIN
      CALL ANMODE
      Z=ABS(Y)
      WRITE (6,105)
      FORMAT (9X,29HTHE NEW COMPLEX POLE WILL BE ,F10.7,6H +/- J,F10.7)
      CALL RECOVR
      CALL NEWLIN
      CALL ANMODE
      WRITE (6,106)
      FORMAT (21X,32HIF CORRECT TYPE 'Y', IF NOT 'N'.)
      103
      104
      105
      106
      CALL RECOVR
      CALL SCURSR(ICHAR,IX,IY)
      IF (ICHAR.NE.121.AND.ICHAR.NE.89) GO TO 10
      CALL NUCRL
      CALL STRITS(4,1,X,Y)
      RETURN
      END

      SUBROUTINE ARZCT
      COMMON IXXX,XXX(4),POLZRO(20,5),IERROR
      DIMENSION LTRARZ(64)
      DATA LTRARZ/4HTO A,4HDD A,4H REA,4HL ZE '4HRO T,4HO TH,4HE DI
      X '4HS- '4HPLAY '4H ENT '4HER T,4H HEAL '4HPART,4H WIT
      X '4HHIN '4HTHE '4HBOX '4HPROV '4HIDED '4H TH,4HE NU,4H MEMBER
      X ,4H IS ,4HTO 1,4HNCLU,4HDE A,4H DEC,4H IMAL,4H AND,4H MIN

```

```

        '4HUS   ,4HSIGN,4H AS, '4HAPPR,4HOPRI,4HATE, '4H TH,4HE BO
        '4HX    ,4HMUST,4H CUN,4HTAIN,4H SIG,4HN D,4HECIM,4HAL A
        '4HND   ,4HNUMB,4HER NOT,4HE T,4HHE M,4HAGNI,4HTUDE
        '4H OF   ,4HTHE 4H MUS,4H MUS,4H BE,4H LES,4HS TH,4HEN T /
        DATA LTRARZ(64)/4HEN. /
        IF(IERROR.NE.0) RETURN
        CALL ERASE
        CALL MOVABS(0,528)
        DO 30 I=1,57,8
        CALL ANMODE
        WRITE(6,100) LTRARZ(I+J-1), J=1,8
        CALL RECOVR
        CALL NEWLIN
        CALL FORMAT(21X,8A4)
        CALL NEWLIN
        CALL ANMODE
        WRITE(6,101)
        FORMAT(27X,4HREAL)
        CALL RECOVR
        CALL NEWLIN
        CALL MOVABS(320,302)
        CALL DRWREL(0,22)
        CALL DRWREL(138,0)
        CALL DRWREL(0,-22)
        CALL DRWREL(-138,0)
        CALL CARTN
        CALL ANMODE
        WRITE(6,103)
        FORMAT(22X,1>)
        READ(5,104)
        FORMAT(10,7)
        CALL RECOVR
        IF(IABS(X).GE.10) IERROR=12
        IF(IERROR.NE.0) RETURN
        CALL NEWLIN
        CALL NEWLIN
        CALL ANMODE
        Z=0
        WRITE(6,105)
        FORMAT(15X,1>)
        CALL RECOVR
        CALL NEWLIN
        CALL ANMODE
        WRITE(6,106)
        FORMAT(21X,32HIF CORRECT TYPE *Y*, IF NOT *N*.)
        CALL RECOVR
ASDF3673
ASDF3674
ASDF3675
ASDF3676
ASDF3677
ASDF3678
ASDF3679
ASDF3680
ASDF3681
ASDF3682
ASDF3683
ASDF3684
ASDF3685
ASDF3686
ASDF3687
ASDF3688
ASDF3689
ASDF3690
ASDF3691
ASDF3692
ASDF3693
ASDF3694
ASDF3695
ASDF3696
ASDF3697
ASDF3698
ASDF3699
ASDF3700
ASDF3701
ASDF3702
ASDF3703
ASDF3704
ASDF3705
ASDF3706
ASDF3707
ASDF3708
ASDF3709
ASDF3710
ASDF3711
ASDF3712
ASDF3713
ASDF3714
ASDF3715
ASDF3716
ASDF3717
ASDF3718
ASDF3719
ASDF3720

```

```

CALL SCURSR(ICHAR(IY),CHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
IF(CHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
CALL NUC
CALL STRRTS(1,1,X,0,0)
RETURN
END

SUBROUTINE ARPRCT
COMMON IXXXXXX(4) POLZRD(20,5),IERROR
DIMENSION LTRARP(64)
DATA LTRARP/4HTO A,4H DD A,4H REA,4H PD,4H LE T,4H MO TH,4H E DI
        '4H S-      '4H ENT,4H HER T,4H HEAL R,4H HE R,4H PART,4H WIT
        '4H HIN '4H THE '4H PROV,4H IDED,4H TH,4H HE NU,4H MEMBER
        '4H NCGLU,4H DE A,4H DEC,4H IMAL,4H AND,4H MIN
        '4H IS   '4H TO 1,4H HBOX,4H DED,4H DEC,4H IMAL,4H AND,4H MIN
        '4H HUS '4H SIGN,4H AS,4H APPR,4H PR,4H HATE,4H TH,4H HE BO
        '4H X    '4H MUST,4H CON,4H TAIN,4H SIG,4H HN,4H ECIM,4H HAL A
        '4H NDB '4H NUMB,4H HER,4H NOT,4HE: T,4H E M,4H HAGNI,4H TUDE,
        '4H OF  '4H THE,4H POLE,4H MUS,4H HT BE,4H ONE,4H OR,4H LESS,/ /
DATA LTRARP(64)/4H.
CALL CHCKSZ(1,3)
IF(IERROR.NE.0)RETURN
CALL ERASE
CALL MOVABS(0,528)
DO 30 I=1,57,8
CALL ANMODE
WRITE(6,100)(LTRARP(I+J-1),J=1,8)
30   FORMAT(1X,8A4)
CALL NEWLIN
CALL ANMODE
WRITE(6,101)
FORMAT(12X,4HREAL)
101  CALL RECOVR
CALL NEWLIN
CALL MOVABS(320,302)
CALL DRWREL(0,12,2)
CALL DRWREL(138,0)
CALL DRWREL(0,12,2)
CALL DRWREL(-138,0)
CALL MOVREL(0,3)
CALL CARTN
CALL ANMODE
WRITE(6,103)
FORMAT(122X,>'')
103  READ(5,104)
FORMAT(F10.7)
CALL RECOVR

```

```

IF(ABS(X).GT.1.0)IERROR=13
IF(IERROR.NE.0)CALL ERROR
IF(IERROR.NE.0)RETURN
CALL NEWLIN
CALL NEWLIN
CALL ANMODE
Z=0
WRITE(6,105) X,Z
FORMAT(15X,26H THE NEW REAL POLE WILL BE ,F10.7,3H +J,F10.7)
CALL RECOVR
CALL NEWLIN
CALL ANMODE
WRITE(6,106)
FORMAT(21X,32H IF CORRECT TYPE 'Y', IF NOT 'N' .)
CALL RECOVR
CALL SCURSR(ICHAR IX,IY)
IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
CALL NUC
CALL STRRTS(3,1,X,0.)
RETURN
END

105
      WRITE(6,105) X,Z
      FORMAT(15X,26H THE NEW REAL POLE WILL BE ,F10.7,3H +J,F10.7)

106
      WRITE(6,106)
      FORMAT(21X,32H IF CORRECT TYPE 'Y', IF NOT 'N' .)
      CALL RECOVR
      CALL SCURSR(ICHAR IX,IY)
      IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
      CALL NUC
      CALL STRRTS(3,1,X,0.)
      RETURN
END

SUBROUTINE DCZRCT
COMMON IXXX(4), POLZERO(20,5), IERROR
DIMENSION LTRDCZ(64)
DATA LTRDCZ/4H0D,4HELT,4HEA,4HCOMP,4HLEX,4HZERO,4HFRO,
        4HDISP,4HLEY,4HCENT,4HERT,4HHE,4HX,A,
        4HND,4HTHE,4HTE,4HCOOR,4HOINA,4HTES,4HOF,4HPO,4HN,
        4HFEAR,4HNE,4HOF,4HHE,4HOTS,4HTO,4HREF,4HELFT,
        4HED,4HENT,4HR,4HSE,4HVALU,4HES,W,4HITHI,4HN,
        4HE,4HB0XE,4HS,4HNCLU,4HDE,4HDEC,4HIMAL,4HAN,
        4HNO,4HMINU,4HS,4HGN,4HS,4HAP,4HROP,4HRIAT,4HE,
        4HSIGN,4HIND,4HICAT,4HES,P,4HOSIT,4HIVE,4HVALU/
        DATA LTRDCZ(64)/4HES./
        CALL CHKCSZ(-1,2)
        IF(IERROR.NE.0)RETURN
        CALL ERASE
        DO 30 I=1,57,8
        CALL ANMODE
        WRITE(6,100)(LTRDCZ(I+J-1), J=1,8)
30      CALL RECOVR
        CALL NEWLIN
        FORMAT(21X,8A4)
        CALL NEWLIN
        CALL ANMODE
        WRITE(6,101)
        FORMAT(29X,X,12X,'Y')
100
101

```

```

CALL RECOVER
CALL NEWLIN
CALL NOVABS(320,302)
CALL DRWREL(0,22)
CALL DRWREL(138,0)
CALL DRWREL(0,-22)
CALL DRWREL(-138,0)
CALL MOVREL(184,0)
CALL DRWREL(0,22)
CALL DRWREL(140,0)
CALL DRWREL(0,-22)
CALL DRWREL(-140,0)
CALL MOVREL(0,3)
CALL CARTN
CALL ANMODE
WRITE(6,103)
FORMAT(22X,'>')
103 READ(5,104) X,Y
FORMAT(F10.7,5X,F10.7)
CALL RECOVER
CALL LOCATE(12,X,Y,LINEPZ)
CALL NEWLIN
CALL NEWLIN
CALL ANMODE
WRITE(6,105) POLZRO(LINEPZ),PAIR WILL BE ,F10.7,6H +/- J ,F10.7)
104 CALL RECOVER
CALL NEWLIN
CALL ANMODE
WRITE(6,106)
FORMAT(21X,32HIF CORRECT TYPE *Y*, IF NOT *N*.)
105 CALL RECOVER
CALL SCURR(ICHAR,IX,IY)
IF(ICHAR.NE.89)GO TO 10
CALL UPDATE(2,LINEPZ)
CALL NUC
RETURN
END
106

```

XXXXXX

```

SUBROUTINE DCPRCT(POLZRO(20,5),IERROR
COMMON IX,XX(4),POLZRO,DIMENSION LTRDCP(64)
DATA LTRDCP/4HTO D,4HELT,4HE A,4HCOMP,4HLEX,4HPOLE,4H FRO
        4H CIR,4HLE,4H ENT,4HER T,4HHE P
        4H H,4HTHE,4HUNIT,4HCOR,4HDINA,4HTESES,4HOF T,4HHE P
        4HXX,4HINT,4HNEAR,4H ONE,4H OF,4HROOT,4H THE,4HS TO,4H BE
        4HOELT,4HETED,4H EN,4HTER,4HES 1,4HNVALU,4H THE,4H TH
        4HE ,4HBOXE,4HS. 1,4HNCLU,4HDE A,4H DEC,4HIMAL,4H, AN
ASDF3817
ASDF3818
ASDF3819
ASDF3820
ASDF3821
ASDF3822
ASDF3823
ASDF3824
ASDF3825
ASDF3826
ASDF3827
ASDF3828
ASDF3829
ASDF3830
ASDF3831
ASDF3832
ASDF3833
ASDF3834
ASDF3835
ASDF3836
ASDF3837
ASDF3838
ASDF3839
ASDF3840
ASDF3841
ASDF3842
ASDF3843
ASDF3844
ASDF3845
ASDF3846
ASDF3847
ASDF3848
ASDF3849
ASDF3850
ASDF3851
ASDF3852
ASDF3853
ASDF3854
ASDF3855
ASDF3856
ASDF3857
ASDF3858
ASDF3859
ASDF3860
ASDF3861
ASDF3862
ASDF3863
ASDF3864

```

```

        '4HMINU,4HS SI,'4HGN A,'4HS AP,'4HPROP,'4HRIAT,'4HE
        '4HSIGN'4H IND,'4HICAT,'4HES P,'4HOSIT,'4HIVE,'4HVÁLU/
        /'4HND LTRDCP{64}/4HES.
        CALL CHCKSZ{-1,4}
        IF(1)ERROR=NE.0}RETURN
        CALL ERASE{0,528}
        DO30 I=1,5,8
        CALL MOVAB{0,528}
        CALL ANMODE
        WRITE{6,100}{ILTRDCP(I+J-1), J=1,8}
        CALL NEWLIN
        CALL RECOVR
        WRITE{6,101}
        FORMAT{2IX,12X, *Y*}
        CALL RECOVR
        CALL NEWLIN{320,302}
        CALL DRWREL{0,2,1}
        CALL DRWREL{1,3,8,2,0}
        CALL DRWREL{0,-2,2,1}
        CALL DRWREL{-1,3,8,0,1}
        CALL MOVREL{184,2,0,1}
        CALL DRWREL{0,2,2,1}
        CALL DRWREL{1,4,0,2,0,1}
        CALL DRWREL{0,-2,2,1}
        CALL DRWREL{-1,4,0,0,1}
        CALL CARTN
        CALL ANMODE
        WRITE{6,103}
        FORMAT{22X,>'1}
        READ{5,104},X,Y
        FORMAT{F10.7,5X,F10.7}
        CALL RECOVR
        CALL LOCATE{4,X,Y,LINEPZ}
        CALL NEWLIN
        CALL ANMODE
        WRITE{6,105}{POLZROSLINEPZ,1} POLZROLLINEPZ{2}
        FORMATE{105,26HDELETED POLÉ PAIR WILL BE ,F10.7,6H +/- J,F10.7}
        CALL RECOVR
        CALL LOCATE{4,X,Y,LINEPZ}
        CALL NEWLIN
        CALL ANMODE
        WRITE{6,106}

```

```

106  FORMAT(21X,3HIF CORRECT TYPE 'Y', IF NOT 'N'.)
      CALL RECOVR
      CALL SCURSR(ICHAR,IX,IY)
      IF(ICHAR.NE.121)AND(ICHAR.NE.89)GO TO 10
      CALL UPDATE(4,LINEPZ)
      CALL NUC
      RETURN
      END

```

```

SUBROUTINE DRZRCT
COMMON IXXXX(4),POLZRO(20,5),IERROR
DIMENSION LTRDRZ(64)
DATA LTRDRZ/4HTO D,4HELET,4HE A,4HREAL,4H ZER,4HO, FR,4HOM T
      X   '4HHE, '4HHER, '4HENT, '4HREAL, '4H ZER, '4HHE, '4H C, '4HODD
      X   '4HIN-, '4HISP, '4HLAY, '4HENT, '4HHER, '4HHE, '4H C, '4H
      X   '4HTO, '4HOF A, '4HPO I, '4HNT N, '4HENT, '4HHER, '4HHE, '4H ROOT
      X   '4HBE D, '4HED, '4HLET, '4HED, '4HENT, '4HHER, '4HHE, '4H VALUE
      X   '4HWITH, '4HINT, '4HHE B, '4HDX, '4HROVI, '4HD ED, '4H INC
      X   '4HLUDE, '4HDE, '4HCIMA, '4HND M, '4HN M, '4HND M, '4HN AS
      X   '4HAPR, '4HDE, '4HATE, '4HNO, '4HSIG, '4HN IN, '4H INDICA,
      X   '4HTES, '4HPO, '4HOPRI, '4HATE, '4HNO, '4HSIG, '4HN IN, '4H /
      DATA LTRDRZ(64)/4H
      CALL CHCKSZ(-1)
      IF(IERRQR.NE.0)RETURN
      10 CALL ERASE
      CALL MOVABS(0,528)
      DO 30 I=1,57,8
      CALL ANMODE
      WRITE(6,100)(LTRDRZ(I+J-1),J=1,8)
      30 CALL RECOVR
      CALL NEWLIN
      100 FORMAT(21X,8A4)
      CALL NEWLIN
      CALL ANMODE
      WRITE(6,101)
      101 FORMAT(28X1;X1)
      CALL RECOVR
      CALL NEWLIN
      CALL MOVABS(320,302)
      CALL DRWREL(0,22)
      CALL DRWREL(1,38,10)
      CALL DRWREL(0,1-22)
      CALL DRWREL(-1,38,0)
      CALL MOVREL(0,3)
      CALL CARTNE
      CALL ANMODE
      WRITE(6,103)
      103 FORMAT(22X,>'1

```

```

      READ(5,104) X
      FORMAT(F10.7)
      CALL RECOVR
      CALL LOCATE(1,X,0.,LINEPZ)
      CALL NEWLIN
      CALL ANMODE
      Z=0
      WRITE(6,105) POLZRO(LINEPZ,1),POLZRO(LINEPZ,2)
104   FORMAT(15X,'26HDELETED REAL ZERO WILL BE ',F10.7,3H +J,F10.7)
      CALL RECOVR
      CALL NEWLIN
      CALL ANMODE
      WRITE(6,106)
105   FORMAT(2IX,32HIF CORRECT TYPE 'Y'. IF NOT 'N'.)
      CALL SCURS(ICHAR'IX',IV)
      IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
      CALL UPDATE(I,LINEPZ)
      CALL NUC
      RETURN
      END

106   FORMAT(2IX,32HIF CORRECT TYPE 'Y'. IF NOT 'N'.)
      CALL RECOVR
      CALL SCURS(ICHAR'IX',IV)
      IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
      CALL UPDATE(I,LINEPZ)
      CALL NUC
      RETURN
      END

      SUBROUTINE DRPRCT
COMMON IXXXX(4),POLZRO(20,5),IERROR
      DIMENSION LTRDRP(64)
      DATA LTRDRP/4HTO D,4HELT '4HE A, '4HREAL, '4H POL, '4HE FR, '4HOM T
      X '4HHE '4HENT, '4H CIR, '4HCLC, '4H ER T, '4HHE '4HX C
      X '4HOR, '4HDINA, '4HTE O, '4HFA, '4HPOIN, '4H HAR T, '4HHE R
      X '4HOOT, '4HTO B, '4HE DE, '4HLE, '4HD E, '4HINTER, '4H THE, '4H VAL
      X '4HUE, '4HWIT, '4HIN T, '4HHE B, '4HDX P, '4HROVI, '4HDED, '4H INC
      X '4HLUDE, '4HA DE, '4HCIMA, '4HLCMA, '4HNUS, '4HN AS
      X '4HAPPR, '4HOPRI, '4HATE, '4H NO, '4H SIG, '4HN IN, '4HICA /
      X '4HTEST, '4HAPPO, '4HSITI, '4HVALE, '4H, '4H
      DATA LTRDRP(64)/4H /
      IF(IERROR.NE.0)RETURN
10     CALL CHCKSZ(-1,3)
      CALL ERASE(0,528)
      DO 30 I=1,57,8
      CALL MOVAB(S(0,528)
      CALL RECOVR
      WRITE(6,100)(LTRDRP(I+J-1), J=1,8)
30     CALL NEWLIN
      CALL ANMODE
      WRITE(6,101)
100    FORMAT(12IX,8A4)
      CALL NEWLIN
      CALL ANMODE
      WRITE(6,101)
      ASDF3961
      ASDF3962
      ASDF3963
      ASDF3964
      ASDF3965
      ASDF3966
      ASDF3967
      ASDF3968
      ASDF3969
      ASDF3970
      ASDF3971
      ASDF3972
      ASDF3973
      ASDF3974
      ASDF3975
      ASDF3976
      ASDF3977
      ASDF3978
      ASDF3979
      ASDF3980
      ASDF3981
      ASDF3982
      ASDF3983
      ASDF3984
      ASDF3985
      ASDF3986
      ASDF3987
      ASDF3988
      ASDF3989
      ASDF3990
      ASDF3991
      ASDF3992
      ASDF3993
      ASDF3994
      ASDF3995
      ASDF3996
      ASDF3997
      ASDF3998
      ASDF3999
      ASDF4000
      ASDF4001
      ASDF4002
      ASDF4003
      ASDF4004
      ASDF4005
      ASDF4006
      ASDF4007
      ASDF4008

```

```

101   FORMAT(28X,'X')
      CALL RECOVR
      CALL NEWLIN
      CALL MOVABS(320,302)
      CALL DRWREL(0,22)
      CALL DRWREL(138,0)
      CALL DRWREL(0,-22)
      CALL DRWREL(-138,0)
      CALL MOVREL(0,3)
      CALL CARTNE
      CALL ANMODE
      CALL RECOVR
      WRITE(6,103)
      FORMAT(12,2X,1,>,*)
      READ(5,104)
      FORMAT(F10.7)
      CALL RECOVR
      CALL LOCATE(3,X,0.,LINEPZ)
      CALL NEWLIN
      CALL ANMODE
      WRITE(6,105)
      FORMAT(15X,1POLZR0(LINEPZ,1)POLZR0(LINEPZ,2),
             12HDELETED REAL POLE WILL BE ,F10.7,3H +J,F10.7)
      CALL RECOVR
      CALL NEWLIN
      CALL ANMODE
      WRITE(6,106)
      FORMAT(21X,32H IF CORRECT TYPE 'Y', IF NOT 'N' .)
      CALL RECOVR
      CALL SCUR(CHAR,IX,IV)
      IF(CHAR.NE.'12')AND.(CHAR.NE.'89')GO TO 10
      CALL UPDATE(3,LINEPZ)
      CALL NUC
      RETURN
      END

105
106
      SUBROUTINE ACZPLR POLZR0(20,5),IERROR
      COMMON IXXXXX(4) POLZR0(20,5)
      DIMENSION LTPACZ(64)
      DATA LTPACZ/4HDD,A,4H COM,4HPLEX,4H ZER,4H
      X           4H    4H    4H    4H    4H    4H    4H    THE
      X           4H    4HD   4HD   4H    4H    4H    4H    HADIA,4H
      X           4H    4H    4H    4H    4H    4H    4H    AN
      X           4H    4H    4H    4H    4H    4H    4H    ENT,4H
      X           4H    4H    4H    4H    4H    4H    4H    HER,4H
      X           4H    4H    4H    4H    4H    4H    4H    E R,4H
      X           4H    4H    4H    4H    4H    4H    4H    MPON,4H
      X           4H    4H    4H    4H    4H    4H    4H    ENT,4H
      X           4H    4H    4H    4H    4H    4H    4H    WHIT,4H
      X           4H    4H    4H    4H    4H    4H    4H    PROV
      X           4H    4H    4H    4H    4H    4H    4H    HAGNI,4H
      X           4H    4H    4H    4H    4H    4H    4H    HIN,4H
      X           4H    4H    4H    4H    4H    4H    4H    HROV
      X           4H    4H    4H    4H    4H    4H    4H    HOF
      X           4H    4H    4H    4H    4H    4H    4H    UDDE,4H
      X           4H    4H    4H    4H    4H    4H    4H    HETA,4H
      X           4H    4H    4H    4H    4H    4H    4H    RAD
      X           4H    4H    4H    4H    4H    4H    4H    HADI
      X           4H    4H    4H    4H    4H    4H    4H    RES,4H
      X           4H    4H    4H    4H    4H    4H    4H    A D,4H
      X           4H    4H    4H    4H    4H    4H    4H    HECIM
      X           4H    4H    4H    4H    4H    4H    4H    MIN,4H
      X           4H    4H    4H    4H    4H    4H    4H    HUS
      X           4H    4H    4H    4H    4H    4H    4H    BOX,4H
      DATA LTPACZ(64)/4HES.
      CALL CHCKS2(2,2)

```

```

10      IF( IERROR.NE.0 ) RETURN
        CALL ERASE S(0, 528)
        DO 30 I=1,57,8
          CALL ANMODE
          WRITE(6,100) (LTPACZ(I+J-1), J=1,8)
30      CALL RECOVR
        CALL NEWLIN
        FORMAT(2IX,8A4)
100     CALL NEWLIN
        CALL ANMODE
        WRITE(6,101)
        FORMAT(25X,'MAGNITUDE', 8X, 'ANGLE')
101     CALL RECOVR
        CALL NEWLIN
        CALL ANMODE
        WRITE(6,102)
        FORMAT(134X,3H+/-)
        CALL RECOVR
        CALL ANGLE(504,304)
        CALL MOVABS(320,302)
        CALL DRWREL(0,22)
        CALL DRWREL(138,20)
        CALL DRWREL(0,-22)
        CALL DRWREL(-138,0)
        CALL MOVREL(212,0)
        CALL DRWREL(0,22)
        CALL DRWREL(140,20)
        CALL DRWREL(0,-22)
        CALL MOVREL(-140,0)
        CALL CARTN
        CALL ANMODE
        WRITE(6,103)
        FORMAT(22X,0)
        READ(5,104) RHO, THETA
104     FORMAT(F10.7,5X,F10.7)
        CALL RECOVR
        IF( RHO.GE.10 ) IERROR=14
        IF( IERROR.NE.0 ) CALL ERROR
        IF( IERROR.NE.0 ) RETURN
        CALL NEWLIN
        CALL ANMODE
        WRITE(6,105)
        THETA=ABS(THETA)
        WRITE(6,105) RHO, THETA
        FORMAT(9X,3OH) THE NEW COMPLEX ZEROS WILL BE ,F10.7,6H +/- ,F10.7)
105     CALL RECOVR

```

```

CALL ANGLE( 727,260)
CALL NEWLIN
CALL ANMODE
WRITE(6,106)
FORMAT(21X,32HIF CORRECT TYPE 'Y', IF NOT 'N'.)
CALL RECOVR
CALL SCURSR(ICHAR IX,1Y)
IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
CALL NUC
CALL STRRTS(2,2,RHO,THETA)
RETURN
END

SUBROUTINE ACPLR
COMMON IXXX(4),POLZRO(20,5),ERROR
DIMENSION LTPACP(64)
DATA LTPACP/4H0 A,4HDD A,4H COM,4HPLEX,4H POL,4HE WI,4HTHIN
      ,4HS CIR,4HCL E,4HEN TE,4HR TH,4HE RA,4HDIAL,
      ,4H THE,4HUNLT,4H CO,4HMPOL,4HMMUST,4H WIT,4H HIN,4HPROV
      ,4H AND,4HTHET,4HS,4HS,4HRHO,4HMUST,4H BE,4H HONE,4HORL
      ,4H IDE,4HBXOE,4HS,4HHE,EN,4HTE,4H RAD
      ,4H ESS,4HTHET,4HS MU,4HST B,4HE EN,4HTERE,4H IN,4H
      ,4H IANS,4HEACH,4H NUM,4HBER R,4HREQU,4HIRE S,4H A D,4HECIM
      ,4HALGN,4HAND,4HAS A,4HPPRO,4HPRIA,4HTE A,4H MIN,4HUS S
      ,4HIGN,4HBOT,4H ARE,4H CON,4HFINE,4HD TO,4H THE,4H BOX/
      DATA LTPACP/64/4HES.
CALL CHCKSZ(2,4)
IF(IER2.NE.0)RETURN
CALL ERASE
10 CALL NEWLIN
DO 30 I=1,57,8
CALL ANMODE
WRITE(6,100)(LTPACP(I+J-1), J=1,8)
CALL RECOVR
30 FORMAT(21X,8A4)
CALL NEWLIN
CALL ANMODE
WRITE(6,101)
FORMAT(21X,8A4)
CALL RECOVR
CALL NEWLIN
CALL ANMODE
WRITE(6,102)
FORMAT(21X,8A4)
CALL RECOVR
CALL NEWLIN
CALL ANMODE
101 FORMAT(34X,3H#/-)
CALL RECOVR
CALL ANGLE(504,304)
CALL MOVABS(320,302)
CALL DRWREL(0,2)
102 FORMAT(34X,3H#/-)
CALL RECOVR
CALL ANGLE(504,304)
CALL MOVABS(320,302)
CALL DRWREL(0,2)

```

```

CALL DRWREL(138,0)
CALL DRWREL(0,138,0)
CALL DRWREL(-138,0)
CALL MOVREL(212,0)
CALL DRWREL(0,212,0)
CALL DRWREL(140,0)
CALL DRWREL(0,140,0)
CALL DRWREL(-140,0)
CALL MOVREL(0,3)
CALL CARTN
CALL ANMODE
WRITE(6,103)
FORMAT(2,2X,'')
READ(5,104) RHO, THETA
FORMAT(6,105) RHO, THETA
WRITE(6,105) RHO, THETA
CALL RECOVR
CALL RECOVR
IF(RHO.GT.1.0) IERROR=15
IF(IERROR.NE.0) RETURN
CALL NEWLIN
CALL NEWLIN
CALL ANMODE
THETA=ABS(THETA)
WRITE(6,105) RHO, THETA
FORMAT(6,105) RHO, THETA
NEWLINE
CALL RECOVR
CALL RECOVR
CALL ANGLE(727,260)
CALL NEWLIN
CALL ANMODE
WRITE(6,106)
FORMAT(2,1X,32HIF CORRECT TYPE 'Y', IF NOT 'N'.)
104 CALL RECOVR
CALL SCURSR(ICHAR,IX,IY)
IF(ICHAR.NE.121.AND.ICHAR.NE.89) GO TO 10
CALL NUC
CALL STRRTS(4,2,RHO,THETA)
RETURN
END

105
106

```

```

COMMON IXXXX(14) POLZRO(20,5),IERROR
DIMENSION LTPARZ(64)
DATA LTPARZ/4HTO A,4HDD A,4H REA,4HL ZE,4HRO T,4HO TH,4HE DI
      '4HS-,4HPLAY,4H EN,4HTER,4H HE,4HVALU,4HE OF,4H RHO
      '4H IN,4HTHE,4HBOX,4HIDED,4H TH,4HE MA,4HGNIT
      '4HDE,4H HUDE,4HOF R,4HHO M,4HUST,4HESSE,4H THAN,4H TEN
      '4H THE,4HNUMB,4HER,4HINCL,4HDE,4H CIMA,4HL AN
      '4HD,4HSIGN,4HAS,4HAPP,4HOPRI,4HATE,4HMUST,4H BE
      '4HCON-,4HTAIN,4HED W,4HITHI,4HN TH,4HE BO,4HNO S
      XXXXXXXXX

```

```

X DATA '4HIGN 14HINDI,4HCATE,4HS A ,4HPOSI,4HTIVE,4H VAL,4HUE. / ASDF4201
CALL CMCKSZ(1,1) ASDF4202
IF(IERROR.NE.0)RETURN ASDF4203
CALL ERASE ASDF4204
CALL MOVABS(0,528) ASDF4205
DO 30 I=1,5,8 ASDF4206
CALL ANMODE ASDF4207
WRITE(6,100)(LTPARZ(I+J-1),J=1,8) ASDF4208
CALL RECOVR ASDF4209
CALL NEWLIN ASDF4210
FORMAT(21X,8A4) ASDF4211
30 CALL NEWLIN ASDF4212
FORMAT(21X,8A4) ASDF4213
CALL NEWLIN ASDF4214
CALL ANMODE ASDF4215
WRITE(6,101) ASDF4216
FORMAT(25X,MAGNITUDE*) ASDF4217
CALL RECOVR ASDF4218
CALL NEWLIN ASDF4219
CALL MOVABS(320,302) ASDF4220
CALL DRWREL(0,38,0) ASDF4221
CALL DRWREL(138,0) ASDF4222
CALL DRWREL(0,-22) ASDF4223
CALL DRWREL(-138,0) ASDF4224
CALL MOVREL(0,3) ASDF4225
CALL CARTN ASDF4226
CALL ANMODE ASDF4227
WRITE(6,103) ASDF4228
FORMAT(22X,>) ASDF4229
READ(5,104),RHO ASDF4230
FORMAT(F10.7) ASDF4231
104 IF(RHO.GT.1.0) IERROR=16 ASDF4232
IF(IERROR.NE.0)RETURN ASDF4233
CALL NEWLIN ASDF4234
CALL NEWLIN ASDF4235
CALL ANMODE ASDF4236
THETA=0. ASDF4237
WRITE(6,105) RHO, THETA ASDF4238
FORMAT(6,12X,26HTHE NEW REAL ZERO WILL BE ,F10.7,3X,F10.7) ASDF4239
CALL RECOVR ASDF4240
CALL ANGLE(677,260) ASDF4241
CALL NEWLIN ASDF4242
CALL ANMODE ASDF4243
WRITE(6,106) ASDF4244
FORMAT(21X,32HIF CORRECT TYPE 'Y', IF NOT 'N') ASDF4245
CALL RECOVR ASDF4246
CALL SCURS(ICHAR,'X',LY) ASDF4247
IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10 ASDF4248

```

```

CALL NUC
CALL STRRTS(1,2,RHO,0.)
RETURN
END

```

```

ASDF4249
ASDF4250
ASDF4251
ASDF4252
ASDF4253
ASDF4254
ASDF4255
ASDF4256
ASDF4257
ASDF4258
ASDF4259
ASDF4260
ASDF4261
ASDF4262
ASDF4263
ASDF4264
ASDF4265
ASDF4266
ASDF4267
ASDF4268
ASDF4269
ASDF4270
ASDF4271
ASDF4272
ASDF4273
ASDF4274
ASDF4275
ASDF4276
ASDF4277
ASDF4278
ASDF4279
ASDF4280
ASDF4281
ASDF4282
ASDF4283
ASDF4284
ASDF4285
ASDF4286
ASDF4287
ASDF4288
ASDF4289
ASDF4290
ASDF4291
ASDF4292
ASDF4293
ASDF4294
ASDF4295
ASDF4296

SUBROUTINE ARPPLR
COMMON IXXXX(4),POLZRO(20,5),IERROR
DIMENSION LTPARP(64)
DATA LTPARP/4HTDA,4HDDA,4HREA,4HREAL,4HVAL,4HUEI,
X '4HS-' '4HPLAY,4HEN,4HERA,4HVAL,4HUEI,4HFDI
X X '4HONE '4HDL,'4HESL,'4HIN,'4HTHE,'4HBOX,'4HIDED
X X X '4HTHE,'4HNUMB,'4HERA,'4HINC,'4HDE,'4HCIMA
X X X '4HL '4HSIGN,'4HAS,'4HAPPR,'4HOPRI,'4HHMUST
X X X '4HBE '4HANDN,'4HAIN,'4HDWI,'4HTHIN,'4HTHE,'4HBOX,'4H
X X X '4HUST '4HBE,'4HNE,4H:TH,4HEWA,4HGNIT,'4HDE,'4HOFR,'4HHO M /
X X X DATA LTPARP(64)/4H
CALL CHCKSZ(1,3)
IF(IERROR.NE.0)RETURN
10 CALL ERASE
CALL MOVAB(0,528)
DO 30 I=1,2,8
CALL ANMODE
WRITE(6,100)(LTTPARP(I+J-1),J=1,8)
CALL RECDVR
CALL NEWLIN
FORMAT(2IX,8A4)
CALL NEWLINE
CALL ANMODE
WRITE(6,101)
30 FORMAT(25X,'MAGNITUDE')
101 CALL RECOVR
CALL NEWLIN
CALL MOVAB(320,302)
CALL DRWREL(0,2,2)
CALL DRWREL(1,38,0)
CALL DRWREL(0,1-2,2)
CALL DRWREL(-1,38,0)
CALL MOVREL(0,3)
CALL CARTN
CALL ANMODE
WRITE(6,103)
103 FORMAT(22X,'>')
READ(5,104) RHO
104 FORMAT(F10.7)
CALL RECOVR
IF(RHO.GT.1.0)IERROR=17
IF(IERROR.NE.0)RETURN

```

```

CALL NEWLIN
CALL NEWLIN
CALL ANMODE
THETA=0.105 RHO THETA
FORMAT(12X,12X) NEW REAL POLE WILL BE ,F10.7,3X,F10.7)
105 CALL RECOVR
CALL ANGLE(677,260)
CALL NEWLIN
CALL ANMODE
WRITE(6,106)
FORMAT(21X,32HIF CORRECT TYPE 'Y', IF NOT 'N' .)
106 CALL RECOVR
CALL SCURSR(ICHAR'IX',Y)
IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
CALL NUC
CALL STRRTS(3,2,RHO,0.)
RETURN
END

SUBROUTINE DCZPLR
COMMON IXXXX(4),POLZR(20,5),IERROR
DIMENSION LTPDCZ(64)
DATA LTPDCZ/4HTO 0,4HELT,4HE A * 4HCOMP,4HLEX,4HZERO,4H
X FRO
X '4HM '4HTHE ,4HCOOR,4HDINA,4HES '4HENT,4HES '4H
X AND '4HTA,4HNEAR,4H ONE '4HDELT-'4HDEL-'4HETED,4H
X HDEL-'4HBOXE,4HS '4HINC L,4HDE '4HCLIMA,4HL, A
X '4HTHE '4HNU '4HS '4HN '4HDE '4HDE '4H
X '4HND '4HNU '4HS '4HN '4HDE '4HDE '4H
X '4HNO '4HSIGN '4H IND,4HICAT,4HES P,4HOSIT,4HIVE,4HVLU/
DATA LTPDCZ(64)/4HES /
CALL CHCKSZ(-1,2)
IF(IERROR.NE.0)RETURN
10 CALL ERASE
CALL MOVABS(0,528)
DO 30 I=1,5,8
CALL ANMODE
WRITE(6,100)(LTPDCZ(I+J-1),J=1,8)
30 CALL RECOVR
CALL NEWLIN
FORMAT(21X,8A4)
CALL NEWLIN
CALL ANMODE
WRITE(6,101)
FORMAT(21X,RHO,12X,'THETA')
100 CALL RECOVR
CALL NEWLIN

```

```

CALL ANMODE
WRITE(6,102)
FORMAT(34X,3H+/-)
CALL ANGLE(504,304)
CALL RECOVER
CALL MOVABBS(320,302)
CALL DRWREL(0,2)
CALL DRWREL(138,0)
CALL DRWREL(0,-2)
CALL DRWREL(-138,0)
CALL MOVREL(212,0)
CALL DRWREL(212,2)
CALL DRWREL(0,22)
CALL DRWREL(140,0)
CALL DRWREL(0,-2)
CALL DRWREL(-140,0)
CALL MOVREL(0,3)
CALL CARTN
CALL ANMODE
WRITE(6,103)
FORMAT(22X,'*')
READ(5,104) X,HO,THETA
FORMAT(F10.7,5X,F10.7)
CALL RECOVER
X=RHO*COS(THETA)
Y=RHO*SIN(THETA)
CALL LOCATE(2,X,Y,LINEPZ)
CALL NEWLN
CALL NEWLN
CALL ANMODE
WRITE(6,105) POLZRO(LINEPZ,3),POLZRO(LINEPZ,4)
FORMAT(9X,30HDELETED COMPLEX ZEROS WILL BE ,F10.7,6H +/- ,F10.7)
CALL RECOVER
CALL ANGLE(727,260)
CALL NEWLN
CALL ANMODE
WRITE(6,106)
FORMAT(21X,32HIF CORRECT TYPE 'Y', IF NOT 'N' .)
CALL RECOVER
CALL SCURSR(ICHAR,IX,IY)
IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
CALL UPDATE(2,LINEPZ)
CALL NUC
RETURN
END

SUBROUTINE DCPPLR
COMMON IXXXX(4) POLZRO(20,5),IERROR
DIMENSION LTPDCP(64)

```

```

DATA LTPDCP/4HTO D,4HELET,4HE A,4HCOMP,4HLEX,4HPOLE,4H FRO
X   '4H CIR,4HCLER,4H ENT,4HER T,4HHE
X   '4H UNIT,4H CIR,4HCLER,4H ENT,4HER T,4HHE
X   '4H RHO,4H THE,4H HNT,4H CDR,4HDINA,4HTES,4HOTS A
X   '4H HAR O,4HNE O,4HFTH,4HER T,4HRO,4HOTS
X   '4HPOIN,4HNT,4H HAR O,4HNE O,4HFTH,4HER T,4HRO,4HOTS
X   '4H TO,4H THE,4H HAR O,4HNE O,4HFTH,4HER T,4HRO,4HOTS
X   '4HS IN,4H THE,4H HELET,4HED.
X   '4H S,4H THE,4H BOXE,4HS,4H INCN,4HDE V,4H ALUE
X   '4HHL,4H AND,4H MINU,4HS,4H GNA,4HSAP,4H PROP,4H RIAT
X   '4HE SIGN,4HND S,4HES,4HIMPL,4HIES,4HTIVE,4H VAL/
X   DATA LTPDCP(64)/4HES./
CALL CHCKSZ(-1,4)
IF(IEERROR.NE.0)RETURN
CALL ERASE
DO 30 I=157,8
CALL ANMODE
WRITE(6,100) LTPDCP(I+J-1), J=1,8)
30 CALL MOVABS(0,528)
100 CALL NEWLIN
CALL ANMODE
WRITE(6,101)
FORMAT(27X,'RHO',12X,'THETA')
CALL RECOVR
CALL NEWLIN
FORMAT(21X,8A4)
CALL ANMODE
WRITE(6,102)
FORMAT(34X,3H#/-)
101 CALL RECOVR
CALL ANMODE
FORMAT(27X,'RHO',12X,'THETA')
CALL RECOVR
CALL NEWLIN
FORMAT(21X,8A4)
CALL ANMODE
WRITE(6,103)
FORMAT(22X,103)
CALL MOVABS(504,304)
CALL DRWREL(0,22)
CALL DRWREL(138,20)
CALL DRWREL(0,-22)
CALL MOVREL(212,0)
CALL DRWREL(0,22)
CALL DRWREL(140,20)
CALL DRWREL(0,-22)
CALL MOVREL(0,3)
CALL CARTN
CALL ANMODE
WRITE(6,104)
FORMAT(5104,104)
READ(5104,104) THETA
104 FORMAT(F10.7,5X,F10.7)
CALL RECOVR
ASDF4393
ASDF4394
ASDF4395
ASDF4396
ASDF4397
ASDF4398
ASDF4399
ASDF4400
ASDF4401
ASDF4402
ASDF4403
ASDF4404
ASDF4405
ASDF4406
ASDF4407
ASDF4408
ASDF4409
ASDF4410
ASDF4411
ASDF4412
ASDF4413
ASDF4414
ASDF4415
ASDF4416
ASDF4417
ASDF4418
ASDF4419
ASDF4420
ASDF4421
ASDF4422
ASDF4423
ASDF4424
ASDF4425
ASDF4426
ASDF4427
ASDF4428
ASDF4429
ASDF4430
ASDF4431
ASDF4432
ASDF4433
ASDF4434
ASDF4435
ASDF4436
ASDF4437
ASDF4438
ASDF4439
ASDF4440

```

```

X=RHO*COS(THETA)
Y=RHO*SIN(THETA)
CALL LOCATE(4,X,Y,LINEPZ)
CALL NEWLIN
CALL ANMODE
WRITE(6,105)POLZRQ(LINEPZ,3)*POLZRQ(LINEPZ,4)
FORMAT(3X,29DELETED COMPLEX POLÉ WILL BE ,F10.7,6H +/- ,F10.71
      CALL RECOVR(727,260)
      CALL NEWLIN
      CALL ANMODE
      WRITE(6,106)FORMAT(2IX,32HIF CORRECT TYPE •Y•, IF NOT •N•.)
      CALL RECOVR
      CALL SCURSR(ICHAR IX IY)
      IF(ICHAR•NE.121•AND•ICHAR•NE.89)GO TO 10
      CALL UPDATE(4,LINEPZ)
      CALL NUC
      RETURN
END

105
106

SUBROUTINE DRZPLR
COMMON IXXXX(4),POLZRQ(20,5),JERROR
DIMENSION LTPDRZ(64)
DATA LTPDRZ/4HT0 D,4HELT,4HE A,4HREAL,4HZER,4H ZER,4HOM T
      X,4HHE T,4HENT,4HER T,4HHÉ,4HFR,4HOM T
      X,4HHDSP,4HLAY,4HIS,4HED W,4HIT,4HHR HO,4H COC
      X,4HRDIN,4HAT,4HAS SO,4HCIA T,4HED W,4HIT,4HHR HO,4H COC
      X,4HQF,4HZERO,4H OF,4HAP,4HINT,4HN EA,4HNEA,4H HE TA
      X,4HOT,4HT0 B,4HÉ DE,4HLETT,4HD,4HNTER,4H THE,4H VAL
      X,4HUE,4HWI TH,4HIN T,4HHE B,4HDX,4HROYI,4HDED,4H INC
      X,4HLUDE,4HAD E,4HCIMA,4HL,4HND M,4HINUS,4HSIG,4HN AS
      X,4H DATA LTPDRZ(64)/4HIVE/
      CALL CHCKSZ(-1,1)
      IF(JERROR•NE.0)RETURN
      CALL ERASE
      CALL MOVABS(0,528)
      DO 30 I=1,5,8
      CALL ANMODE
      WRITE(6,100)(LTPDRZ(I+J-1),J=1,8)
30   CALL KECOVR
      CALL NEWLIN
      FORMAT(2IX,8A4)
100  CALL NEWLIN
      CALL ANMODE
      WRITE(6,101)
      FORMAT(2IX,4HDO )
101

```

```

CALL RECOVR
CALL NEWLIN
CALL MOVABS(1320,302)
CALL DRWREL(0,22)
CALL DRWREL(138,0)
CALL DRWREL(0,-22)
CALL DRWREL(-138,0)
CALL MOVREL(0,3)
CALL CARTN
CALL ANMODE
WRITE(6,103)
FORMAT(22X,'>')
103 READ(5,104) RHO
FORMAT(F10.4,7.5X,F10.7)
104 CALL RECOVR
CALL LOCATE(1,RHO,0.,LINEPZ)
CALL NEWLIN
CALL NEWLIN
CALL ANMODE
THETA=0.
WRITE(6,105) POLZRO(LINEPZ,3),POLZRO(LINEPZ,4)
105 FORMAT(12X,26HDELETED REAL ZERO WILL BE ,F10.7,3X,F10.7)
CALL RECOVR
CALL ANGLE(677,260)
CALL ANMODE
WRITE(6,106)
FORMAT(21X,32HIF CORRECT TYPE 'Y', IF NOT 'N')
106 CALL RECOVR
CALL SCURSR(ICHAR,IY)
IF(ICHAR.NE.'121'AND.'1CHAR.NE.'89)GO TO 10
CALL UPDATE(1,LINEPZ)
CALL NUC
RETURN
END

SUBROUTINE DRPPLR
COMMON IXXX(4),POLZRO(20,5),IERROR
DIMENSION LTPDRP(64)
DATA LTPDRP/4HTO D,4HELET,4HE A,4HREAL,4H POL,4HE FR,4HOM,T
        4HHE 4HUNIT,4HCIR,4HENT,4HER T,4HHE,4HRHO,
        4H 4HCOOR,4HDINA,4HCLF,4HET A,4HETA,4H VAL
        4HOF 4HOF Z,4HHERO,4H OF,4HNEAR,4H THE
        4HUE 4HROOT,4HTO,4HBE D,4HELET,4HEO,
        4HE 4HYALU,4HEWI,4HTHIN,4H THE,4H PRO,4HVIDE
        4HD. 4HINC,4HDE,4HCIMA,4HL A,4HND M,4HINUS,
        4H 4HSIGN,4H AS,4HAPPR,4HOPRI,4HATE,4H /
        DATA LTPDRP{64}/4H

```

```

CALL CHCKSZ (-1,3)
IF(IERROR.NE.0)RETURN
CALL ERASE
CALL MOVABS(0,528)
DO 30 I=1,8
CALL ANMODE
WRITE(6,100)(LTPDRP(I+J-1),J=1,8)
CALL RECOVR
CALL NEWLIN
FORMAT(12X,8A4)
CALL NEWLIN
CALL ANMODE
WRITE(6,101)
FORMAT(12X,RHO)
CALL RECOVR
CALL NEWLIN
CALL MOVABS(320,302)
CALL DRWREL(0,2,0)
CALL DRWREL(1,38,0)
CALL DRWREL(0,1,-2)
CALL DRWREL(-1,38,0)
CALL DRWREL(0,3,0)
CALL ANMODE
WRITE(6,103)
FORMAT(12X,>)
READ(5,104) RHO
FORMAT(F10.7)
CALL RECOVR
CALL NEWLIN
CALL LOCATE(3,RHO,0,LINEPZ)
CALL NEWLIN
CALL ANMODE
THETA=0.
WRITE(6,105)POLZERO(LINEPZ,3)
FORMAT(12X,26HDELETED REAL POLE WILL BE ,F10.7,3X,F10.7)
CALL RECOVR
CALL ANGLE(677,260)
CALL NEWLIN
CALL ANMODE
WRITE(6,106)
FORMAT(12X,32HIF CORRECT TYPE 'Y', IF NOT 'N'.)
CALL RECOVR
CALL SCURSR(ICHAR,IX,IY)
IF(ICHAR.NE.121.AND.ICHAR.NE.89)GO TO 10
CALL UPDATE(3,LINEPZ)
CALL NUC
RETURN

```

```

ASDF4585
ASDF4586
ASDF4587
ASDF4588
ASDF4589
ASDF4590
ASDF4591
ASDF4592
ASDF4593
ASDF4594
ASDF4595
ASDF4596
ASDF4597
ASDF4598
ASDF4599
ASDF4600
ASDF4601
ASDF4602
ASDF4603
ASDF4604
ASDF4605
ASDF4606
ASDF4607
ASDF4608
ASDF4609
ASDF4610
ASDF4611
ASDF4612
ASDF4613
ASDF4614
ASDF4615
ASDF4616
ASDF4617
ASDF4618
ASDF4619
ASDF4620
ASDF4621
ASDF4622
ASDF4623
ASDF4624
ASDF4625
ASDF4626
ASDF4627
ASDF4628
ASDF4629
ASDF4630
ASDF4631
ASDF4632

END
SUBROUTINE ANGLE(IX,IY)
CALL MOVABS(IX,IY)
CALL MOVREL(14,20)
CALL DRWREL(9,-18)
CALL DRWREL(20,0)
CALL MOVREL(-3,-1)
CALL DRWREL(-1,7)
CALL DRWREL(-3,5)
CALL DRWREL(-3,3)
CALL DRWREL(-4,2)
CALL MOVREL(0,-20)
RETURN
END

SUBROUTINE ERROR
COMMON IROOTS(4),POLZR(20,5),IERROR
CALL LST
CALL MOVABS(0,154)
CALL ANMODE
GOTO 100
WRITE(6,100)
FORMAT(2,2,4,4,4,6,8,8,6,8,6,8,6)
!MAXIMUM SYSTEM ORDER EXCEEDED.!
100 GOTO 10
WRITE(6,101)
FORMAT(19X,!
101 GOTO 10
WRITE(6,102)
FORMAT(1IX,!
102 GOTO 10
WRITE(6,103)
FORMAT(10X,!
103 GOTO 10
CALL RECOVR
WRITE(6,102)
FORMAT(1IX,!
104 GOTO 10
CALL RECOVR
FORMAT(125X,!
104 CALL RECOVR
FORMAT(6,104)
FORMAT(1IX,!
105 GOTO 10
!ANY KEYBOARD KEY!
1 CALL RECOVR
CALL SCURSR(ICHAR, IX, IY)
IERROR=0
CALL NUC

```

```

      RETURN
      END

      SUBROUTINE IROOT(LST)
COMMON IROOT(4), POLZRO(20,51), IERROR
DIMENSION IRTTP(5), DATA(IZ/1HZ/ITP/1HP/IZP/2HZP/
DATA IRTTP/2H, ERASE
CALL HOME
CALL ANMODE
WRITE(6,102) (IZ, I=1, 70)
FORMAT(1X,70A1)
CALL RECOVR
CALL NEWLIN
CALL ANMODE
WRITE(6,108)
FORMAT(1X,7,5X,"REAL",6X,"Z",3X,"IMAGINARY",3X,"Z")
1 16X,RHO,6X,Z,5X,THETA,5X,Z RT Z)
CALL NEWLIN
CALL RECOVR
CALL ANMODE
WRITE(6,102) (IZ, I= 1, 70)
CALL RECOVR
CALL NEWLIN
DO 10 I=1,10
CALL ANMODE
ITYPEP=POLZRO(I,5)+1.
1 IF(POLZRO(I,5).NE.2.0 .AND. POLZRO(I,5).NE.4.) ITTP(ITYPEP)
1 WRITE(6,104) (ITTP(J), J=1,4)
1 IF(POLZRO(I,5).EQ.2.0 .OR. POLZRO(I,5).EQ.4.)
1 WRITE(6,103) (POLZRO(I,J), J=1,4)
1 FORMAT(1X,7,5X,"REAL",6X,"Z",3X,"IMAGINARY",3X,"Z")
1 3X,Z,7,5X,F10.7,Z,F10.7,
1 104 1 FORMAT(1X,7,5X,F10.7,Z,F10.7,Z,F10.7,
1 104 1 Z,F10.7,Z,A2,Z,F10.7,Z,F10.7,
1 104 1 CALL RECOVR
1 10 CALL NEWLIN
1 10 CONTINUE
1 10 WRITE(6,112) (IZP, I=1,35)
1 12 FORMAT(1X,35A2)
1 12 CALL RECOVR
1 12 CALL NEWLIN
1 12 DO 20 I=1,20
1 12 CALL ANMODE
1 12 ITYPEP=POLZRO(I,5)+1.
1 12 IF(POLZRO(I,5).NE.2..AND.POLZRO(I,5).NE.4..)

```

```

1 WRITE(6,106) (POLZRO(I,J),J=1,4),IRTP(I,TYPEP)
1 IF(POLZR0(1,5).EQ.2,I,0,POLZR0(1,5).EQ.4)
1 WRITE(6,105) (POLZR0(I,J),J=1,4),IRTP(I,TYPEP)
105  FORMAT(1X,P+,/-,F10.7,F10.7,P,F10.7,
106  FORMAT(1X,P,F10.7,P,A2,P,F10.7,P,F10.7,
107  P,A2,P,F10.7,P,A2,P,F10.7,P,F10.7,
1 CALL RECOVR
CALL NEWLIN
CONTINUE
20 CALL ANMODE
WRITE(6,102) (IP, I =1,70)
CALL RECOVR
CALL NEWLIN
CALL ANMODE
WRITE(6,107)
FORMAT(1X,/)
CALL RECOVR
IF(TERROE.EQ.0)RETURN
CALL NEWLIN
CALL ANMODE
WRITE(6,110) IROOTS(1),
FORMAT(20X,NUMBER OF REAL ZEROS:,I3)
107
110
111
113
114
115
116

```

ASDF4681  
ASDF4682  
ASDF4683  
ASDF4684  
ASDF4685  
ASDF4686  
ASDF4687  
ASDF4688  
ASDF4689  
ASDF4690  
ASDF4691  
ASDF4692  
ASDF4693  
ASDF4694  
ASDF4695  
ASDF4696  
ASDF4697  
ASDF4698  
ASDF4699  
ASDF4700  
ASDF4701  
ASDF4702  
ASDF4703  
ASDF4704  
ASDF4705  
ASDF4706  
ASDF4707  
ASDF4708  
ASDF4709  
ASDF4710  
ASDF4711  
ASDF4712  
ASDF4713  
ASDF4714  
ASDF4715  
ASDF4716  
ASDF4717  
ASDF4718  
ASDF4719  
ASDF4720  
ASDF4721  
ASDF4722  
ASDF4723  
ASDF4724  
ASDF4725  
ASDF4726  
ASDF4727  
ASDF4728

IROOTS(2)  
NUMBER OF COMPLEX ZERO PAIRS:,I3)  
IROOTS(3)  
NUMBER OF REAL POLES:,I3)  
IROOTS(4)  
NUMBER OF COMPLEX POLE PAIRS:,I3)  
FORMAT(20X,REAL SPACE THEN RETURN")  
FORMAT(1X,HI)  
FORMAT(5,16) IN  
FORMAT(A1)

```

CALL RECOVR
CALL NUC
RETURN
END

SUBROUTINE PLTTBL
C* SUBROUTINE PLOTS THE POLZRO TABLE OF THE UNIT CIRCLE (12)
C* COMMON IXXXX(4),POLZRO(20,5)
DO 10 I=1,20
C* IF POLZRO(I,5)=0 NO ROOT HAS BEEN STORED
C* IF(POLZRO(I,5).EQ.0) GO TO 10
C* CALL PLOTRT(IFIX(POLZRO(I,5)),POLZRO(I,1),POLZRO(I,2))
10 CONTINUE
RETURN
END

SUBROUTINE CHCKSZ (IDELTA, ITYPE)
C* THIS SUBROUTINE CHECKS THE TABLE OF ROOTS TO SEE
C* IF IT IS POSSIBLE TO EXECUTE THE DESIRED SUBROUTINE
C* IDETA: IS THE CHANGE IN THE NUMBER OF ROOTS EXPECTED
C* BY THE CALLING SUBROUTINE
C* ITYPE: IS THE TYPE OF ROOTS TO BE ALTERED, I.E.,
C* COMPLEX REAL ZERO OR POLE
C* IDETA REAL ZERO OR POLE NUMBER IF IT IS
C* ERROR: RETURNS THE ERROR MESSAGE NUMBER IF IT IS
C* NOT POSSIBLE TO EXECUTE THE SELECTED COMMAND;
C* THE MAXIMUM SYSTEM ORDER IS LIMITED TO TEN AND
C* ROOTS MAY NOT BE DELETED IF THEY HAVE NOT BEEN INPUT
C* COMMON IROOTS(4),PXXXXX(20,5),IERROR
C* IROOTS(1) = FLAG COUNTING REAL ZEROS
C* IROOTS(2) = FLAG COUNTING COMPLEX ZEROS
C* IROOTS(3) = FLAG COUNTING REAL POLES
C* IROOTS(4) = FLAG COUNTING COMPLEX POLE PAIRS
C* DETERMINE WHETHER ROOT(S) ARE BEING ADDED OR DELETED (1)
C* IF(IDELTA.LT.0) GO TO 10
C* ROOT(S) ARE BEING ADDED (3)
C* CALCULATE THE EXPECTED ORDER OF THE SYSTEM (1)
C*
ASDF4729
ASDF4730
ASDF4731
ASDF4732
ASDF4733
ASDF4734
ASDF4735
ASDF4736
ASDF4737
ASDF4738
ASDF4739
ASDF4740
ASDF4741
ASDF4742
ASDF4743
ASDF4744
ASDF4745
ASDF4746
ASDF4747
ASDF4748
ASDF4749
ASDF4750
ASDF4751
ASDF4752
ASDF4753
ASDF4754
ASDF4755
ASDF4756
ASDF4757
ASDF4758
ASDF4759
ASDF4760
ASDF4761
ASDF4762
ASDF4763
ASDF4764
ASDF4765
ASDF4766
ASDF4767
ASDF4768
ASDF4769
ASDF4770
ASDF4771
ASDF4772
ASDF4773
ASDF4774
ASDF4775
ASDF4776

```

```

IF(I TYPE.EQ.1.OR.I TYPE.EQ.2)N ORDER=I ROOTS(1)+2*I ROOTS(2)+I DELTA
ASDF4777
IF(I TYPE.EQ.3.DR.I TYPE.EQ.4)N ORDER=I ROOTS(3)+2*I ROOTS(4)+I DELTA
ASDF4778
C* IF "N ORDER" IS GREATER THAN 10, MAXIMUM SYSTEM ORDER HAS BEEN
ASDF4779
C* EXCEEDED AND AN ERROR RESULTS (1)
ASDF4780
C* IF(N ORDER.GT.10)I ERROR=I TYPE
ASDF4781
20 IF(Y.GT.0.)CALL POINTA(XX,YY)
RETURN
ASDF4782
C* ROOTS ARE BEING DELETED (2)
ASDF4783
C* CALCULATE THE EXPECTED ROOT TOTAL IF THE CALLING
ASDF4784
C* SUBROUTINE EXECUTES (1)
ASDF4785
C* PLUS SIGN IS DUE TO "I DELTA" BEING LESS THAN ZERO
ASDF4786
C* IXPTOT=I ROOTS(I TYPE)+I DELTA
ASDF4787
C* IF THE EXPECTED ROOTS TOTAL "IXPTOT" IS NEGATIVE
ASDF4788
C* AN ERROR IS GENERATED (1)
ASDF4789
C* IF(IXPTOT.LT.0.)I ERROR=I TYPE+4
ASDF4790
999 RETURN
ASDF4791
END
ASDF4792
SUBROUTINE UPDATE(I TYPE,LINEPZ)
ASDF4793
C* THIS SUBROUTINE WILL UPDATE THE POLZRO TABLE WHEN A ROOT IS REMOVED
ASDF4794
C* COMMON I ROOTS(4),POLZRO(20,5)
ASDF4795
C* "LINEPZ" IS THE LINE OF POLZRO ARRAY TO BE DELETED
ASDF4796
C* IF(LINEPZ.EQ.20)GO TO 45
ASDF4797
IF(LINEPZ.EQ.10)GO TO 30
ASDF4798
IF(LINEPZ.EQ.1)GO TO 15
ASDF4799
DO 10 J=LINEPZ,9
ASDF4800
DO 10 K=1,5
ASDF4801
10 POLZRO(J,K)=POLZRO(J+1,K)
ASDF4802
DO 20 M=1,4
ASDF4803
20 POLZRO(10,M)=-10.
ASDF4804
POLZRO(10,5)=0.
ASDF4805
GO TO 60
ASDF4806
DO 40 J=L,LINEPZ,19
ASDF4807
DO 40 K=1,5
ASDF4808
40 POLZRO(J,K)=POLZRO(J+1,K)
ASDF4809
DO 50 M=1,4
ASDF4810
50 POLZRO(20,M)=-10.
ASDF4811
POLZRO(20,5)=0.
ASDF4812

```

```

C* ADJUST THE ROOT COUNTER SINCE A ROOT HAS BEEN DELETED
C* IROOTS(IITYPE)=IROOTS(IITYPE)-1
C* RETURN
C* END

SUBROUTINE LOCATE(IITYPE,X,Y,LINEPZ)
C* THIS SUBROUTINE LOCATES THE STORED ROOT NEAREST THE CURSOR POSITION
C* COMMON IXXXX(4), POLZRO(20,5)

C* "IITYPE" IS THE TYPE OF ROOT SEARCHED
C* "LINEPZ" IS THE LINE OF POLZRO WHICH CONTAINS THE ROOT
C* OF THE DESIRED TYPE WHICH IS CLOSEST TO THE
C* USER-POSITIONED CURSOR
C* "DIST" IS THE SHORTEST DISTANCE FOUND FROM STORED ROOT
C* TO THE USER-POSITIONED CURSOR
C* STRRTS STORES ONLY THE COMPLEX POLE IN THE TOP HALF PLANE
C* SY=ABS(Y)
C* DIST=20.
DO 10 I=1,20
IF(IFIX(POLZRO(I,5)).NE.IITYPE) GO TO 10
CKDIST=SQRT((X-POLZRO(I,1))**2+(SY-POLZRO(I,2))**2)
IF(CKDIST.LT.DIST)LINEPZ=I
IF(CKDIST.LT.DIST)DIST=CKDIST
CONTINUE
10 RETURN
END

SUBROUTINE START
C* THIS SUBROUTINE INITIALIZES ALL THE VARIABLES STORED IN
C* COMMON BEFORE EXECUTION OF THE PROGRAM (10)
C* COMMON IROOTS(4), POLZRO(20,5), TERROR, IOLD
C* IOLD=0
DO 10 I=1,4
IROOTS(I)=0
10 TERROR=0
DO 20 J=1,20
POLZRO(J,5)=0.
DO 20 K=1,4
POLZRO(J,K)=-10.
20 RETURN

```

```

END
      SUBROUTINE STRRTS(IITYPE,MODE,ARGMT1,ARGMT2)
C* THIS SUBROUTINE IS DESIGNED TO STORE ROOTS PREVIOUSLY
C* GENERATED IN THE ROOT TABLE "POLZRO"
COMMON IROOTS(4), POLZRO(20,5), TERROR
PI=3.14159265
IF(ARGMT1.EQ.0..AND.ARGMT2.EQ.0.) GO TO 45
C* GIVEN "MODE", "ARGMT1", AND "ARGMT2" GENERATE THE REAL,
C* IMAGINARY RADII, AND THETA VALUES OF THE UPPER HALF PLANE
C* ROOT TO BE STORED (THIS INCLUDES THE REAL AXIS).
C* GO TO (10,20), MODE
C* "MODE" DICTATES THAT "ARGMT1" AND "ARGMT2" ARE RECTANGULAR
C* "MODE" DICTATES THAT "ARGMT1" AND "ARGMT2" ARE POLAR
10   RREAL=ARGMT1
     RIMAG=ABS(ARGMT2)
     RADIUS=SQRT(ARGMT1**2+ARGMT2**2)
     THETA=ATAN2(ARGMT1,ARGMT2)
     GO TO 30
C* "MODE" DICTATES THAT "ARGMT1" AND "ARGMT2" ARE POLAR
C* 20   RADIUS=ARGMT1
      IF(ARGMT2.LE.-PI) AND ARGMT2.GT.-PI GO TO 40
      IF(ARGMT2.LE.-PI) ARGMT2=ARGMT2+2.*PI
      IF(ARGMT2.GT.PI) ARGMT2=ARGMT2-2.*PI
      GO TO 50
      THETA=ARGMT2
      RREAL=RADIUS*COS(THETA)
      RIMAG=RADIUS*SIN(THETA)
      GO TO 30
C* IF THE ROOT IS TO BE AT THE ORIGIN LIBRARY FUNCTION
C* ASSIGN VALUES SUCH THAT ILLEGAL LIBRARY FUNCTION
C* ARGUMENTS WILL NOT BE ASSIGNED
C* 45   RREAL=0.
      RIMAG=0.
      RADIUS=0.
C* STORAGE PROCEDURE IS A FUNCTION OF THE TYPE OF ROOTS TO BE STORED
C*
ASDF4873
ASDF4874
ASDF4875
ASDF4876
ASDF4877
ASDF4878
ASDF4879
ASDF4880
ASDF4881
ASDF4882
ASDF4883
ASDF4884
ASDF4885
ASDF4886
ASDF4887
ASDF4888
ASDF4889
ASDF4890
ASDF4891
ASDF4892
ASDF4893
ASDF4894
ASDF4895
ASDF4896
ASDF4897
ASDF4898
ASDF4899
ASDF4900
ASDF4901
ASDF4902
ASDF4903
ASDF4904
ASDF4905
ASDF4906
ASDF4907
ASDF4908
ASDF4909
ASDF4910
ASDF4911
ASDF4912
ASDF4913
ASDF4914
ASDF4915
ASDF4916
ASDF4917
ASDF4918
ASDF4919
ASDF4920

```

```

C*      GO TO ( K2, C2, RP, CP ), ITYPE
C*      A REAL ZERO IS BEING STORED
C*      IROOTS(1) IS THE NUMBER OF REAL ZEROS ALREADY
C*          STORED
110    POLZRO( IROOTS(1)+IROOTS(2)+1,1 )=RREAL
      POLZRO( IROOTS(1)+IROOTS(2)+1,2 )=0
      POLZRO( IROOTS(1)+IROOTS(2)+1,3 )=ABS(RREAL)
      IF( ARGMT1.GE.0.) THETA=0.
      IF( ARGMT1.LT.0.) THETA=PI
      POLZRO( IROOTS(1)+IROOTS(2)+1,4 )=THETA
      POLZRO( IROOTS(1)+IROOTS(2)+1,5 )=1.
      IROOTS(1)=IROOTS(1)+1
      GO TO 999
C*      A REAL POLE IS TO BE STORED
C*      IROOTS(3) IS THE NUMBER OF REAL POLES ALREADY STORED
120    POLZRO( IROOTS(3)+IROOTS(4)+1,1 )=RREAL
      POLZRO( IROOTS(3)+IROOTS(4)+1,2 )=0
      POLZRO( IROOTS(3)+IROOTS(4)+1,3 )=ABS(RREAL)
      IF( ARGMT1.GE.0.) THETA=0.
      IF( ARGMT1.LT.0.) THETA=PI
      POLZRO( IROOTS(3)+IROOTS(4)+1,4 )=THETA
      POLZRO( IROOTS(3)+IROOTS(4)+1,5 )=3.
      IROOTS(3)=IROOTS(3)+1
      GO TO 999
C*      A COMPLEX ZERO IS TO BE STORED
C*      IROOTS(2) IS THE NUMBER OF COMPLEX ZERO PAIRS ALREADY STORED
210    POLZRO( IROOTS(2)+IROOTS(1)+1,1 )=RREAL
      POLZRO( IROOTS(2)+IROOTS(1)+1,2 )=ABS(RIMAG)
      POLZRO( IROOTS(2)+IROOTS(1)+1,3 )=ABS(RADIUS)
      IF( ARGMT1.EQ.0.) AND. ARGMT2.EQ.0. ) RADIUS=1.
      POLZRO( IROOTS(2)+IROOTS(1)+1,4 )=ARCCOS(RREAL/ABS(RADIUS))
      IROOTS(2)=IROOTS(2)+1
      GO TO 999
C*      A COMPLEX POLE IS TO BE STORED
C*      IROOTS(4) IS THE NUMBER OF COMPLEX POLE PAIRS ALREADY STORED
220    POLZRO( IROOTS(4)+IROOTS(3)+1,1 )=RREAL
      POLZRO( IROOTS(4)+IROOTS(3)+1,2 )=RIMAG
      POLZRO( IROOTS(4)+IROOTS(3)+1,3 )=ABS(RADIUS)
      IF( ARGMT1.EQ.0. ) AND. ARGMT2.EQ.0. ) RADIUS=1.

```

```

POLZRO( IROOTS(4)+IROOTS(3)+1,4)=ARCCOS(RREAL/ABS(RADIUS))
ASDF4969
POLZRO( IROOTS(4)+IROOTS(3)+1,5)=4.
ASDF4970
IROOTS(4)=IROOTS(4)+1
ASDF4971
IF(I TYPE.EQ.1.JR.I TYPE.EQ.3)CALL PLOTRT(I TYPE,RREAL,0)
ASDF4972
IF(I TYPE.EQ.2.JR.I TYPE.EQ.4)CALL PLOTRT(I TYPE,RREAL,RIMAG)
ASDF4973
RETURN
ASDF4974
END
ASDF4975

SUBROUTINE PLOTRT (ITYPE, RREAL, RIMAG)
ASDF4976
C* THE PURPOSE OF THIS SUBROUTINE IS TO PLOT
ASDF4977
C* THE ROOT JUST ENTERED INTO THE SYSTEM
ASDF4978
C* DIMENSION IZERO(16), ISTAR(16)
ASDF4979
C* DATA POINTS REQUIRED FOR DRAWING ZEROS
ASDF4980
C* DATA IZERO/2,-2,0,-2,-2,-2,0,-2,2,0,-2,2,0/
ASDF4981
C* DATA ISTAR/-5,5,10,-10,-5,10,0,-10,5,10,-10,-10,10,5,-10,0/
ASDF4982
ASDF4983
ASDF4984
ASDF4985
ASDF4986
ASDF4987
ASDF4988
ASDF4989
ASDF4990
ASDF4991
ASDF4992
ASDF4993
ASDF4994
ASDF4995
ASDF4996
ASDF4997
ASDF4998
ASDF4999
ASDF5000
ASDF5001
ASDF5002
ASDF5003
ASDF5004
ASDF5005
ASDF5006
ASDF5007
ASDF5008
ASDF5009
ASDF5010
ASDF5011
ASDF5012
ASDF5013
ASDF5014
ASDF5015
ASDF5016

C* IF ZERO IS OUTSIDE THE UNIT CIRCLE, PLOT A STAR.
C* RADIUS = SQRT(RREAL**2 + RIMAG**2)
C* IF(RADIUS.GT.1)GO TO 300
C* SINCE ROOT IS INSIDE THE UNIT CIRCLE
C* IF THE ROOT IS A ZERO GO TO 100
C* IF THE ROOT IS A POLE GO TO 200
C* RZ,CZ,RP,CP
C* GO TO (100,100,200,200),ITYPE
C* CENTER THE ZERO ON THE LOCATION STORED IN POLZRO
C* 100 CALL MOVEA(RREAL,RIMAG)
C* GENERATE THE ZERO (3)
C* CALL MOVRNL(1,3)
DO 120 I=1,15
120 CALL DRWRL(IZERO(I),IZERO(I+1))

C* IF THE ZERO IS REAL, RETURN
C* IF(I TYPE.EQ.1)GO TO 999
C* PLOT THE CORRESPONDING COMPLEX ZERO IN THE LOWER HALF PLANE (4)
C*

```

```

CALL MOVEA(RREAL,-RIMAG)
CALL MOVREL(1,3)
DO 130 I=1,15 12
    CALL DRWREL(I,0),I,0,I+1)
C* PLOT THE POLE (REAL, OR UPPER HALF PLANE) (5)
C* 200 CALL MOVEA(RREAL,RIMAG)
    CALL MOVREL(3,3)
    CALL DRWREL(-6,-6)
    CALL MOVREL(0,6)
    CALL DRWREL(6,-6)
C* IF THE POLE IS REAL, RETURN
C* IF ITYPE.EQ.3 GO TO 999
C* IF THE POLE IS COMPLEX, PLOT THE CORRESPONDING
C* LOWER HALF PLANE POLE (5)
C* 200 CALL MOVEA(RREAL,-RIMAG)
    CALL MOVREL(3,3)
    CALL DRWREL(-6,-6)
    CALL MOVREL(0,6)
    CALL DRWREL(6,-6)
GO TO 999
300 ANGLE=ATAN2(RIMAG,RREAL)
PREAL=1.05*COS(ANGLE)
PIMAG=1.05*SIN(ANGLE)
CALL MOVEA(PREAL,PIMAG)
DO 320 M=1,2
    DO 310 I=1,16 4
        CALL MOVREL(I,STAR(I),ISTAR(I+1))
        CALL DRWREL(ISTAR(I+2),ISTAR(I+3))
    CONTINUE
    IF(M.EQ.2.OR.ITYPE.EQ.1) GO TO 999
    CALL MOVEA(PREAL,-PIMAG)
    RETURN
END
310
320
999

```

APPENDIX H: SOURCE DECK FOR ASDF COMMAND: RESPONSE

```

ASDF6001
ASDF6002
ASDF6003
ASDF6004
ASDF6005
ASDF6006
ASDF6007
ASDF6008
ASDF6009
ASDF6010
ASDF6011
ASDF6012
ASDF6013
ASDF6014
ASDF6015
ASDF6016
ASDF6017
ASDF6018
ASDF6019
ASDF6020
ASDF6021
ASDF6022
ASDF6023
ASDF6024
ASDF6025
ASDF6026
ASDF6027
ASDF6028
ASDF6029
ASDF6030
ASDF6031
ASDF6032
ASDF6033
ASDF6034
ASDF6035
ASDF6036
ASDF6037
ASDF6038
ASDF6040
ASDF6041
ASDF6042
ASDF6043
ASDF6044
ASDF6045
ASDF6046
ASDF6047
ASDF6048

C***** SOURCE DECK FOR ASDF COMMAND: RESPONSE
C***** COMMON IROOTS(4),POLZRO(20,5),ERROR
C***** COMMON /ABVCTR/A(11)B(11)
C***** COMMON /IMPULS/Y(1025),YS(1025),EN(1025)
C***** COMMON /FREQ/YP(1026),YM(1026),PI(1026)
C***** LINEAR=1
C***** LOG=2

C* INITIALIZE A AND B TO ZERO
C* DO 5 K=1,20
      A(K)=0.
      B(K)=0.
      5

C* READ THE POLZRO TABLE OFF OF THE FILE
C* DO 20 I=1,20
      100  FORMAT(1X,5F12.8)
      20   READ(1,100) (POLZRO(I,J),J=1,5)
C* READ THE IROOTS VALUES FROM THE FILE
C* READ(1,101) (IROOTS(I),I=1,4)
      101  FORMAT(1X,4I2)
      102  READ(1,102) FLTRGN
      102  FORMAT(1X,F12.8)
      FLTRGN=ABS(FLTRGN)
      ICHAR=0

C* PRINT OUT A TABLE OF THE POLES AND ZEROS
C* CALL FLTR2(FLTRGN)

C* GENERATE THE A(K) COEFFICIENTS
C* CALL ASUBK(A,NORDER)
      NDEN=NORDER+1

C* GENERATE THE B(R) COEFFICIENTS
C* CALL BSUBR(B,NORDER)
      NNUM=NORDER+1

```

```

C* CHECK TO SEE IF THE FILTER IS CAUSAL
C* ASDF6049
C* ASDF6050
C* ASDF6051
C* ASDF6052
C* ASDF6053
C* ASDF6054
C* ASDF6055
C* ASDF6056
C* ASDF6057
C* ASDF6058
C* ASDF6059
C* ASDF6060
C* ASDF6061
C* ASDF6062
C* ASDF6063
C* ASDF6064
C* ASDF6065
C* ASDF6066
C* ASDF6067
C* ASDF6068
C* ASDF6069
C* ASDF6070
C* ASDF6071
C* ASDF6072
C* ASDF6073
C* ASDF6074
C* ASDF6075
C* ASDF6076
C* ASDF6077
C* ASDF6078
C* ASDF6079
C* ASDF6080
C* ASDF6081
C* ASDF6082
C* ASDF6083
C* ASDF6084
C* ASDF6085
C* ASDF6086
C* ASDF6087
C* ASDF6088
C* ASDF6089
C* ASDF6090
C* ASDF6091
C* ASDF6092
C* ASDF6093
C* ASDF6094
C* ASDF6095
C* ASDF6096

ASDF6051
ASDF6052
ASDF6053
ASDF6054
ASDF6055
ASDF6056
ASDF6057
ASDF6058
ASDF6059
ASDF6060
ASDF6061
ASDF6062
ASDF6063
ASDF6064
ASDF6065
ASDF6066
ASDF6067
ASDF6068
ASDF6069
ASDF6070
ASDF6071
ASDF6072
ASDF6073
ASDF6074
ASDF6075
ASDF6076
ASDF6077
ASDF6078
ASDF6079
ASDF6080
ASDF6081
ASDF6082
ASDF6083
ASDF6084
ASDF6085
ASDF6086
ASDF6087
ASDF6088
ASDF6089
ASDF6090
ASDF6091
ASDF6092
ASDF6093
ASDF6094
ASDF6095
ASDF6096

103 FORMAT(10(7),' FILTER IS NOT CAUSAL - PROGRAM TERMINATE S')
C* ADJUST THE COEFFICIENTS IF NNUM DOES NOT EQUAL NDEN
C* ASDF6051
C* ASDF6052
C* ASDF6053
C* ASDF6054
C* ASDF6055
C* ASDF6056
C* ASDF6057
C* ASDF6058
C* ASDF6059
C* ASDF6060
C* ASDF6061
C* ASDF6062
C* ASDF6063
C* ASDF6064
C* ASDF6065
C* ASDF6066
C* ASDF6067
C* ASDF6068
C* ASDF6069
C* ASDF6070
C* ASDF6071
C* ASDF6072
C* ASDF6073
C* ASDF6074
C* ASDF6075
C* ASDF6076
C* ASDF6077
C* ASDF6078
C* ASDF6079
C* ASDF6080
C* ASDF6081
C* ASDF6082
C* ASDF6083
C* ASDF6084
C* ASDF6085
C* ASDF6086
C* ASDF6087
C* ASDF6088
C* ASDF6089
C* ASDF6090
C* ASDF6091
C* ASDF6092
C* ASDF6093
C* ASDF6094
C* ASDF6095
C* ASDF6096

C* COMPUTE THE UNIT SAMPLE RESPONSE
C* CALL RSPNSE(0,FLTRGN)
C* PLOT THE UNIT SAMPLE RESPONSE
C* CALL PLTIMP(ICHAR)
C* IF(ICHAR.EQ.88.OR.ICHAR.EQ.120)GO TO 30
C* CALCULATE THE STEP RESPONSE
C* CALL RSPNSE(1,FLTRGN)
C* PLOT THE STEP RESPONSE
C* CALL PLTSTP(ICHAR)
C* IF(ICHAR.EQ.88.OR.ICHAR.EQ.120)GO TO 30
C* COMPUTE THE MAGNITUDE AND PHASE OF THE TRANSFER FUNCTION
C* CALL FRQNCY(INNUM,NDEN,FLTRGN)
C* PLOT THE PHASE OF THE TRANSFER FUNCTION
C* CALL PLTTRF(3,LINEAR,ICHAR)
C* IF(ICHAR.EQ.88.OR.ICHAR.EQ.120)GO TO 30
C* PLOT THE MAGNITUDE OF THE TRANSFER FUNCTION
C* FIRST WITH LINEAR AXIS, THEN IN DECIBELS
C* CALL PLTTRF(4,LINEAR,ICHAR)
C* IF(ICHAR.EQ.88.OR.ICHAR.EQ.120)GO TO 30
C* CALL PLTTRF(4,LOG,ICHAR)
C* IF(ICHAR.EQ.88.OR.ICHAR.EQ.120)GO TO 30
C* STOP
C* END

SUBROUTINE ASUBK (POLE,NORDER)

```

```

C* GENERATE THE AK COEFFICIENTS FROM THE POLES
C* COMMON IROOTS(4), POLZRO(20,5), TERROR
C* COMPLEX POLES(11), ACOEF(11)
C* REAL POLE(11)
C* INITIALIZE ALL THE VECTORS AND INDICES TO ZERO
C*
      DO 5 K=1,11
      POLES(K)=(0.,0.)
      POLE(K)=0.
      ACOEF(K)=0.
      5   "J" INDEXES THE TABLE "POLES"
      "K" INDEXES THE TABLE "POLZRO"
C*
      J=1
      K=1
C* COMPUTE THE ORDER OF THE SYSTEM OF POLES
C* NORDER=IROOTS(3)+2*IROOTS(4)
      IF(NORDER.NE.0)GO TO 10
      POLE(1)=1.0
      RETURN
C* THE VECTOR "POLES" WILL CONTAIN A LIST OF ALL
C* THE POLES, IE., X+JY, X+JY, . . .
C* 10  POLES(J)=CMPLX(POLZRO(10+K,1),POLZRO(10+K,2))
C* TEST TO SEE IF ABLE ROOTS HAVE BEEN
C* STORED IN THE "POLES" VECTOR
C* IF(J.EQ.NORDER)GO TO 20
      J=J+1
C* IF THE ROOT IS REAL CONTINUE PROCESSING THE NEXT ROOT
      IF(POLZRO(K+10,5).NE.0)GO TO 15
      K=K+1
      GO TO 10
C* SINCE THE ROOT IS COMPLEX PUT THE CONJUGATE
C* OF THE ROOT IN THE "POLES" TABLE.
C* 15  POLES(J)=CMPLX(POLZRO(10+K,1),-POLZRO(10+K,2))

```

```

IF(J.EQ.NORDER) GO TO 20
J=J+1
K=K+1
GO TO 10

C* GENERATE THE COEFFICIENTS FOR THE D(Z) POLYNOMIAL
C* OF THE TRANSFER FUNCTION H(Z).
C* 20 CALL COEFF(POLES,NORDER,Acoef)
C* CHANGE THE COEFFICIENTS FROM COMPLEX ASUBK TO REAL ASUBK
C* DO 40 J=1,11
C* POLE(J)=REAL(Acoef(j))
C* RETURN
C* END

SUBROUTINE BSJBK(ZERO,NORDER)
C* GENERATE THE B(R) COEFFICIENTS FROM THE ZEROS
C* COMMON IROOTS(4),POLZRO(20,5),IERROR
C* COMPLEX ZERO(11),BCOEF(11)
C* REAL ZERO(11)
C* INITIALIZE ALL VECTORS AND INDICES
C* DO 5 K=1,11
C* ZERO(K)=(0.,0.)
C* ZERO(K)=0.
C* BCOEF(K)=(0.,0.)
C* 5 C* "J" INDEXES THE "ZERO'S" TABLE
C* C* "K" INDEXES THE "POLZRO" TABLE
C* J=1
C* K=1

C* COMPUTE THE ORDER OF THE SYSTEM OF ZEROS.
C* NORDER=IROOTS(1)+2*IROOTS(2)
C* IF(NORDER.NE.0) GO TO 10
C* ZERO(1)=1.0
C* RETURN
C* THE VECTOR "ZEROS" CONTAINS A LIST OF ALL
C* OF THE ZEROS, IE., X+JO, X+jY, . . .

```

```

10  ZEROS(J)=CMPLX(POLZRO(K,1),POLZI(K,2))
C* CHECK TO SEE IF ALL THE ROOTS HAVE BEEN PROCESSED
C* IF(J,FQ,NORDER) GO TO 20
J=J+1
C* IF THE ROOT IS REAL CONTINUE PROCESSING THE NEXT ROOT
C* IF(POLZRO(K,5).NE.1) GO TO 15
K=K+1
GO TO 10
C* SINCE THE ROOT IS COMPLEX, ENTER THE CONJUGATE
C* INTO THE TABLE "ZEROS".
C* ZEROS(J)=CMPLX(POLZRO(K,1),-POLZRO(K,2))
15  IF(J.EQ.NORDER) GO TO 20
J=J+1
K=K+1
GO TO 10
C* GENERATE THE BSUBR COEFFICIENTS
C* CALL COEFF(ZEROS, NORDER, BCOEF)
20  CALL COEFF(ZEROS, NORDER, BCOEF)
C* MAKE THE COEFFICIENTS BSUBR REAL.
C*
DO 40 J=1,11
ZERO(J)=REAL(BCOEF(J))
RETURN
END

SUBROUTINE COEFF(V,N,H1)
C* "V" - VECTOR OF ROOTS: "N" - THE ORDER OF THE SYSTEM
C* "H1" - VECTOR WITH THE FINAL COEFFICIENTS
C* H(1)=Z*(V1, H(2)=Z*(V1, H(3)=Z*(V1, . . . , H(11)=Z*(-10)
C* COMPLEX H1(11),H2(11),H3(11),V(11)
C* INITIALIZE VECTORS
IZERO=0
DO 10 I=1,11
H1(I)=(0.,0.)
H2(I)=(0.,0.)
H3(I)=(0.,0.)
10  H1(I)=(1.,0.)
C*
ASDF6193
ASDF6194
ASDF6195
ASDF6196
ASDF6197
ASDF6198
ASDF6199
ASDF6200
ASDF6201
ASDF6202
ASDF6203
ASDF6204
ASDF6205
ASDF6206
ASDF6207
ASDF6208
ASDF6209
ASDF6210
ASDF6211
ASDF6212
ASDF6213
ASDF6214
ASDF6215
ASDF6216
ASDF6217
ASDF6218
ASDF6219
ASDF6220
ASDF6221
ASDF6222
ASDF6223
ASDF6224
ASDF6225
ASDF6226
ASDF6227
ASDF6228
ASDF6229
ASDF6230
ASDF6231
ASDF6232
ASDF6233
ASDF6234
ASDF6235
ASDF6236
ASDF6237
ASDF6238
ASDF6239
ASDF6240

```

```

C* THE ROOTS COME FROM THE FORMER SUBROUTINE
C* THESE ARE ROOTS OF THE POLYNOMIALS N(Z), AND D(Z)
C* WHERE H(Z)=N(Z)/D(Z)
C* THE FACTORS OF THE POLYNOMIAL ARE OF THE FORM Z-ROOT
C*
      DO 15 K=1,11
      V(K)=-V(K)
15
C* WHEN K=N, WE HAVE GENERATED THE H1 COEFFICIENTS
C* OF N(Z), OR D(Z) OF H(Z)=N(Z)/D(Z)
C* THE REMAINING ITERATIONS ARE PERFORMED TO SIMPLIFY
C* OBTAINING COEFFICIENTS FOR N(Z**-1), AND D(Z**-1) LATER
C*
      DO 30 K=1,10
C* "H2" REPRESENTS THE PREVIOUS RESULT TIMES Z**(-1)
C* DO 40 I=1,10
40   H2(I+1)=H1(I)
      H2(I)=(0.,0.)
      DO 50 I=1,11
      H3(I)=H1(I)*V(I)
50
C* GENERATE THE NEW FINAL PRODUCT WITH K ROOTS MULTIPLIED.
C* DO 60 I=1,11
60   H1(I)=H2(I)+H3(I)
C* GET THE NEXT ROOT TO BE MULTIPLIED AND PUT IT INTO "V(1)"*
C* DO 70 I=1,10
70   V(1)=V(I+1)
      CONTINUE
30
C* TO GET THE COEFFICIENTS FOR H(Z**-1)=N(Z**-1)/D(Z**-1)
C* THE ORDER OF THE COEFFICIENTS MUST BE REVERSED.
C*
      DO 80 I=1,11
80   H2(I)=H1(I-1)
      DO 90 I=1,11
90   H1(I)=H2(I)
      RETURN
95
END

SUBROUTINE ADJUST(NNUM,NDEN)
COMMON /ABVCTR/A(11),B(11)
IDELTA=NDEN-NNUM
ISTOP=11-IDELTA
ASDF6241
ASDF6242
ASDF6243
ASDF6244
ASDF6245
ASDF6246
ASDF6247
ASDF6248
ASDF6249
ASDF6250
ASDF6251
ASDF6252
ASDF6253
ASDF6254
ASDF6255
ASDF6256
ASDF6257
ASDF6258
ASDF6259
ASDF6260
ASDF6261
ASDF6262
ASDF6263
ASDF6264
ASDF6265
ASDF6266
ASDF6267
ASDF6268
ASDF6269
ASDF6270
ASDF6271
ASDF6272
ASDF6273
ASDF6274
ASDF6275
ASDF6276
ASDF6277
ASDF6278
ASDF6279
ASDF6280
ASDF6281
ASDF6282
ASDF6283
ASDF6284
ASDF6285
ASDF6286
ASDF6287
ASDF6288

```

```

10 DO 10 I=1,1025
    B(12-I)=B(12-I-1)DELTA
    DO 20 K=1,1025
    B(K)=0.
    RETURN
   END

      SUBROUTINE PLTIMP(ICHAR)
C* THIS SUBROUTINE PLOTS THE UNIT SAMPLE RESPONSE
C*
      DIMENSION PICT(1025)
      COMMON /IMPULS/YI(1025), VS(1025), EN(1025)
      DO 5 K=1,1024
      EN(K+1)=K-1
      EN(1)=YI(1025)
      NFIN=YI(1025)
      DO 13 K=1,NFIN
      PICT(K+1)=YI(K)
      CONTINUE
      PICT(1)=YI(1025)
      CALL INIT
      CALL XFRM(2)
      CALL YFRM(2)
      IF(NFIN.LT.-70)CALL LINE(-1)
      IF(NFIN.GE.-70)CALL LINE(0)
      IF(NFIN.LT.-70)CALL SYMBOL(1)
      IF(NFIN.GE.-70)CALL SYMBOL(0)
      CALL SIZE(4)
      CALL PLOT(EN,PICT)
      JFI=YI(1025)+1
      IF(NFIN.GE.-70)GO TO 40
      DO 30 K=2,JFIN
      CALL MOVEA(JEN(K),PICT(K))
      CALL DRAWA(EN(K),0.0)
      CONTINUE
      30 CALL MOVEA(0,0)
      CALL DRAWA(EN(JFIN),0.0)
      CALL LABLE
      CALL VCURSR(ICHAR,X,Y)
      CALL FIN
      RETURN
   END

      SUBROUTINE PLTSTP(ICHAR)
C* THIS SUBROUTINE PLOTS THE UNIT STEP RESPONSE
C*
      ASDF6289
      ASDF6290
      ASDF6291
      ASDF6292
      ASDF6293
      ASDF6294
      ASDF6295
      ASDF6296
      ASDF6297
      ASDF6298
      ASDF6299
      ASDF6300
      ASDF6301
      ASDF6302
      ASDF6303
      ASDF6304
      ASDF6305
      ASDF6306
      ASDF6307
      ASDF6308
      ASDF6309
      ASDF6310
      ASDF6311
      ASDF6312
      ASDF6313
      ASDF6314
      ASDF6315
      ASDF6316
      ASDF6317
      ASDF6318
      ASDF6319
      ASDF6320
      ASDF6321
      ASDF6322
      ASDF6323
      ASDF6324
      ASDF6325
      ASDF6326
      ASDF6327
      ASDF6328
      ASDF6329
      ASDF6330
      ASDF6331
      ASDF6332
      ASDF6333
      ASDF6334
      ASDF6335
      ASDF6336

```

```

DIMENSION PICT(1025), IMPULS, YP(1025), YM(1025), EN(1025)
COMMON /IMPLS/ XLAST=-500.
DO 5 K=1,1024
  EN(K+1)=Y(1,1025)
  NFIN=Y(1,1025)
  DO 13 K=1,NFIN
    PICT(K+1)=Y(K)
    CONTINUE
    PICT(1)=NFIN
    CALL INIT
    CALL XFRM(2)
    CALL YFRM(2)
    IF(NFIN.LT.70)CALL LINE(-1)
    IF(NFIN.GE.70)CALL LINE(0)
    IF(NFIN.LT.70)CALL SYMBOL(1)
    IF(NFIN.GE.70)CALL SYMBOL(0)
    CALL SIZES(4)
    CALL PLOT(EN,PICT)
    JFIN=NFIN+1
    IF(NFIN.GE.70)GO TO 40
    DO 30 K=2,JFIN
      CALL MOVEA(EN(K),PICT(K))
      CALL DRAWA(EN(K),0,0)
    30 CONTINUE
    CALL MOVEA(0,0,0)
    CALL DRAWA(EN(JFIN),0,0)
    CALL LABLE
    CALL VCURSR(ICHAR,X,Y)
    CALL FIN
    RETURN
  END

  SUBROUTINE PLITRF(IFNCTN,ISCALE,ICHAR)
C* THIS SUBROUTINE PLOTS BOTH THE PHASE AND
C* MAGNITUDE OF THE TRANSFER FUNCTION (LINEAR AND LOG)
C*
  COMMON /FREQ/ YP(1026),YM(1026), PI(1026)
  DO 10 K=1,1024
    PI(K+2)=FLOAT(K-1)*3.14/1024.
    PI(1)=1.025.
    PI(2)=0.
    CALL INIT
    CALL XFRM(2)
    CALL YFRM(2)
    IF(IFNCTN.EQ.3)CALL PLOT(PI,YP)
  10

```

```

      IF(ISCALE.EQ.1) GO TO 20
      DO 15 I=3,1026
      YM(I)=2.0.*ALOG10(YM(I))
15
      YM(2)=0.1
      IF(IFACTN.EQ.4) CALL PLOT(PI,YM)
20
      CALL LABEL
      CALL TSEND
      CALL VCURSR(ICHAR,X,Y)
      CALL FIN
      RETURN
END

SUBROUTINE RSPNSE (IFUNCTN,FLTRGN)

C* THIS SUBROUTINE COMPUTES THE UNIT SAMPLE RESPONSE OF THE SYSTEM
C* THE "Z" VECTOR HOLDS THE DELAYED VALUES
C* FOR THE RECURSIVE CALCULATION.
C*
DIMENSION Z(111)
REAL INPUT
C* "ABVCTR" IS THE PAIR OF VECTORS HOLDING
C* THE VALUES OF A(K), AND B(K)
C* COMMON /ABVCTR/ A(111), B(111)
C* "IMPS" IS THE LABELED COMMON HOLDING THE UNIT SAMPLE RESPONSE
C* COMMON /IMPS/ Y(11025), YS(11025), EN(11025)
C* INITIALIZE THE Z VECTOR
C* XLAST=0.
C* XMIN=0.
C* XMAX=0.
C* DELTA=0.
DO 5 K=1,11
      Z(K)=0.
5
C* COMPUTE THE 1024 POINT UNIT SAMPLE OR STEP RESPONSE
C* DO 30 N=1,1024
C* EACH VALUE OF XSUBN WILL BE ONE EXCEPT FOR THE CASE
C* OF THE UNIT SAMPLE RESPONSE WHEN N>1, AND THEN XSUBN=0.
C* XSUBN = 1.

```

```

      IF(N.GT.1.AND.IFNCTN.EQ.0)XSUBN = 0.
      INPUT=XSUBN
      DO 10 K=2,11
      INPUT=INPUT-A(K)*Z(K)
10     Z(1)=INPUT
      OUTPUT=0.
      DO 20 K=1,11
      OUTPUT=OUTPUT+B(K)*Z(K)
20     DO 25 K=1,10
      Z(12-K)=Z(11-K)
25     IEND=N
      END=N

C* TEST TO SEE IF A STEADY STATE HAS BEEN ACHIEVED.
C* IF(ABS(OUTPUT).GT.XMAX)XMAX=ABS(OUTPUT)
27     DIFFER=.01*XMAX
      IF(Abs(OUTPUT-XLAST).GT.DIFFER)DELT=0.
      XLAST=DELT
      DELTA=DELT+.1
      IF(DELT.GT.20)GO TO 38
      IF(IFNCTN.EQ.0)YS(N)=OUTPUT*FLTRGN
      IF(IFNCTN.EQ.1)YS(N)=OUTPUT*FLTRGN
      IF(IFNCTN.EQ.0)YS(1025)=IEND-15
      IF(IFNCTN.EQ.1)YS(1025)=IEND-15
      RETURN
999    END

      SUBROUTINE FRQNCY(INNUM, NDEN, FLTRGN)
C* FREQUENCY COMPUTES THE FREQUENCY RESPONSE FOR
C* THE FILTER BEING ANALYZED.
C* COMMON /ABVCTR/A(11),B(11)
COMMON /FREQ/ YP(1026),YM(1026)
REAL*8 X,Y,THETA,ZRO,ONE,AA(11),BB(11),XX,G(2)
COMPLEX*16 Z,FRCBOT,FRCBOT,HOFZ,LEXP,TERM,TERMD
EQUIVALENCE {G,HOFZ}
ZRO=0.0D+00
ONE=1.0D+00

C* MAKE THE COEFFICIENTS DOUBLE PRECISION
C*
      DO 20 K=1,11
      AA(K)=A(K)
      BB(K)=B(K)
20     CUNTINJE
C* COMPUTE PHASE AND MAGNITUDE OF H(Z)

```

```

C* DO 60 K=1,1025
      THETA=FLOAT(K-1)*3.14159265/1024.
 25   Z=CDDEXP(DCMPLX(ZR0,THETA))
      FRCTOP=0.
      FRCBOT=0.

C* COMPUTE THE VALUE OF THE NUMERATOR OF H(Z)
C*
C* DO 40 N=1,NNUM
      ZEXP=Z**((N-1)
      TERM=DCMPLX(BB(N),ZRO)/ZEXP
      FRCTOP=FRCTOP+TERM
      CONTINUE
 40   C* COMPUTE THE VALUE OF THE DENOMINATOR FACTORS OF H(Z)
C*
C* DO 50 N=2,NDEN
      TERMD=DCMPLX(A(N),ZRO)/Z**((N-1)
      FRCBOT=FRCBOT+TERMD
      CONTINUE
 50   C* GET H(Z) IN FINAL FORM
C* H0FZ=FRCTOP/(DCMPLX(ONE,ZRO)+FRCBOT)
C* COMPUTE THE MAGNITUDE OF H(Z)
C*
C* YM(K+2)=CDABS(H0FZ)
 55   YM(K+2)=YM(K+2)*FLTRGN
C* COMPUTE THE PHASE OF H(Z)
C*
C* X=G(1)
Y=G(2)
IF(X.EQ.ZRO.AND.Y.EQ.ZRO)YP(K+2)=YP(K+1)
IF(X.EQ.ZRO.AND.Y.EQ.ZRO)GO TO 60
XX=DATAN2(Y,X)
YP(K+2)=XX
CONTINUE
YP(L)=1.025.
YP(2)=0.
YM(1)=1.025.
YM(2)=0.
RETURN
END

```

```

SUBROUTINE FLTR2(FLTRGN)
C* FLTR2 WRITES A LISTING OF ALL
C* POLE AND ZERO LOCATIONS FOR REVIEW BEFORE
C* PROCEEDING WITH THE PLOTTING OF RESPONSES
C*
COMMON IROOTS(4),POLZRO(20,5)
DIMENSION IRTTP(5)
DATA IZ/1HZ/,IP/1HP/,IZP/2HZP/
DATA IRTTP/2H ,2HRZ,2HCL,2HRP,2HCP/
CALL INIT
CALL FIN
WRATE{6,102}{17,I=1,70}
102 FORMAT{1X,70A1}
WRITE{6,108}{1X,Z,5X,REAL,Z,5X,IMAGINARY,Z,5X,Z}
108 1,6X,RHC,6X,Z,I=1,70}
WRITE{6,102}{12,I=1,70}
DO 10 I=1,10
 1TYPEP=POLZRO{1,5}+1.
 1IF{POLZRO{1,5}>NE2: AND POLZRO{1,5}>NE4:}
 1IWRITE{6,104}{1,5}{POLZRO{1,J},J=1,4}IRTP{1,TYPEP}
 1IF{POLZRO{1,5}>EQ2: OR POLZRO{1,5}>EQ4:}
 1IWRITE{6,103}{1,5}{POLZRO{1,J},J=1,4}IRTP{1,TYPEP}
103 FORMAT{1Z,F10.7,-F10.7,2,F10.7,2,F10.7,
 1,3X,Z,+/-F10.7,2,F10.7,2,F10.7,2,F10.7,
 1,FORMAT{1Z,F10.7,2,A2,Z,F10.7,2,A2,Z,F10.7,
 10 CONTINUE
 10 WRITE{6,112}{17P,I=1,35}
 112 FORMAT{1X,35A2}
  DO 20 I=11,20
  1TYPEP=POLZRO{1,5}+1.
  1IF{POLZRO{1,5}>NE2: AND POLZRO{1,5}>NE4:}
  1IWRITE{6,106}{1,5}{POLZRO{1,J},J=1,4}IRTP{1,TYPEP}
  1IF{POLZRO{1,5}>EQ2: OR POLZRO{1,5}>EQ4:}
  1IWRITE{6,105}{1,5}{POLZRO{1,J},J=1,4}IRTP{1,TYPEP}
105 FORMAT{1P,F10.7,+,F10.7,P,A2,P,F10.7,
 1,3X,P,+/-F10.7,P,A2,P,F10.7,
 106 FORMAT{1P,F10.7,P,A2,P,F10.7,P,F10.7,
 1,FORMAT{1P,F10.7,P,A2,P,F10.7,P,F10.7,
 20 CONTINUE
 20 WRITE{6,102}{1P,I=1,70}
 20 WRITE{6,107}{1,}
 107 FORMAT{/}
 107 WRITE{6,110}{1,10}IROOTS{1}
 110 FORMAT{20X,NUMBER OF REAL ZEROS:,I3}
 110 WRITE{6,111}{1,11}IROOTS{2}

```

AD-A093 252

NAVAL POSTGRADUATE SCHOOL MONTEREY CA  
ADVANCED SIMULATION OF DIGITAL FILTERS. (U)  
SEP 80 G S DOYLE

F/G 9/3

UNCLASSIFIED

NL

4 of 4  
AD-A093 252

END  
DATE 4-19-80  
2 81  
DHC

```

111  FORMAT(20X,'NUMBER OF COMPLEX ZERO PAIRS:',I3)
112  WRITE(6,113) IROOTS(3)
113  FORMAT(20X,'NUMBER OF REAL POLES:',I3)
114  WRITE(6,114) IROOTS(4)
115  FORMAT(20X,'NUMBER OF COMPLEX POLE PAIRS:',I3)
116  WRITE(6,117) FILTER
117  FORMAT(25X,'FILTER GAIN:',F12.8)
118  WRITE(6,115)
119  FORMAT(' HIT SPACE THEN RETURN')
120  READ(5,116)
121  FORMAT(1A1)
122  RETURN
123  END

C* SUBROUTINE LABLE WRITES THE LABLES ON EACH
C* OF THE FIVE PLOTS DRAWN
C*
124  DIMENSION ITITLE(40)
125  CALL ANMODE
126  READ(2,100) IX,IY,INUM,(ITITLE(J),J=1,40)
127  CALL RECOVER
128  CALL MOVABS(IX,IY)
129  CALL ANMODE
130  WRITE(6,101) ITITLE(J),J=1,INUM
131  FORMAT(1X,30A1)
132  READ(2,100) IX,IY,INUM,(ITITLE(J),J=1,40)
133  DO 10 I=1,INUM
134    CALL FECVR
135    CALL MOVABS(IX,IY)
136    CALL ANMODE
137    WRITE(6,102) ITITLE(I)
138    FORMAT(1X,A1)
139    IY=IY-22
140    READ(2,100) IX,IY,INUM,(ITITLE(J),J=1,40)
141    CALL RECOVER
142    CALL MOVABS(IX,IY)
143    CALL ANMODE
144    WRITE(6,101) (ITITLE(J),J=1,INUM)
145    READ(2,100) IX,IY,INUM,(ITITLE(J),J=1,40)
146    CALL RECOVER
147    CALL MOVABS(IX,IY)
148    CALL ANMODE
149    WRITE(6,101) (ITITLE(J),J=1,INUM)
150    CALL RECOVER
151    CALL TSEND
152  RETURN
153  END

```

APPENDIX I: SOURCE DECK FOR ASDF COMMAND: HRD\$CPY

```

ASDF7001
ASDF7002
ASDF7003
ASDF7004
ASDF7005
ASDF7006
ASDF7007
ASDF7008
ASDF7009
ASDF7010
ASDF7011
ASDF7012
ASDF7013
ASDF7014
ASDF7015
ASDF7016
ASDF7017
ASDF7018
ASDF7019
ASDF7020
ASDF7021
ASDF7022
ASDF7023
ASDF7024
ASDF7025
ASDF7026
ASDF7027
ASDF7028
ASDF7029
ASDF7030
ASDF7031
ASDF7032
ASDF7033
ASDF7034
ASDF7035
ASDF7036
ASDF7037
ASDF7038
ASDF7039
ASDF7040
ASDF7041
ASDF7042
ASDF7043
ASDF7044
ASDF7045
ASDF7046
ASDF7047
ASDF7048

***** SOURCE DECK FOR ASDF COMMAND: HRD$CPY ****
***** COMMON IROOTS(4) POLZRO(20,5),IERROR
***** COMMON /ABVCTR/ A(11),B(11)
***** COMMON /IMPULS/ Y(1026),YS(1026),EN(1026)
***** COMMON /FREQ/ YP(1026),WM(1026),PI(1026),WMDB(1026)
***** CALL ERRSET(208,256,-1,1,1)
***** LINEAR=1
***** LOG=2

C* INITIALIZE A AND B TO ZERO
C* DO 5 K=1,20
      DO 5 K=1,20
        A(K)=0.
        B(K)=0.
5
C* READ THE POLZRO TABLE OFF OF THE FILE
C* DO 20 I=1,20
      DO 20 I=1,20
        READ(5,100)(POLZRO(I,J),J=1,5)
100   FORMAT(1X,5F12.8)
C* READ THE IROOTS VALUES, AND FILTER GAIN FROM THE FILE
C* READ(5,101)(IROOTS(I),I=1,4)
      READ(5,101)(IROOTS(I),I=1,4)
101   FORMAT(1X,4I2)
        READ(5,102)FLTRGN
102   FORMAT(1X,1F12.8)
        FLTRGN=ABS(FLTRGN)

C* PRINT OUT A TABLE OF THE POLES AND ZEROS
C* CALL FLTR2(FLTRGN)
C* GENERATE THE A(K) COEFFICIENTS
      CALL ASUBK(A,NORDER)
      NDEN=NORDER+1
C* GENERATE THE B(R) COEFFICIENTS
      CALL BSUBR(B,NORDER)
      NNIN=NORDER+1
C* CHECK TO SEE IF THE FILTER IS CAUSAL

```

```

C*      IF(NDEN.GT.1) WRITE(6,103)
103    FORMAT(10F7.4,FILTER IS NOT CAUSAL - PROGRAM TERMINATES)
C*      ADJUST THE COEFFICIENTS IF NNUM DOES NOT EQUAL NDEN
C*      IF(NNUM.NE.NDEN) CALL ADJUST(NNUM,NDEN)
C*      COMPUTE THE UNIT SAMPLE RESPONSE
C*      CALL RSPNSE(0,FLTRGN)
C*      CALCULATE THE STEP RESPONSE
C*      CALL RSPNSE(1,FLTRGN)
C*      CALCULATE THE FREQUENCY RESPONSE
C*      CALL FRQNCY(NDEN,FLTRGN)
C*      CALL PRPLT(IYIPTS,IYSPTS,NUMPLT)
C*      PLOT THE UNIT SAMPLE RESPONSE
C*      CALL PLTIMP(IYIPTS,FLTRGN,NUMPLT)
C*      PLOT THE STEP RESPONSE
C*      CALL PLTSTP(IYIPTS,FLTRGN,NUMPLT)
C*      PLOT THE MAGNITUDE OF THE TRANSFER FUNCTION
C*      CALL PLTTRF(3,LINEAR,FLTRGN,NUMPLT)
C*      PLOT THE MAGNITUDE OF THE TRANSFER FUNCTION
C*      CALL PLTTRF(4,LINEAR,FLTRGN,NUMPLT)
C*      CALL PLTTRF(4,LOG,FLTRGN,NUMPLT)
C*      PLOT THE UNIT CIRCLE WITH POLES AND ZEROS
C*      CALL UNTCR(NUMPLT)
C*      OUTPUT THE DATA
C*      CALL OUTNUM
      STOP
      END

```

```

SUBROUTINE ADJUST(INNUM,NDEN)
COMMON /ABVCTR/A(11),B(11)
IDELTA=NDEN-NNUM
1STOP=1-IIDELTA
DO 10 I=1,1STOP
   B(12-I)=B(12-I-IDELTA)
  10 DO 20 K=1,1IDELTA
   B(K)=0
  20 NNUH=NDEN
      RETURN
END

SUBROUTINE OUTNUM
C* OUTNUM PRINTS OUT THE NUMERICAL VALUES
C* OF THE FILTER'S RESPONSES
C*
COMMON /IMPULS/Y1(1026),YS(1026),YM(1026),PI(1026),
COMMON /FREQ/YP(1026),VM(1026),VMDR(1026)
DIMENSION M(1026)
DO 20 L=1,1026
   M(L)=L-1
  20 DO 40 I=1,18
      CALL HEADNG
     DO 40 J=1,6
        IBEG=(I-1)*60+(J-1)*10+1
        IEND=IBEG+9
        IF(I.EQ.18.AND.J.EQ.1)IEND=1024
        WRITE(6,104)(M(K),Y1(K),YS(K),YP(K),YM(K),PI(K),K=IBEG,IEND)
       104 FORMAT(10(2X),10E20.8,3E21.8,/,10E20.4)
        IF(I.EQ.18.AND.J.EQ.1)GO TO 41
        CONTINUE
       40 WRITE(6,105)
       41 FORMAT(1H1)
       105 FORMAT(1H1)
      RETURN
END

SUBROUTINE HEADING
C* HEADING PRINTS THE PAGE HEADINGS
C*
DATA IX/1HX/
WRITE(6,100)
  100 FORMAT(1H1)
  WRITE(6,101)(IX,I=1,114)
  101 FORMAT(IX14AI)
  WRITE(6,108)

```

```

108  FORMAT( ' X' ,1I3,' 1I2X, ' X' )
      WRITE(6,103) X, N, 5X, 'UNIT SAMPLE RESPONSE', 3X, 'STEP RESPONSE', 3X
103  FORMAT( ' X' ,PHASE OF H(Z), {RADIAN}, ' 2X, MAGNITUDE OF H(Z), 4X,
      X' ,OMEGA (RADIAN), X' )
      WRITE(6,108)
      WRITE(6,101)(IX, I=1,114)
      WRITE(6,102)
      FORMAT(7/
      RETURN
      END

      SUBROUTINE UNTCR( NUMPLT)
C*  UNTCR PLOTS THE UNIT CIRCLE AND
C*  ALL POLES AND ZEROS
C*
      DIMENSION UCX(362),UCY(362)
      COMMON IROOTS(4),POLZRO(20,5),I_ERROR
      DO 10 I=1,361
      THETA=FLOAT(I-1)*2*3.14159/360.
      UCX(I)=2.*COS(THETA)
      UCY(I)=2.*SIN(THETA)
10    CONTINUE
      CALL BOX(0,FLTRGN,NUMPLT)
      CALL PL0T(7117,5381,-3)
      CALL PL0T(2.75,4.25,+3)
      CALL PL0T(8.25,4.25,+2)
      CALL PL0T(5.5,1.5,+3)
      CALL PL0T(5.5,7.0,+2)
      IUP=+3
      IDOWN=-2
      HDLTA=.2
      X=2.75
      DO 70 I=1,23
      IF(I,NE.7,AND.I,NE.17,AND.I,NE.2,AND.I,NE.22)GO TO 71
      CALL PL0T(X,Y,IUP)
      Y=4.45
      CALL PL0T(X,Y,IDOWN)
      GO TO 70
71    CALL PL0T(X,Y,IUP)
      Y=Y-VDLTA
      CALL PL0T(X,Y,IDOWN)
      X=X+HDLTA
      VDLTA=.25

```

```

HDLTA=.2
Y=1.5
DO 80 I=1,23
X=5.4
IF(I,1.NE.7.AND.I,1.NE.17.AND.I,1.NE.2.AND.I,1.NE.22)GO TO 81
X=5.3 PLOT(X,Y,IUP)
CALL PLOT(X,Y,IDOWN)
GO TO 80
CALL PLOT(X,Y,IUP)
X=X+HDLTA
CALL PLOT(X,Y,IDOWN)
Y=Y+VOLTA
CALL PLOT(5.5*25,-3)
DO 60 I=1,360
CALL PLOT(UCX(I),UCY(I),+3)
CALL PLOT(UCX(I),UCY(I),+2)
CALL PLOT(UCX(I),UCY(I),+2)
CALL SYMBOL(-1.4,+2.8125,1875,11HUNIT CIRCLE ZERO.)
CALL SYMBOL(-2.4,-3.,1875,26HFILTER POLE ZERO LOCATIONS,0.,26)
DO 30 I=1,20
DO 30 J=1,3
POLZRO(I,J)=POLZRO(I,J)*2.5
DO 40 I=1,10
IF(POLZRO(I,3)*EQ.-2.5)GO TO 40
IF(POLZRO(I,1)=2.625*COS(POLZRO(I,4))
POLZRO(I,2)=2.625*SIN(POLZRO(I,4))
CALL SYMBOL(POLZRO(I,5).NE.1.)CALL SYMBOL(POLZRO(I,2),-1)
IF(POLZRO(I,5).NE.1.)CONTINUE
X1,0,*-1
GO TO 40
IF(POLZRO(I,5).NE.1.)CALL SYMBOL(POLZRO(I,2),25,10,-1)
40 CONTINUE
DO 50 I=1,10
IF(POLZRO(I,1)*EQ.-2.5)GO TO 50
CALL SYMBOL(POLZRO(I,3).NE.3.)CALL SYMBOL(POLZRO(I,4),-1)
IF(POLZRO(I,5).NE.1.)CONTINUE
CALL PLOT(0.,0.,4999)
50 RETURN
END

SUBROUTINE ASJBK (POLE,NORDER)
ASDF7193
ASDF7194
ASDF7195
ASDF7196
ASDF7197
ASDF7198
ASDF7199
ASDF7200
ASDF7201
ASDF7202
ASDF7203
ASDF7204
ASDF7205
ASDF7206
ASDF7207
ASDF7208
ASDF7209
ASDF7210
ASDF7211
ASDF7212
ASDF7213
ASDF7214
ASDF7215
ASDF7216
ASDF7217
ASDF7218
ASDF7219
ASDF7220
ASDF7221
ASDF7222
ASDF7223
ASDF7224
ASDF7225
ASDF7226
ASDF7227
ASDF7228
ASDF7229
ASDF7230
ASDF7231
ASDF7232
ASDF7233
ASDF7234
ASDF7235
ASDF7236
ASDF7237
ASDF7238
ASDF7239
ASDF7240

```

```

C* GENERATE THE AK COEFFICIENTS FROM THE POLES
C* COMMON IROOTS(4), POLZRO(20,5), IERROR
C* COMPLEX POLES(11), ACDEF(11)
C* REAL POLE(11)
C* INITIALIZE ALL THE VECTORS AND INDICES TO ZERO
C* DO 5 K=1,11
C*      POLES(K)=(0.,0.)
C*      POLE(K)=0.
C*      ACDEF(K)=0.
5   C** "J" INDEXES THE TABLE "POLES"
C** "K" INDEXES THE TABLE "POLZRO"
      J=1
      K=1
C* COMPUTE THE ORDER OF THE SYSTEM OF POLES
C* NORDER=IROOTS(3)+2*IROOTS(4)
C* IF(NORDER.NE.0)GO TO 10
C*      POLER(1)=1.0
C*      RETURN
C* THE VECTOR "POLES" WILL CONTAIN A LIST OF ALL
C* THE POLES, I.E., X+JO, X-JY, . . .
10  C*      POLES(J)=CHPLX(POLZRO(10+K,1),POLZRO(10+K,2))
C* TEST TO SEE IF ALL ROOTS HAVE BEEN
C*      IF(J.EQ.NORDER)GO TO 20
C*      J=J+1
C* IF THE RJOT IS REAL CONTINUE PROCESSING THE NEXT ROOT
C*      IF(POLZRO(K+10,5).NE.3)GO TO 15
C*      K=K+1
C*      GO TO 10
C* SINCE THE ROOT IS COMPLEX PUT THE CONJUGATE
C* OF THE ROOT IN THE "POLES" TABLE.
15  C*      POLES(J)=CHPLX(POLZRO(10+K,1),-POLZRO(10+K,2))
C*      IF(J.EQ.NORDER) GO TO 20

```

```

J=J+1
K=K+1
GO TO 10

C* GENERATE THE COEFFICIENTS FOR THE D(Z) POLYNOMIAL
C* OF THE TRANSFER FUNCTION H(Z).
C* 20 CALL COEFF(POLES,NORDER,ACDEF)
C* C CHANGE THE COEFFICIENTS FROM COMPLEX ASUBK TO REAL ASUBK
C*
C* DO 40 J=1,11
C* POLE(J)=REAL(ACDEF(J))
C* RETURN
C* END

SUBROUTINE BSUBR(ZERO,NORDER)

C* GENERATE THE B(R) COEFFICIENTS FROM THE ZEROS
C* COMMON IROOTS(4),POLZRO(20),1,ERROR
C* COMPLEX ZEROES(11),BCDEF(11)
C* REAL ZERO(11)
C* C INITIALIZE ALL VECTORS AND INDICES
C* DO 5 K=1,11
C* ZEROS(K)=(0.,0.)
C* ZERO(K)=0
C* BCDEF(K)=(0.,0.)
C* 5
C* "J" INDEXES THE "ZEROS" TABLE
C* "K" INDEXES THE "POLZRO" TABLE
C* C
C* J=1
C* K=1
C* COMPUTE THE ORDER OF THE SYSTEM OF ZEROS.
C* NORDER=IROOTS(1)+2*IROOTS(2)
C* IF(NORDER.NE.0)GO TO 10
C* ZERO(1)=1.0
C* RETURN
C* C THE VECTOR "ZEROS" CONTAINS A LIST OF ALL
C* OF THE ZEROS, IE., X+JY, X+JY, . . .
C* 10 ZEROS(J)=CMPLX(IPOLZRO(K,1),POLZRO(K,2))

```

```

C* CHECK TO SEE IF ALL THE ROOTS HAVE BEEN PROCESSED
C* IF(J, EQ, NORDER) GO TO 20
      J=J+1
C* IF THE ROOT IS REAL CONTINUE PROCESSING THE NEXT ROOT
      IF(POLZR(K,5).NE.1) GO TO 15
      K=K+1
      GO TO 10
C* SINCE THE ROOT IS COMPLEX, ENTER THE CONJUGATE
C* INTO THE TABLE "ZEROS".
C* 15 ZEROS(J)=CMPLX(POLZR(K,1),-POLZR(K,2))
      I=F(J, EQ, NORDER) GO TO 20
      J=J+1
      K=K+1
      GO TO 10
C* GENERATE THE BSUBR COEFFICIENTS
C* 20 CALL COEFF(ZEROS, NORDER, BCoeff)
C* MAKE THE COEFFICIENTS BSUBR REAL.
C* DO 40 J=1,11
      ZERO(J)=REAL(BCoeff(J))
      RETURN
END

SUBROUTINE COEFF(V,N,H1)
C* "V" - VECTOR OF ROOTS; "N" - THE ORDER OF THE SYSTEM
C* "H1" - VECTOR WITH THE FINAL COEFFICIENTS
C* H(1)=Z**(-1), H(2)=Z**(-1), . . . , H(N)=Z**(-10)
C* COMPLEX H1(11), H2(11), H3(11), V(11)
C* INITIALIZE VECTORS
      ZERO=0
      DO 10 I=1,11
      H1(I)=(0.,0.)
      H2(I)=(0.,0.)
      H3(I)=(0.,0.)
      H1(I)=(1.,0.)
10   H3(I)=(1.,0.)

C* THE ROOTS COME FROM THE FORMER SUBROUTINE

```

```

C* THESE ARE ROOTS OF THE POLYNOMIALS N(Z), AND D(Z)
C* WHERE H(Z)=N(Z)/D(Z)
C* THE FACTORS OF THE POLYNOMIAL ARE OF THE FORM Z-ROOT
C*
      DO 15 K=1,11
      V(K)=-V(K)
15
C* WHEN K=N, WE HAVE GENERATED THE H1 COEFFICIENTS
C* OF N(Z), OR D(Z) OF H(Z)=N(Z)/D(Z)
C* THE REMAINING ITERATIONS ARE PERFORMED TO SIMPLIFY
C* OBTAINING COEFFICIENTS FOR N(Z**-1), AND D(Z**-1) LATER
C*
      DO 30 K=1,10
C* "H2" REPRESENTS THE PREVIOUS RESULT TIMES Z**(-1)
C*
      DO 40 I=1,10
      H2(I+1)=H1(I)
      H2(1)=0.0
40
      DO 50 I=1,1
      H3(I)=H1(I)*V(I)
50
C* GENERATE THE NEW FINAL PRODUCT WITH K ROOTS MULTIPLIED.
C*
      DO 60 I=1,1
      H1(I)=H2(I)+H3(I)
60
C* GET THE NEXT ROOT TO BE MULTIPLIED AND PUT IT INTO "V(1)"
C*
      DO 70 I=1,1
      V(1)=V(I+1)
70
      CONTINUE
30
C* TO GET THE COEFFICIENTS FOR H(Z**-1)=N(Z**-1)/D(Z**-1)
C* THE ORDER OF THE COEFFICIENTS MUST BE REVERSED.
C*
      DO 80 I=1,1
      H2(I)=H1(I-1)
      DO 90 I=1,1
      H1(I)=H2(I)
90
      RETURN
80
      END
95
C* SUBROUTINE RSPNSE (IFNC TN,FLTRGN)
C* THIS SUBROUTINE COMPUTES THE UNIT SAMPLE RESPONSE OF THE SYSTEM
C* THE "Z" VECTOR HOLDS THE DELAYED VALUES
ASDF7386
ASDF7387
ASDF7388
ASDF7389
ASDF7390
ASDF7391
ASDF7392
ASDF7393
ASDF7394
ASDF7395
ASDF7396
ASDF7397
ASDF7398
ASDF7399
ASDF7400
ASDF7401
ASDF7402
ASDF7403
ASDF7404
ASDF7405
ASDF7406
ASDF7407
ASDF7408
ASDF7409
ASDF7410
ASDF7411
ASDF7412
ASDF7413
ASDF7414
ASDF7415
ASDF7416
ASDF7417
ASDF7418
ASDF7419
ASDF7420
ASDF7421
ASDF7422
ASDF7423
ASDF7424
ASDF7425
ASDF7426
ASDF7427
ASDF7428
ASDF7429
ASDF7430
ASDF7431
ASDF7432
ASDF7433

```

```

C* FOR THE RECURSIVE CALCULATION.
C* REAL*8 XMIN,XMAX,XLAST,XSUBN,INPUT,OUTPUT,AA(11),BB(11),
C* XZ(11),DIFFER,DFTRGN,ZRO,ONE,PTOONE
C* "ABVCTR" IS THE PAIR OF VECTORS HOLDING
C* THE VALUES OF A(K), AND B(K)
COMMON /ABVCTR/ A(11), B(11)
C* "IMPULS" IS THE LABELED COMMON HOLDING THE UNIT SAMPLE RESPONSE
COMMON /IMPULS/ YI(1026), YS(1026), EN(1026)
C* INITIALIZE THE CONSTANTS AND Z VECTOR
C* IFLAG=0
ZRO=0.0D+00
ONE=1.0D+00
PTOONE=1.0D-02
XMIN=ZRO
XMAX=ZRO
XLAST=ZRO
DELTAE=0
DFTRGN=FLTRGN
DO 4 K=1,1
  AA(K)=A(K)
  BB(K)=B(K)
  DO 5 K=1,1
    Z(K)=0.
5
C* COMPUTE THE 1024 POINT UNIT SAMPLE OR STEP RESPONSE
C* DO 30 N=1,1024
C* EACH VALUE OF XSUBN WILL BE ONE EXCEPT FOR THE CASE
C* OF THE UNIT SAMPLE RESPONSE WHEN N>1, AND THEN XSUBN=0.
C* XSUBN=ONE
IF(N.GT.1.AND.IFNCTN.EQ.0)XSUBN=ZRO
INPUT=XSUBN
DO 10 K=2,1
  INPUT=INPUT-A(K)*Z(K)
10 Z(1)=INPUT
  OUTPUT=ZRO
  DO 20 K=1,1
    OUTPUT=OUTPUT+B(K)*Z(K)
20 DO 25 K=1,10

```

```

25   Z(12-K)=Z(11-K)
      IEND=N
C*  TEST TO SEE IF A STEADY STATE HAS BEEN ACHIEVED.
C*
      IF(DABS(OUTPUT).GT.XMAX)XMAX=DABS(OUTPUT)
      DIFFER=PTOONE*XMAX
      IF(DABS(OUTPUT-XLAST).GT.DIFFER)DELT=0.
      XLAST=OUTPUT
      DELTA=DELT+1.
      IF(IFNCTN.EQ.0)YI(N)=OUTPUT*DFTRGN
      IF(IFNCTN.EQ.1)YS(N)=OUTPUT*DFTRGN
      IF(DELT.LE.20.)GO TO 30
      IFLAG=1
      DELTA=-2000.0
      IF(IFNCTN.EQ.0)YI(1025)=IEND-15
      CONTINUE
      IF(IFNCTN.EQ.0.AND.IFNCTN.EQ.0)YI(1025)=1024.
      IF(IFLAG.EQ.0.AND.IFNCTN.EQ.1)YS(1025)=1024.
      RETURN
END

38   SUBROUTINE FRQNY(NUML,NUEN,FLTRGN)
      COMMON /ABVCTR/A(11),B(11)
      COMMON /FREQ/YP(1026),YM(1026),PI(1026),YMDB(1026)
      REAL*8 X,Y,THETA,ZRO,ONE,AA(11),BB(11),XX,G(2)
      COMPLEX*16 Z,FRCBOT,FRCTOP,HOFZ,ZEXP,TERM,TERMD
      EQUIVALENCE {G,HOFZ}
      ZRO=0.0D+00
      ONE=1.0D+00
      END

30   C* MAKE THE COEFFICIENTS DOUBLE PRECISION
      DO 456 KKK=1,11
        AA(KKK)=A(KKK)
        BB(KKK)=B(KKK)
      CONTINUE
      456  DO 60 K=1,1025
        THETA=FLOAT(K-1)*3.14159265/1024.
        Z=CDEXP(DCMPLX(ZRO,THETA))
        FRCTOP=0.
        FRCBOT=0.
        DO 40 N=1,NUML
          ZEXP=Z***(N-1)
          TERM=DCMPLX(BB(N)*ZRO)/ZEXP
          FRCTOP=FRCTOP+TERM
        CONTINUE
      60   END

```

```

DO 50 N=2,NDEN
TERMD=DCMPLX(N,ZRO)/Z**(N-1)
FRCBOT=FRCBOT+TERMD
50
C* CALCULATE H(Z)
C* HOFZ=FRCTOP/(DCMPLX(ONE,ZRO)+FRCBOT)
      YH(K)=YH(K)*FLTRGN
55
      X=G(1)
      Y=G(2)
      IF(X.EQ.ZRO.AND.Y.EQ.ZRO)GO TO 60
      X=DATAN2(Y,X)
      YP(K)=XX
      CONTINUE
      RETURN
END

SUBROUTINE FLTR2(FLTRGN)
COMMON IROOTS(4),POLZRO(20,5)
DIMENSION IRTTP(5)
DATA IRTTP/1HZ,1P/1HP,IZP/2HZP/
DATA IRTTP/2H ,2HRZ,2HRP,2HCP/
WRITE(6,100)
100 FORMAT(1H1)
WRITE(6,101)
101 FORMAT(6I102)/(1Z,I=1,70)
102 FORMAT(3IX,7OAI)
      WRITE(6,108)
108 FORMAT(3IX,7I5X,"REAL",6X,7I3X,"IMAGINARY",3X,"Z"
      1,6X,1R0,6X,7I5X,"THETA",5X,7RF,Z,I=1,70,
      DO 100 I=1,10
      ITYPEP=POLZRO(I,5)+1
      IF(POLZRO(I,5).NE.2D(.1,0))AND(POLZRO(I,5).NE.4D(.1))
      1 WRITE(6,104)(POLZRO(I,J),(POLZRO(I,J).EQ.POLZRO(I,J)).IRTP(I,TYPEP)
      1 IF(POLZRO(I,5).EQ.2D(.1,0).OR.POLZRO(I,J).EQ.4D(.1))
      1 WRITE(6,103)(POLZRO(I,J),J=1,4).IRTP(I,TYPEP)
103 FORMAT(30X,Z+,F10.7,Z+,F10.7,Z+,F10.7,Z+,F10.7,
      13X,Z+-,F10.7,Z+,A2+,Z+,F10.7,Z+,A2+,Z+,F10.7,
      104 FORMAT(30X,Z+,F10.7,Z+,A2+,Z+,F10.7,Z+,F10.7,
      10 CONTINUE
      WRITE(6,112)(IZP,I=1,35)
112 FORMAT(3IX,35A2)

```

```

DO 20 I=11,20
  ITYPE=POLZR(1,5)*I
  IF(ITYPE.EQ.2) AND .NOT.POLZR(1,5).NE.4 ITYPE=4
  IWRITE(6,106)(POLZR(1,5),J=1,4)
  IWRITER(6,105)(POLZR(1,5),EQ2,J=1,4)
  IWRITER(6,105)(POLZR(1,5),P+,J=1,4)
  IWRITER(6,105)(POLZR(1,5),P-/J,1,4)
  105  FORMAT(30X,P+/-F10.7,P10.7,P+,P-,F10.7,
  106  FORMAT(30X,P,F10.7,P10.7,P+,P-,F10.7,P+,F10.7,
  1, P,F10.7,P10.7,P+,P-,F10.7,P+,F10.7,
  20  CONTINUE
      WRITE(6,102),(IP,I=1,70)
      WRITE(6,107)
  107  FORMAT(//)
      WRITE(6,110)IROOTS(1)
  110  FORMAT(50X,'NUMBER OF REAL ZEROS:',I3)
      WRITE(6,111)IROOTS(2)
  111  FORMAT(50X,'NUMBER OF COMPLEX ZERO PAIRS:',I3)
      WRITE(6,113)IROOTS(3)
  113  FORMAT(50X,'NUMBER OF REAL POLES:',I3)
      WRITE(6,114)IROOTS(4)
  114  FORMAT(50X,'NUMBER OF COMPLEX POLE PAIRS:',I3)
      WRITE(6,115)FLTRGN
  115  FORMAT(50X,'FILTER GAIN:',F12.8)
      RETURN(6,100)
END

SUBROUTINE PRPLT(IYIPTS,IYSPTS,NUMPLT)
COMMON /FREQ/YP(1026),YS(1026),EN(1026),
NUMPLT=1
IYIPTS=YI(1025)
IYSPTS=YS(1025)
CALL WINDOW(0.,45.,0.,21.11)
CALL PLOTS(0.,0.,0.,0.)
ISUB=2
IF(ABS(YI(1)).LE.ABS(YI(2)))ISUB=1
ITEMP=YI(ISUB)
YI(ISUB)=0.
CALL SCALE(YI,5.,1024.,+1)
ISUB=2
IF(ABS(YS(1)).LE.ABS(YS(2)))ISUB=1
ASDF7579
ASDF7580
ASDF7581
ASDF7582
ASDF7583
ASDF7584
ASDF7585
ASDF7586
ASDF7587
ASDF7588
ASDF7589
ASDF7589
ASDF7591
ASDF7592
ASDF7593
ASDF7594
ASDF7595
ASDF7596
ASDF7597
ASDF7598
ASDF7599
ASDF7600
ASDF7601
ASDF7602
ASDF7603
ASDF7604
ASDF7605
ASDF7606
ASDF7607
ASDF7608
ASDF7609
ASDF7610
ASDF7611
ASDF7612
ASDF7613
ASDF7614
ASDF7615
ASDF7616
ASDF7617
ASDF7618
ASDF7619
ASDF7620
ASDF7621
ASDF7622
ASDF7623
ASDF7624
ASDF7625

```

```

C* THIS SUBROUTINE SCALES THE ORDINATE
C* DATA BEFORE PLOTTING
C*
COMMON /IMPULS/YI(1026),YS(1026),EN(1026),
NUMPLT=1
IYIPTS=YI(1025)
IYSPTS=YS(1025)
CALL WINDOW(0.,45.,0.,21.11)
CALL PLOTS(0.,0.,0.,0.)
ISUB=2
IF(ABS(YI(1)).LE.ABS(YI(2)))ISUB=1
ITEMP=YI(ISUB)
YI(ISUB)=0.
CALL SCALE(YI,5.,1024.,+1)
ISUB=2
IF(ABS(YS(1)).LE.ABS(YS(2)))ISUB=1

```

```

TEMP=YS(IISUB)
YS(IISUB)=0
CALL SCALE(YS,5.,1024.,+1)
YH(1)=0
TEMP=YH(1)
CALL SCALE(YH,5.,1024.,+1)
YH(1)=TEMP
DO 10 I=1,1024
  IF(YH(I) .EQ. 0.) YM(I)=1E-70
  YMDB(I)=20.*ALDG10(YM(I))
  IISUB=2*(YMDB(I))+1
  IF(ABS(YMDB(I))+1.E-ABSYMDB(I)) IISUB=1
  TEMP=YMDB(IISUB)*LE.ABS(YMDB(I))+1
C* THIS STATEMENT PREVENTS THE STAIRCASE FOR
C* ALL PASS FILTERS
C*
      YMDB(IISUB)=-10.
      CALL SCALE(YMDB,5.,1024.,+1)
      YMDB(1)=TEMP
      CALL SCALE(YP,5.,1024.,+1)
      RETURN
END

SUBROUTINE PLTIMP(LAST,FLTRGN,NUMPLT)
C* THIS SUBROUTINE PLOTS THE UNIT SAMPLE RESPONSE
C* COMMON /IMPULS/YI(1026),YS(1026),EN(1026)
CALL BOX(1,FLTRGN,NUMPLT)
DO 5 I=1,1024
EN(I)=I-1
CALL SCALE(EN,10.,LAST)+1)
CALL AXIS(2,179.,2,2012,1HN,-1,8,0,0,EN(LAST+1),EN(LAST+2))
CALL AXIS(2,179.,2,2012,20HN,1,8,0,0,RESPONSE,+20.,5.,90.,YI(1025))
X YI(1026)
X ALLPLOT(2,179.,2,2012,-3)
CYZERO=(-YI(1025)/YI(1026))
ISTOP=8.*EN(LAST+2)+1
IF ISTOP.GT.1024 ISTOP=1024
FVAL=EN(LAST+1)
DELTA=EN(LAST+2)
DO 7 I=1,ISTOP
EN(I)=I-1
DO 10 K=1,I STOP
X=(EN(K)-FYAL)/DELT
Y=(YI(K)-YI(1025))/YI(1026)
ASDF7626
ASDF7627
ASDF7628
ASDF7629
ASDF7630
ASDF7631
ASDF7632
ASDF7633
ASDF7634
ASDF7635
ASDF7636
ASDF7637
ASDF7638
ASDF7639
ASDF7640
ASDF7641
ASDF7642
ASDF7643
ASDF7644
ASDF7645
ASDF7646
ASDF7647
ASDF7648
ASDF7649
ASDF7650
ASDF7651
ASDF7652
ASDF7653
ASDF7654
ASDF7655
ASDF7656
ASDF7657
ASDF7658
ASDF7659
ASDF7660
ASDF7661
ASDF7662
ASDF7663
ASDF7664
ASDF7665
ASDF7666
ASDF7667
ASDF7668
ASDF7669
ASDF7670
ASDF7671
ASDF7672
ASDF7673
ASDF7674

```

```

IF(Y.GE.YZERO.AND.ISTOP.LE.80)CALL SYMBOL(X,Y,.1,180.,-1)
IF(Y.LT.YZERO.AND.ISTOP.LE.80)CALL SYMBOL(X,Y,.1,1,0.,-1)
CALL PLOT(X,Y,+3)
CALL PLOT(X,Y,0.)CALL PLOT(X,Y,+2)
10 IF(YZERO.GE.0.)CALL PLOT(X,Y,0.)
IF(YZERO.LT.0.)GOTO 999
CALL PLOT(X,YZERO,+3)
CALL PLOT(X,YZERO,+2)
CALL PLOT(X,YZERO,-2)
CALL PLOT(X,YZERO,-2)
NUMPLT=NUMPLT+1
RETURN
END

SUBROUTINE PLTSTP(IAST,FLTRGN,NUMPLT)
C* THIS SUBROUTINE PLOTS THE UNIT STEP RESPONSE
C* COMMON /IMPUIS/YI(1026),YS(1026),EN(1026)
CALL BOX(1FLTRGN,NUMPLT)
DD(5)=I-1
EN(5)=I-1
CALL SCALE(EN(8,IAST+1))
CALL AXIS(2.179,2.2012,13)
HSTEP RESPONSE,+13,5.,90.,YS(1025),
XYS(1026)
CALL AXIS(2.179,2.2012,1HN,-1,8.,0.,EN(LAST+1),EN(LAST+2))
CALL PLOT(2.179,2.2012,-3)
YZERO=(-YS(I025)/YS(I026))
ISTOP=8.*EN(LAST+2)+1.5
IF(ISTOP>1024)ISTOP=1024
FVAL=EN(LAST+1)
DELT=EN(LAST+2)
DO 7 I=1,ISTOP
EN(5)=I-1
DO 10 K=1,ISTOP/DELTA
X=(EN(K)-FVAL)/DELTA
Y=(YS(K)-YS(1025))/S(1026)
IF(ISTOP.LE.80)CALL SYMBOL(X,Y,.1,180.,-1)
CALL PLOT(X,Y,+3)
CALL PLOT(X,Y,0.)CALL PLOT(X,Y,+2)
10 IF(YZERO.GE.0.)GOTO 999
CALL PLOT(X,YZERO,+3)
CALL PLOT(X,YZERO,+2)
CALL PLOT(X,YZERO,-2)
CALL PLOT(X,YZERO,-2)
NUMPLT=NUMPLT+1
RETURN
END

```

```

ASDF7722
ASDF7724
ASDF7725
ASDF7726
ASDF7727
ASDF7728
ASDF7729
ASDF7730
ASDF7731
ASDF7732
ASDF7733
ASDF7734
ASDF7735
ASDF7736
ASDF7737
ASDF7738
ASDF7739
ASDF7740
ASDF7741
ASDF7742
ASDF7743
ASDF7744
ASDF7745
ASDF7746
ASDF7747
ASDF7748
ASDF7749
ASDF7750
ASDF7751
ASDF7752
ASDF7753
ASDF7754
ASDF7755
ASDF7756
ASDF7757
ASDF7758
ASDF7759
ASDF7760
ASDF7761
ASDF7762
ASDF7763
ASDF7764
ASDF7765
ASDF7766
ASDF7767
ASDF7768
ASDF7769

SUBROUTINE PLTTRF(IFNCTN,ITYPE,FLTRGN,NUMPLT)

C* THIS SUBROUTINE PLOTS THE PHASE AND
C* MAGNITUDE OF THE TRANSFER FUNCTION
C*
COMMON /FREQ/YP(1026),YM(1026),PI(1026),YMDB(1026)
DO 10 K=1,1024
PI(K)=FLOAT((K-1)*3.14159)/1024.
10 CALL BOX(1,FLTRGN,NUMPLT)
CALL SCALE(P18*1.024,+1)
CALL AXIS(2.179*2.2012,-7.8,0.,PI(1025)+PI(1026))
IF(IFNCTN.EQ.4)GO TO 30
CALL SCALE(2.1024,+1)
CALL AXIS(2.179*2.2012,-24,5.,90.)
XYP(1025)=YP(1026)
XCALL PLOT(2.179*2.2012,-3)
CALL LINE(PI,YP,1024,1,0,0)
GO TO 40
IF(ITYPE.EQ.2)GO TO 50
CALL AXIS(2.179,2.2012,17,MAGNITUDE OF H(Z),+17.5,90.,YM(1025),
YM(1026))
CALL PLOT(2.179*2.2012,-3)
CALL LINE(PI,Y4,1024,1,0,0)
GO TO 60
50 CALL AXIS(2.179*2.2012,22,MAGNITUDE OF H(Z) (DB),
X+22.5,90.,YMDB(1025)+YMDB(1026))
CALL PLOT(2.179*2.2012,-3)
CALL LINE(PI,YMDB,1024,1,0,0)
CALL PLOT(2.179,-2.2012,-3)
NUMPLT=NUMPLT+1
RETURN
END

SUBROUTINE BOX(I,FLTRGN,NUMPLT)
C* THIS SUBROUTINE DRAWS THE BOUNDARIES OF
C* THE PLOTTING AREAS
C*
DIMENSION CORNER(6,2)
DATA CORNER/1.0,13.,0.,13.,0.,1.,10.,-10.,10.,-10./
CALL FACTOR(.89)
CALL PLOT(CORNER(NUMPLT,1),CORNER(NUMPLT,2),-3)
CALL PLOT(12.375,0.,5625,+2)
CALL PLOT(12.375,9.5625,+2)
CALL PLOT(0.,9.5625,+2)
IF(I.E2.0)RETURN
CALL SYMBOL(7.4922,1.83,.139,14HF FILTER GAIN = ,0.,+14)

```

CALL NUMBER(9.4297,1.83,139,FLTRGN,0.0+5)  
RETURN  
END

ASDF7770  
ASDF7771  
ASDF7772  
ASDF7773

## REFERENCES

- 1 Blackman, R. B., Data Smoothing and Processing, p. 76, Addison-Wesley, 1965.
- 2 Chen, Chi-Tsong, One-Dimensional Digital Signal Processing, p. 289-331, Marcel Dekker, 1979.
- 3 Hamming, R. W., Digital Filters, p. 213-219, Prentice Hall, 1977.
- 4 Naval Postgraduate School, Users Manual, p. 3.1-4.69, 1979.
- 5 Oppenheim A. V. and Schafer R. W., Digital Signal Processing, 148-181, Prentice Hall, 1975.
- 6 Rabiner, L. R. and Gold, B., Theory and Application of Digital Signal Processing, 40-354, Prentice Hall, 1975.
- 7 Raney, S. D., Using the Versatec Plotter at NPS, 1979.
- 8 Stanley, W. D., Digital Signal Processing, pp. 88-101, Reston, 1975.
- 9 Tektronix, 4012 Computer Display Terminal Users Instruction Manual, 1973.
- 10 Tektronix, Plot 10 Terminal Control System User's Manual, 1977.

INITIAL DISTRIBUTION LIST

|   | No. Copies |
|---|------------|
| 1. Defense Technical Information Center<br>Cameron Station<br>Alexandria, Virginia 22314  | 2          |
| 2. Library, Code 0142<br>Naval Postgraduate School<br>Monterey, California 93940  | 2          |
| 3. Department Chairman, Code 62<br>Department Of Electrical Engineering<br>Naval Postgraduate School<br>Monterey, California 93940        | 1          |
| 4. Professor D. C. Kirk, Code 62Ki<br>Department Of Electrical Engineering<br>Naval Postgraduate School<br>Monterey, California 93940     | 10         |
| 5. Professor S. Parker, Code 62Px<br>Department Of Electrical Engineering<br>Naval Postgraduate School<br>Monterey, California 93940      | 1          |
| 6. Professor R. D. Strum, Code 62St<br>Department of Electrical Engineering<br>Naval Postgraduate School<br>Monterey, California 93940    | 1          |
| 7. Professor Robert H. Nunn, Code 69Nm<br>Department of Mechanical Engineering<br>Naval Postgraduate School<br>Monterey, California 93940 | 1          |
| 8. Ms. Jane Foust, Code 0141<br>Naval Postgraduate School<br>Monterey, California 93940   | 1          |
| 9. Captain Gerald S. Doyle, USA<br>Orchard Drive<br>Chester, New Jersey 07930   | 2          |